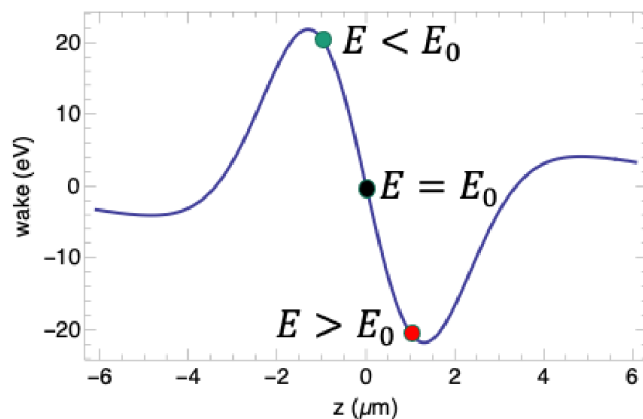


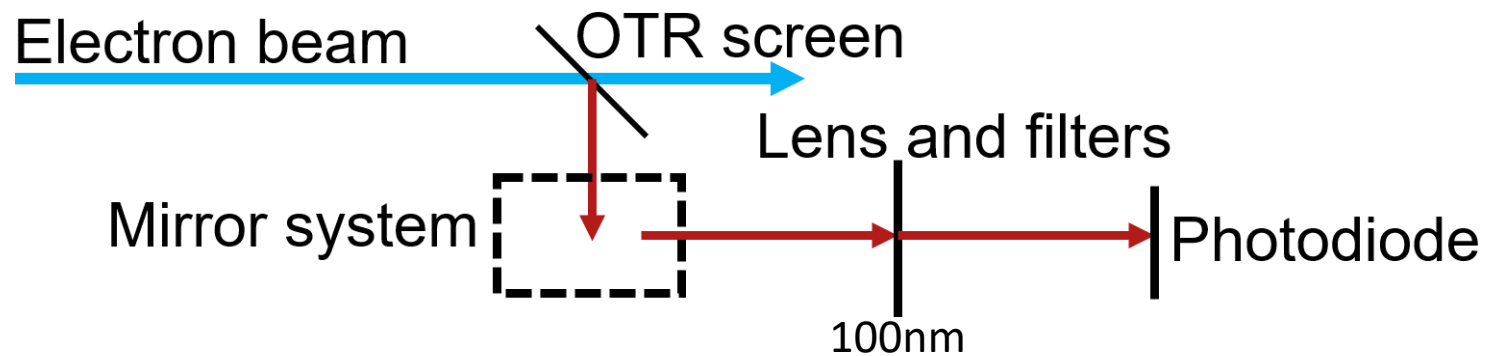


Noise in Intense Electron Bunches at FAST

S. Klado[†], S. Nagaitsev, J. Ruan, A. Lumpkin, R. Thurman-Keup, A. Saewert, D. Broemmelsiek, J. Jarvis, Y.-K. Kim, Z. Huang



0 – 6 μm

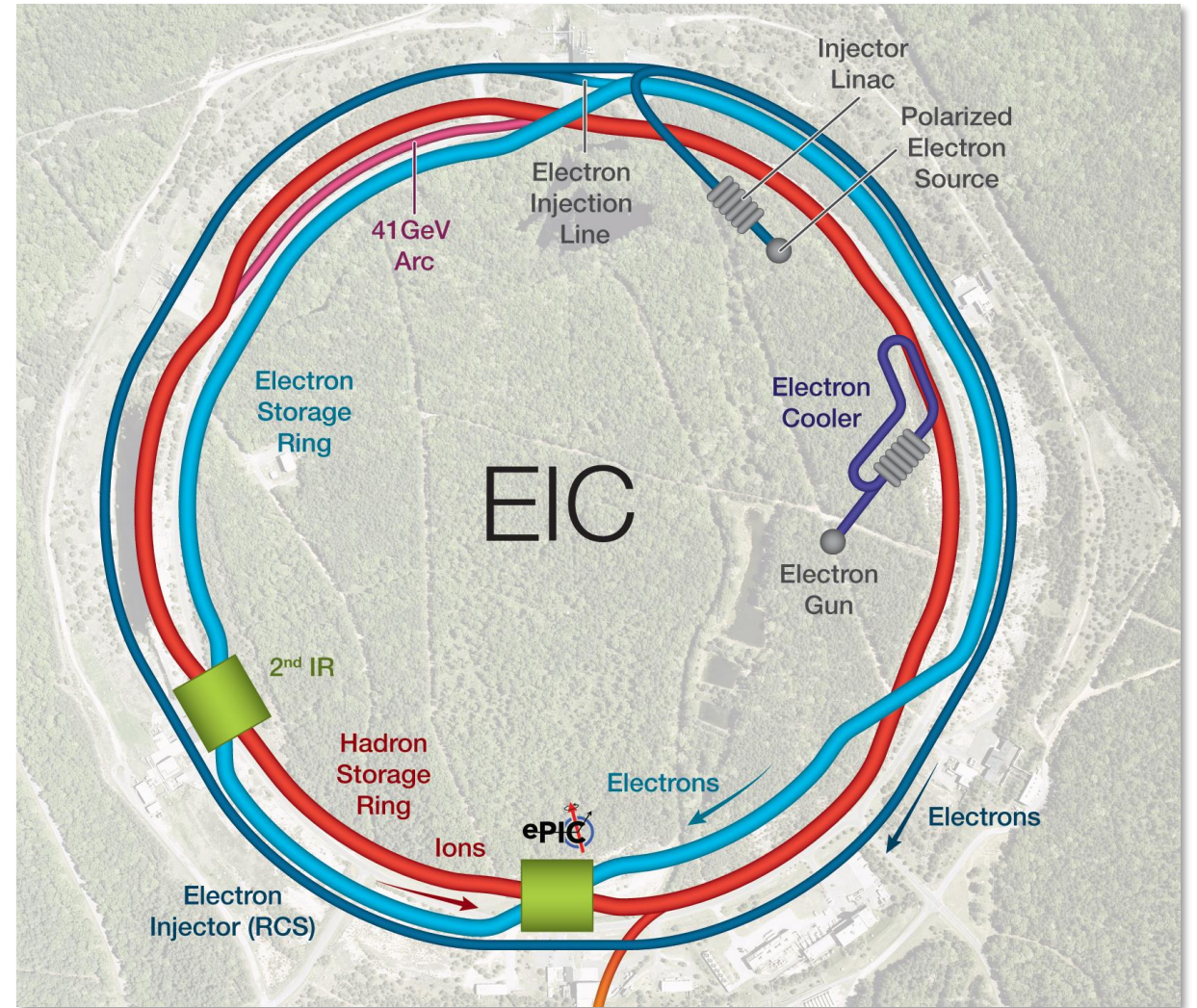


Electron-Ion Collider

- High luminosity: $L = 10^{33}$ to $10^{34} \text{ cm}^{-2}\text{sec}^{-1}$ - a factor 100 to 1000 beyond HERA

	Electrons	Protons
Beam energies	2.5 - 18 GeV	41- 275 GeV
Center of mass energy range	$E_{\text{cm}} = 20\text{-}140 \text{ GeV}$	

	Electrons	Protons
Beam energies	10 GeV	275 GeV
Center of mass energy	$E_{\text{cm}} = 105 \text{ GeV}$	
number of bunches	nb =1160	
crossing angle	25 mrad	
Bunch Charge	$1.7 \cdot 10^{11}e$	$0.7 \cdot 10^{11}e$
Total beam current	2.5 A	1 A
Beam emittance, horizontal	20 nm	9.5 nm
Beam emittance, vertical	1.2 nm	1.5 nm
β - function at IP, horizontal	43 cm	90 cm
β - function at IP, vertical	5 cm	4 cm
Beam-beam tuneshift, horizontal	0.073	0.014
Beam-beam tuneshift, vertical	0.1	0.007
Luminosity at $E_{\text{cm}} = 105 \text{ GeV}$	$1 \cdot 10^{34} \text{ cm}^{-2}\text{s}^{-1}$	



Beam Cooling

| Transverse momentum energy growth:

Source: longitudinal degree of freedom.

