# **Detailed Phase Space Reconstruction** using Neural Networks and **Differentiable Simulations**

Physics and Applications of High Brightness Beams San Sebastián, Spain - June 20th , 2023

Juan Pablo Gonzalez-Aguilera\* (UChicago)

Ryan Roussel, Auralee Edelen, Christopher Mayes, Daniel Ratner (SLAC)

Seongyeol Kim, John Power, Eric Wisniewski (ANL)



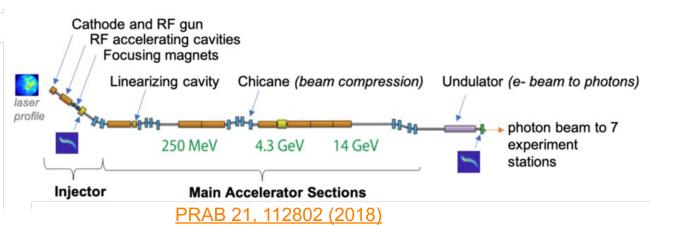


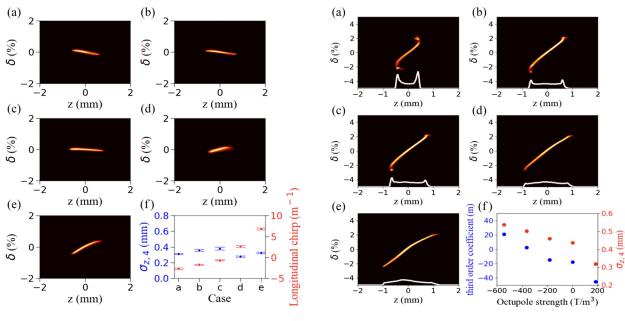