Coupling to transverse degree **processes:**

- Scattering (intra-beam, beam-beam, residual gas)
- Improper bending and/or focusing at injection
- Interaction with beam's environment (e.g. wake fields)
- Space-charge effects
- Secondary and tertiary beams

Necessary: $\langle p_{\perp} \rangle \sim 10^{-4} \langle p_{\parallel} \rangle$

Cooling is a reduction in the phase space occupied by the beam (for the same number of particles)

- The figure of merit – beam emittance

$$\varepsilon_{x,n} = \beta\gamma \left(\langle x^2 \rangle \langle \theta_x^2 \rangle - \langle x\theta_x \rangle^2 \right)^{1/2}$$

$$\theta_x = \frac{p_x}{\beta\gamma M c}$$

Beam Cooling

- At 275 GeV, IBS times are: H/L = 1.5/4 hours
- IBS heating rate scales as $\lambda_{\perp} \sim \frac{1}{\gamma^{1.5}}$

| Thus, the hadron cooling system must provide ~1-2 hour horizontal cooling time to prevent emittance blowup and conserve luminosity

- We are calling it Strong Hadron Cooling

Two basic methods employed for hadron cooling today:

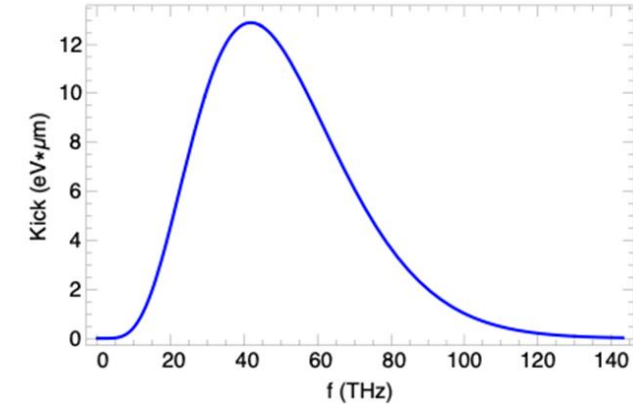
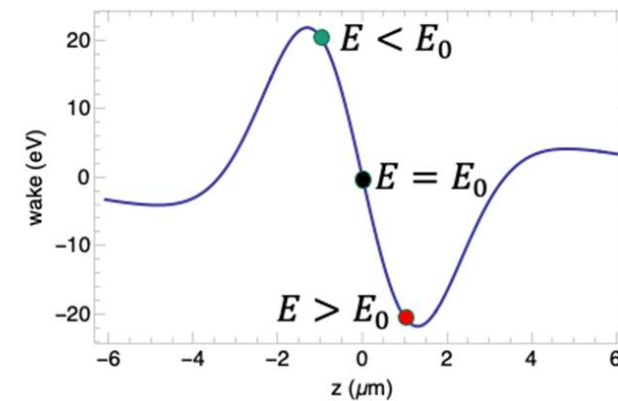
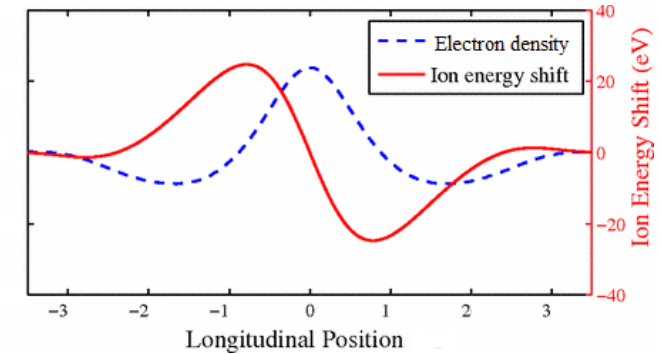
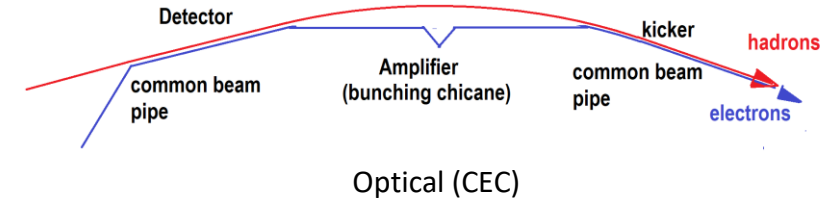
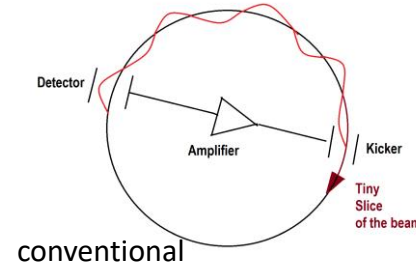
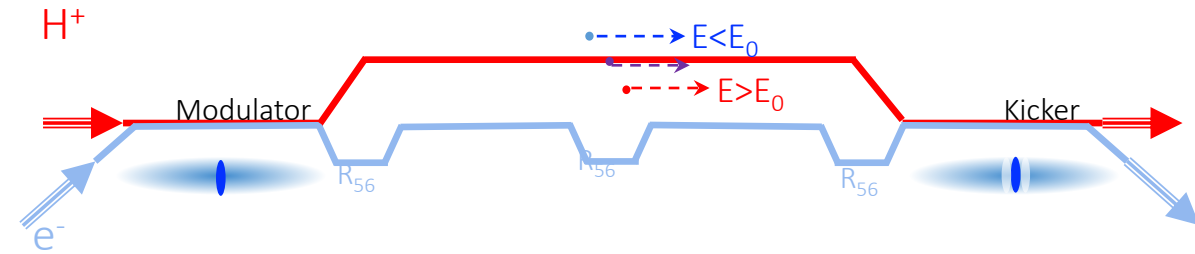
Electron cooling – energy exchange

- Many low-energy proton/ion rings.
- Highest hadron beam energy to date - 8.9 GeV at Fermilab
- Cooling rate: $\lambda_{\perp} \sim \frac{1}{\gamma^{2.5}}$

Stochastic cooling (1984 Nobel Prize in Physics)

- CERN, Fermilab, GSI, RHIC, etc.

Optical Stochastic cooling



Concept:

Coherent electron cooling with microbunching amplification

- Type of stochastic cooling based on transit time between the modulator and the kicker
- Typical bandwidth of **~40 THz** (conventional SC **~10 GHz**)
- **This is a longitudinal-only cooling scheme.** Cooling in x and y requires coupling/sharing of cooling.
- Achievable cooling times of about 1 hour for 275 GeV protons

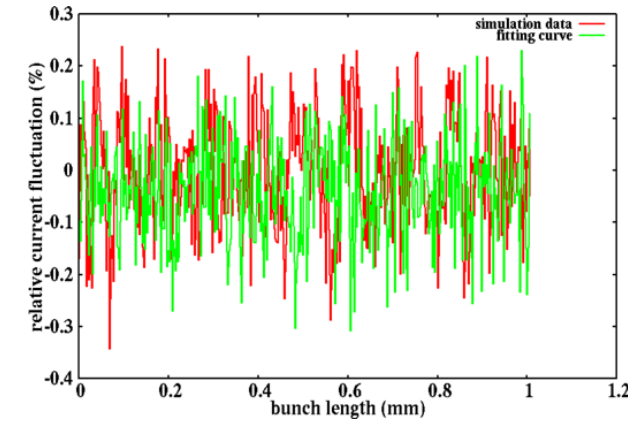
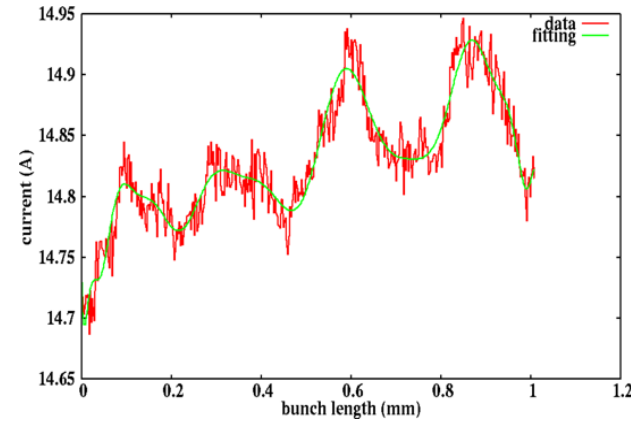
Electron beam noise

Noise = beam density fluctuations above (Poissonian) **shot noise**, $F = 1$

$$F = \frac{\text{var}(\mathcal{N})}{\langle \mathcal{N} \rangle}$$

Fano factor

| We would like to confirm that for the ERL electron bunches $F < 2$ at $\lambda \sim 3\mu\text{m}$

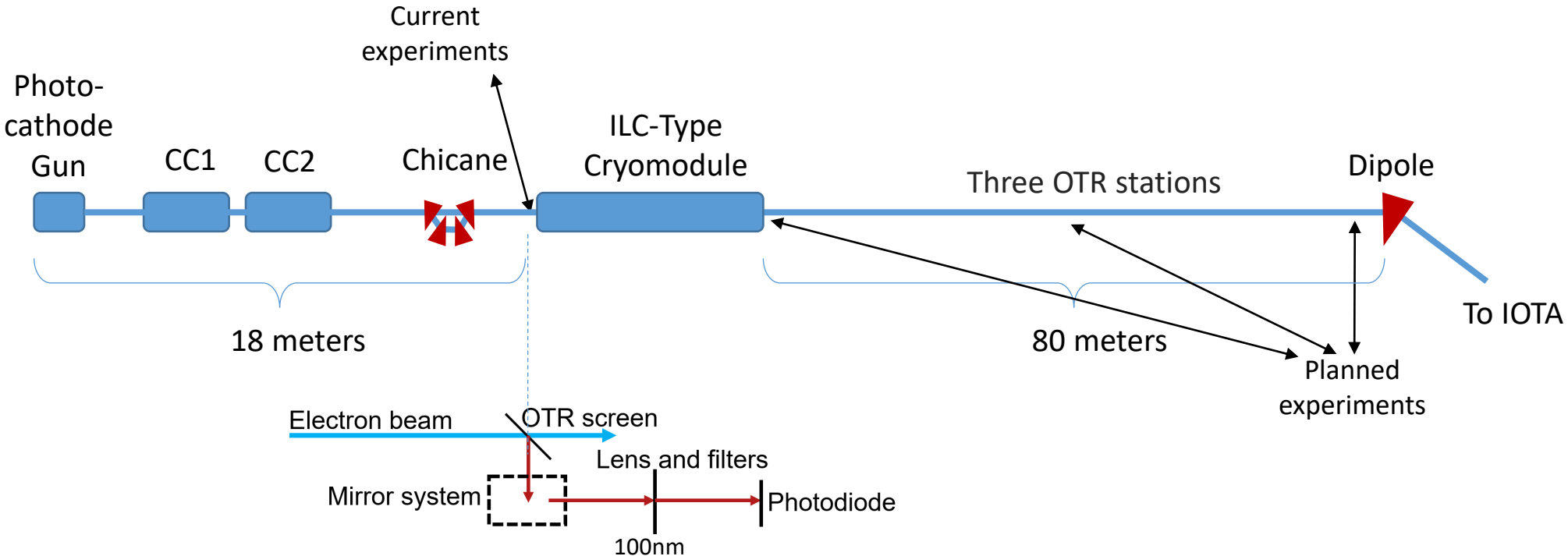


- IMPACT simulation (LBNL): energy spread, emittance, and bunch length matched well to GPT results
- Observed > 250 μm modulation with noise amplitude 2x shot noise. It will not be amplified in the cooler.
- 250 μm modulation will **not affect the diffusion rate**
- Current fluctuation through the linac and the merger is **close to the shot noise level**

Experiment. EIC and FAST

| Beam spectrum ↔ Transition Radiation (TR) spectrum

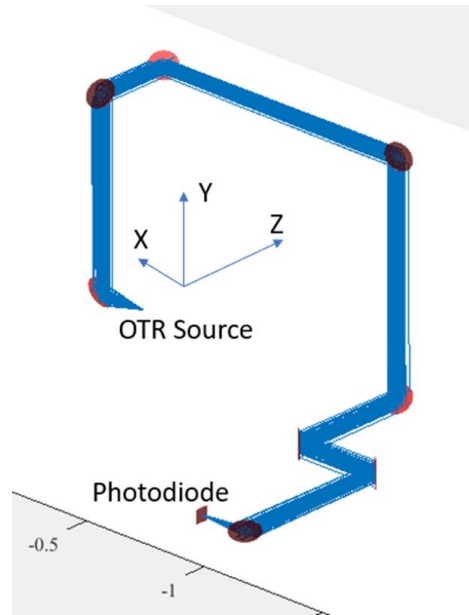
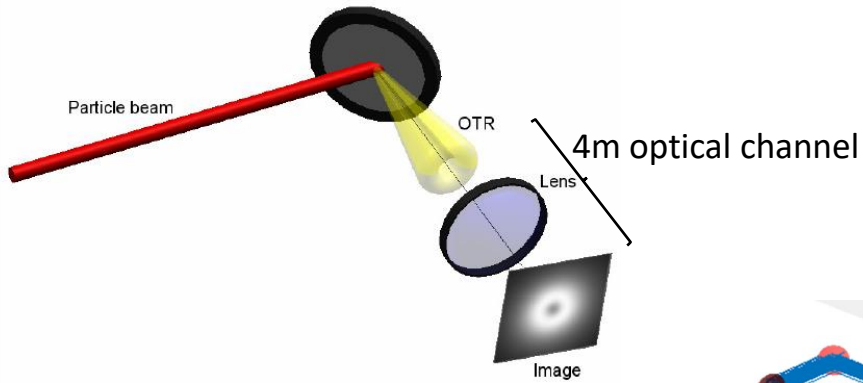
	FAST	EIC (100 GeV)	EIC (275 GeV)	Current experiment
Electron beam energy	50 – 300 MeV	50 MeV	137 MeV	32 MeV
Bunch charge	0 – 3 nC	1 nC	1 nC	0.2 – 1.1 nC
Emittance (norm, rms)	~3 μm (at 1 nC)	2.8 μm	2.8 μm	
Bunch length	0.3 – 20 mm	9 mm	8 mm	0.15-5 mm
Drift section (amplifier)	80 m	100 m	100 m	



Optical Transition Radiation. Its registration

$$\frac{dI}{d\omega d\Omega} = \frac{Z_0 e^2}{4\pi^3} |n \times \beta|^2 \left[\frac{1}{1 - (\beta n)^2} \right]^2$$

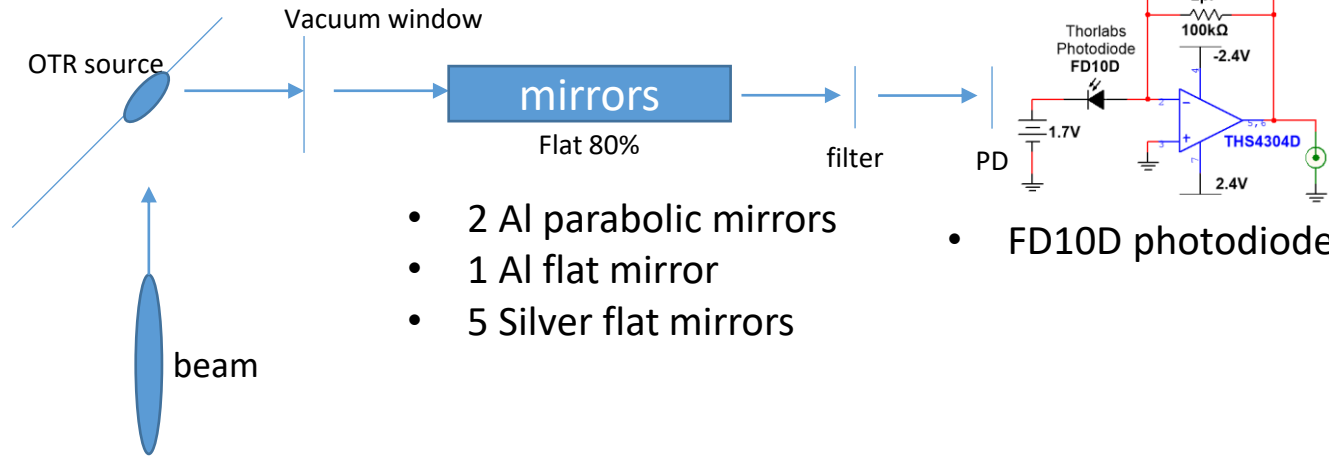
- One particle



- Beam size dependence is determined by the PD size ($\gamma \gg 1$)

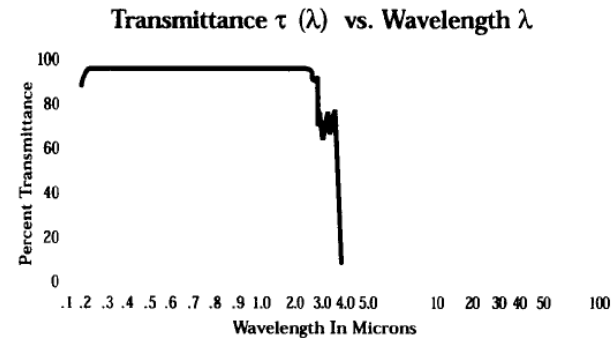
$$\frac{dI}{d\omega d\Omega} \sim N \left(1 - \exp\left(-\frac{a^2}{2\sigma^2}\right) \right)$$

- SiO₂ (fused silica) glass vacuum window

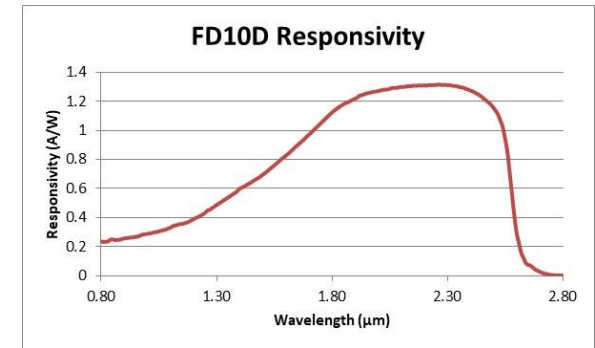


- 2 Al parabolic mirrors
- 1 Al flat mirror
- 5 Silver flat mirrors

- FD10D photodiode



Vacuum window transmittance

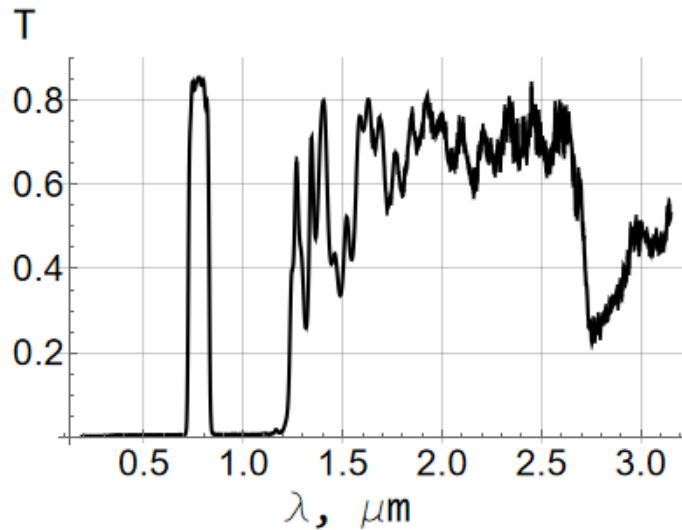


Photodiode responsivity

Data Analysis Flow

Transitions:

- Vacuum window
- Flat and parabolic mirrors
- Filters
- PD responsivity



Filter transmission example

Pass OTR through the light channel (Theory and Experiment)



Compare voltage $U(\lambda)$ for a set of filters (set of single values)



Discrete Homogeneous Fredholm Integral Equation

$$\int T(n, \lambda) \frac{dI}{d\lambda} d\lambda = U(n)$$



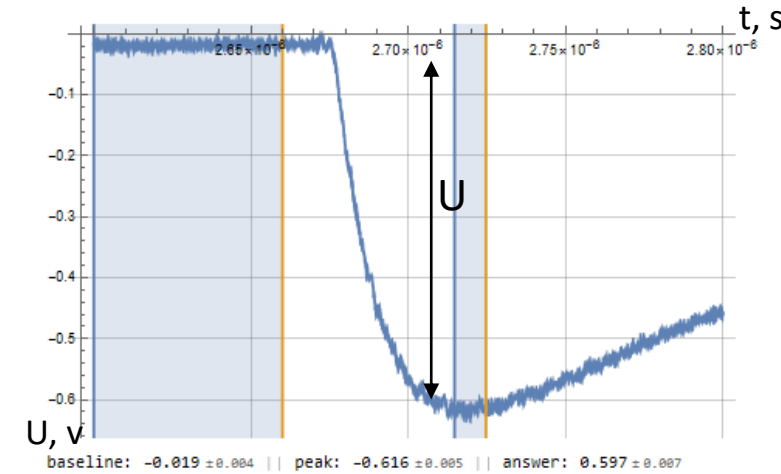
System of integral equations

If filters are narrow-band:

- Integrals are easily evaluated \rightarrow unique solution

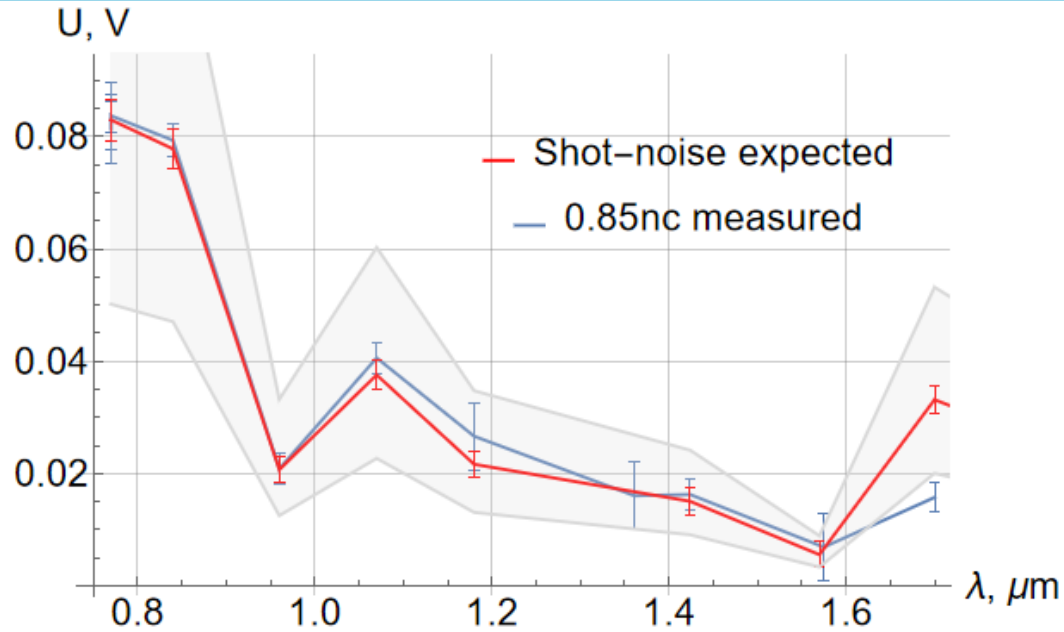
In reality:

- Ambiguous, guessed solution



Averaged scope data (voltage) example

OTR power Theory and Experiment comparison. Low noise



Predicted and Experimental $U(\lambda)$ comparison. 9 filters



! Noise in the system is $F = 1 \div 1.62$

$$\frac{d^2 I}{d\omega d\Omega} = \underbrace{\frac{d^2 I_1}{d\omega d\Omega}}_{\text{Incoherent term}} \left[N + N^2 \underbrace{\left| \int \rho(z) \exp\left(iw \frac{z}{c}\right) dz \right|^2}_{\text{Coherent term}} \right]$$

N – number of particles

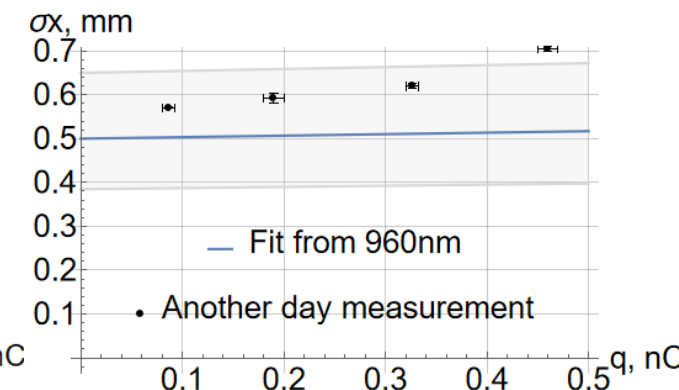
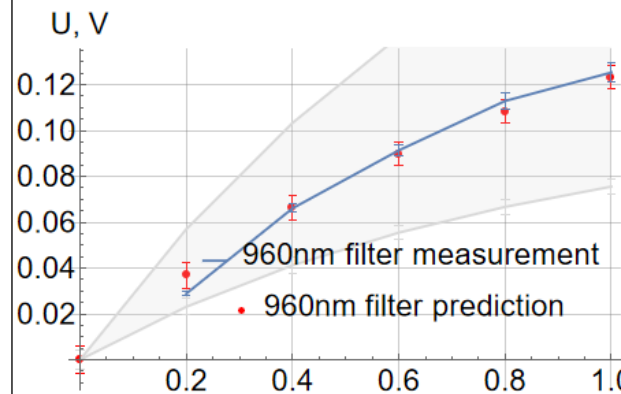
$$\frac{\text{Red}}{\text{Gray}} - 1 = N \left| \int \rho(z) \exp\left(iw \frac{z}{c}\right) dz \right|^2$$

$$\int \rho(z) \exp\left(iw \frac{z}{c}\right) dz = \sqrt{\frac{\text{Red}}{\text{Gray}} - 1} \frac{1}{\sqrt{N}} = \frac{\int \rho(z) \exp\left(iw \frac{z}{c}\right) dz}{\int \rho(z) \exp\left(i0 \frac{z}{c}\right) dz}$$

$$\text{Shot-noise: } \frac{\int \rho(z) \exp\left(iw \frac{z}{c}\right) dz}{\int \rho(z) \exp\left(i0 \frac{z}{c}\right) dz} \approx \frac{1}{1.129 \sqrt{N}}$$

$$F = \sqrt{\frac{\text{Red}}{\text{Gray}} - 1} \frac{1.129}{\sqrt{N}}$$

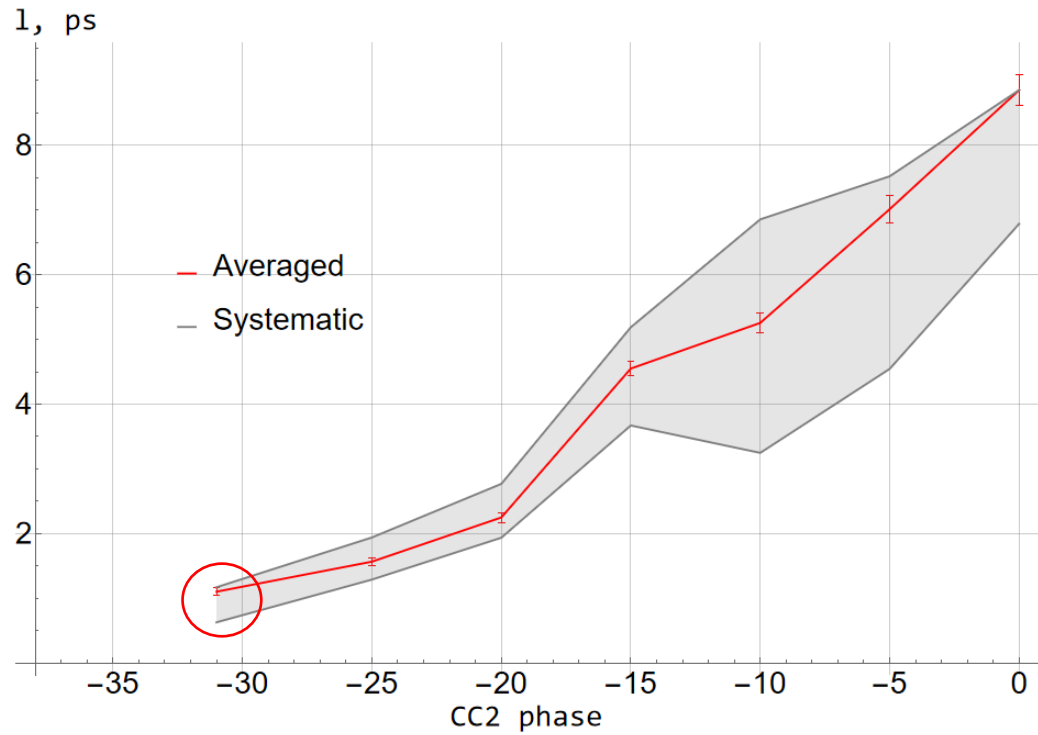
35% σ error \rightarrow 50% U error \rightarrow 62% F error



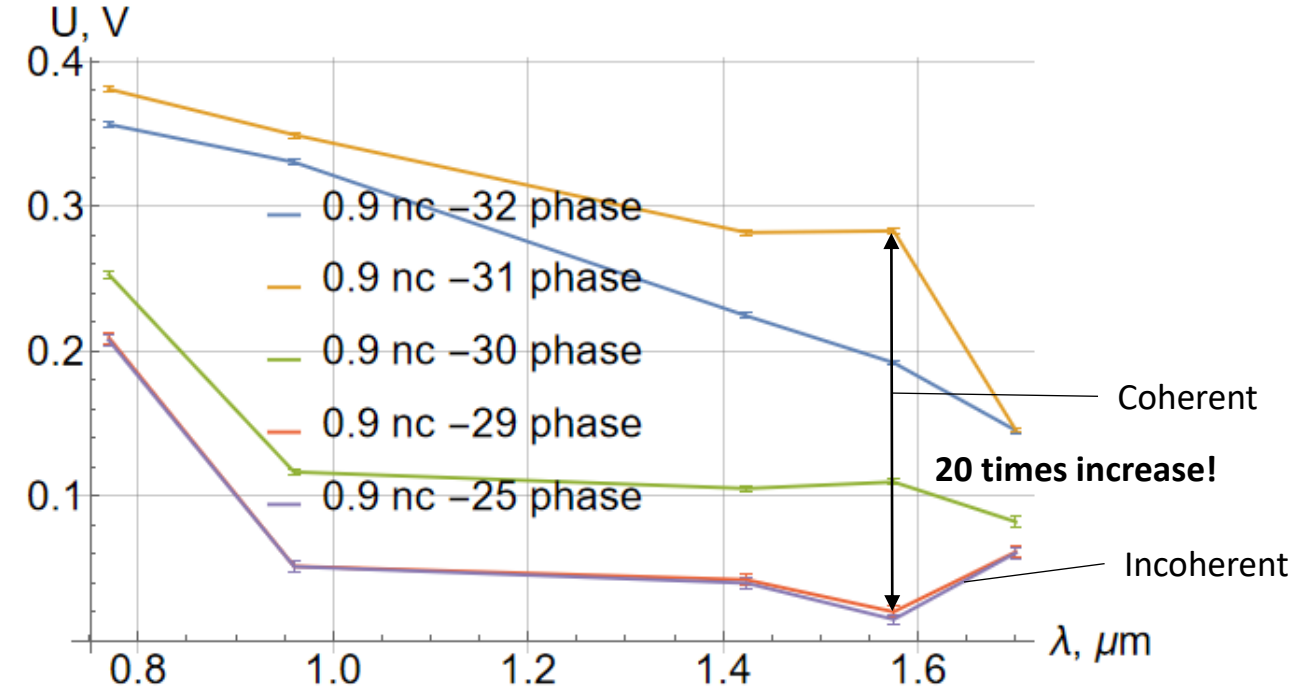
Beam size measurement error in work. Example

Bunch compression

$$\frac{d^2 I}{d\omega d\Omega} = \frac{d^2 I_1}{d\omega d\Omega} \left[N + N^2 \left| \int \rho(z) \exp\left(i\omega \frac{z}{c}\right) dz \right|^2 \right]$$



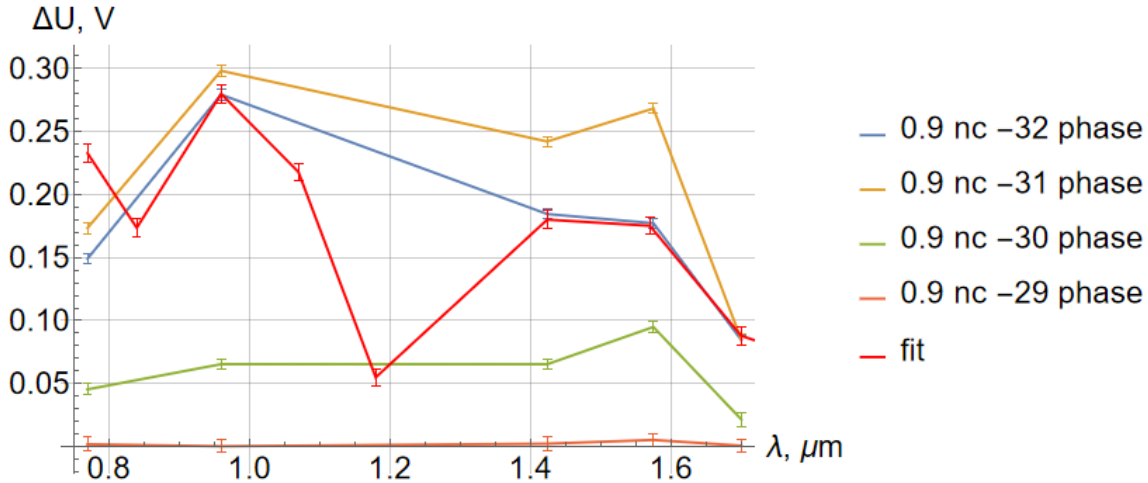
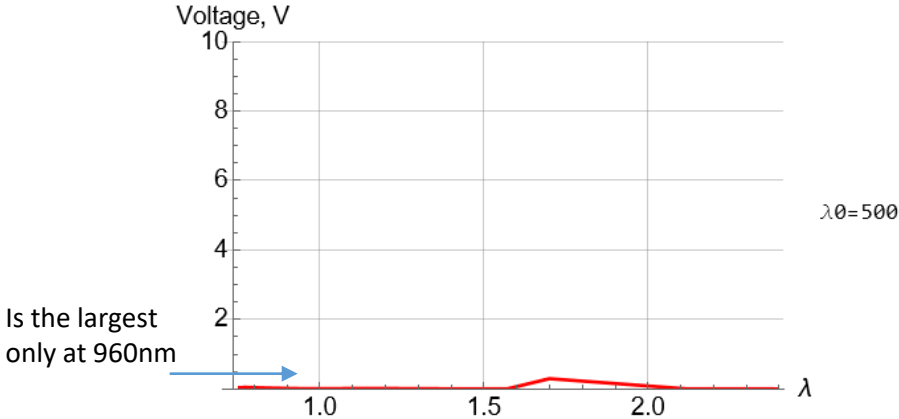
Beam length dependence on CC2 phase.
Interesting region is circled red



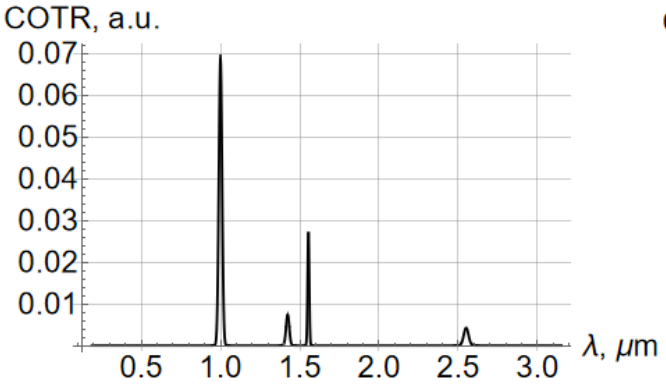
OTR energy per 100-nm BW dependence on wavelength
for different bunch lengths

Fano factor of $\langle F(\lambda) \rangle \sim 3$

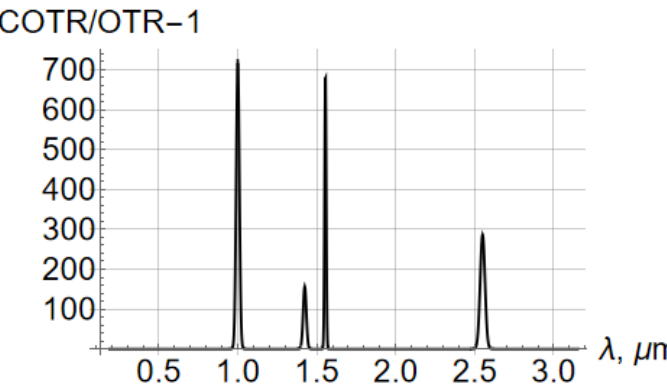
Elevated noise



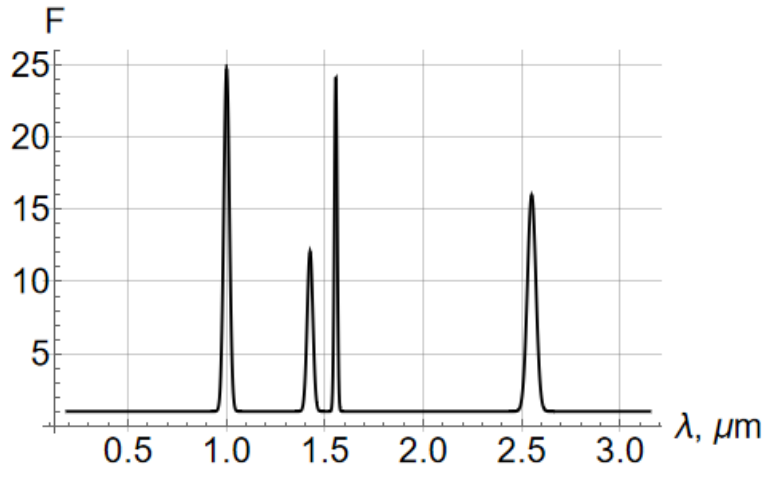
An attempt to fit the elevated noise picture



Additional OTR spectrum when the beam is compressed



$$N \left| \int \rho(z) \exp\left(2\pi i \frac{z}{\lambda}\right) dz \right|^2$$

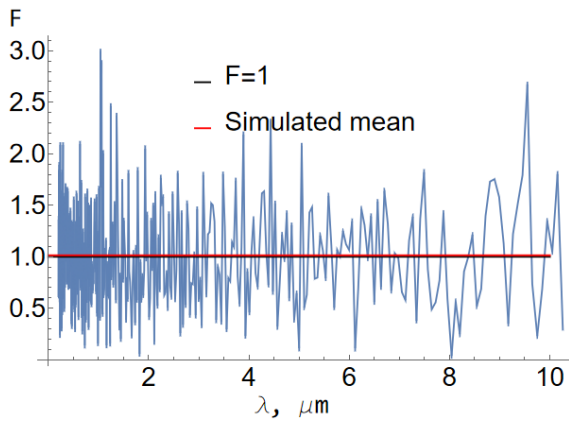


Fano factor

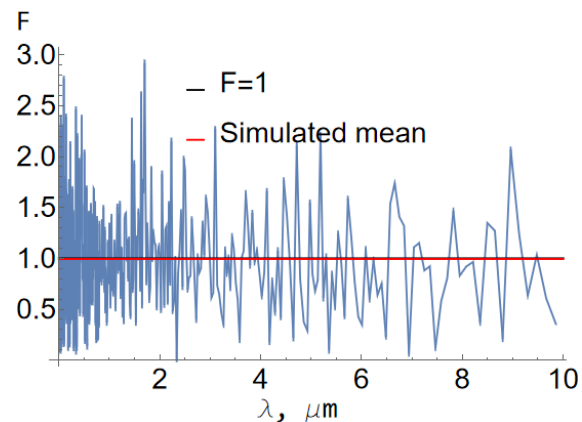
- No COTR at < 0.9 μm
- Peak at 1.5-1.6 μm
- Peak at 0.9-1 μm

Simulations

- ImpactX
- Cross-checked with ASTRA



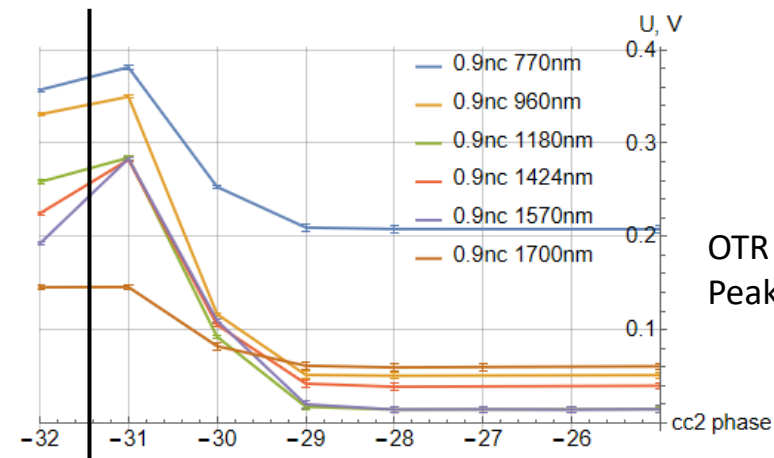
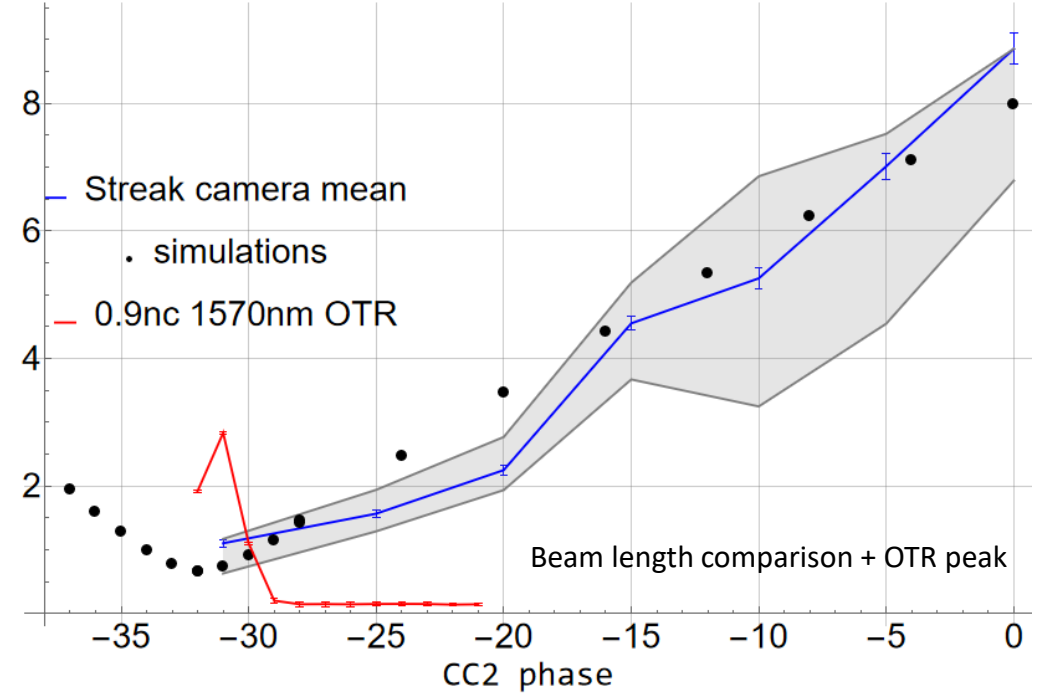
Uncompressed beam



Compressed beam

- No microbunching? Need more accuracy
- Gain plot (with initial distortion) shows the same

Beam length, ps; U, 0.1V



OTR peak on multiple filters.
Peak ~31.4 (from symmetry)

Next steps

Data analysis:

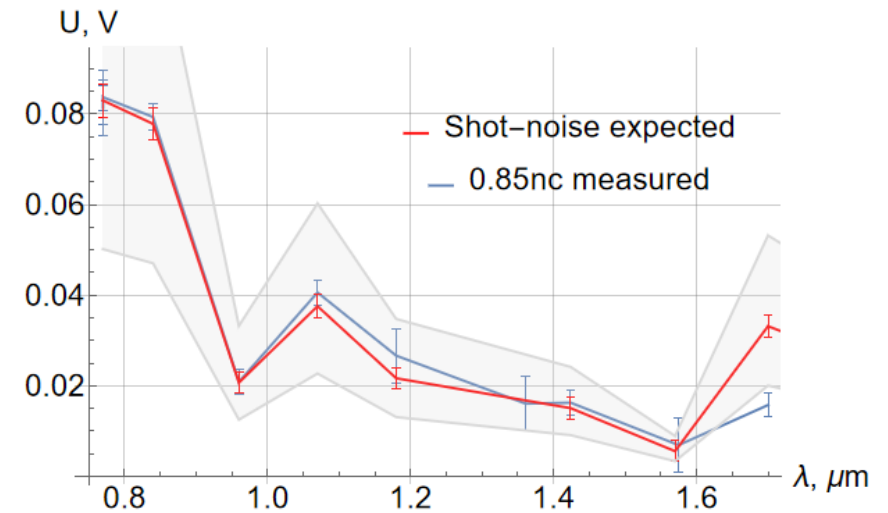
- Fit the elevated noise automatically
- Fit the vacuum window transmission lower edge

Simulations

- Regular tracking:
Beam length vs cc2 phase for the high energy channel
- Microbunching:
Increase accuracy and compare with other tools like GPT

Experiment:

- Perform the experiment with ultimate control of the beam size
- Create additional measurement stations in the high energy line
- Try other filters / neutral density filters to improve the data

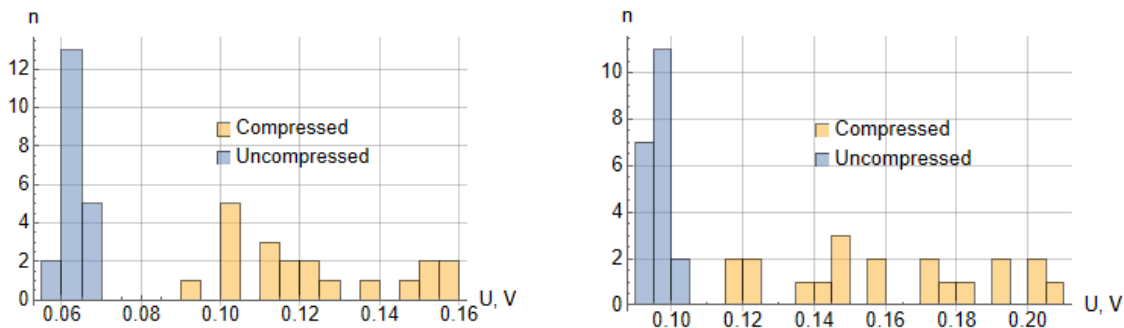
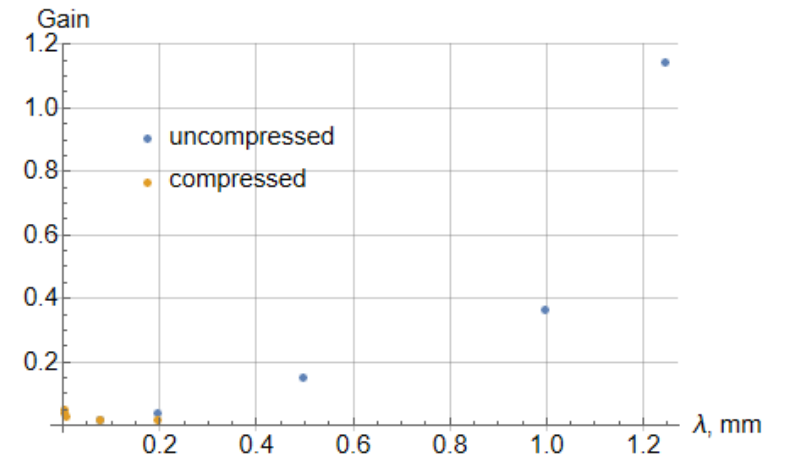


Noise in the system is $F = 1 \div 1.62$

Thank you! Questions time.

EIC features

- Large range of center-of-mass **energies** $E_{\text{cm}} = 29$ to 140 GeV/u
- **Polarized beams** with flexible spin patterns
- Favorable condition for **detector acceptance** such as $p_{\text{T}} = 200$ MeV/c
- Large range of **hadron species**: protons ...Uranium
- Collisions of electrons with **polarized protons and light ions** (^3He , d,...)



Signal fluctuations measurements

Possible discrepancy in beam length experiment vs simulation explanation

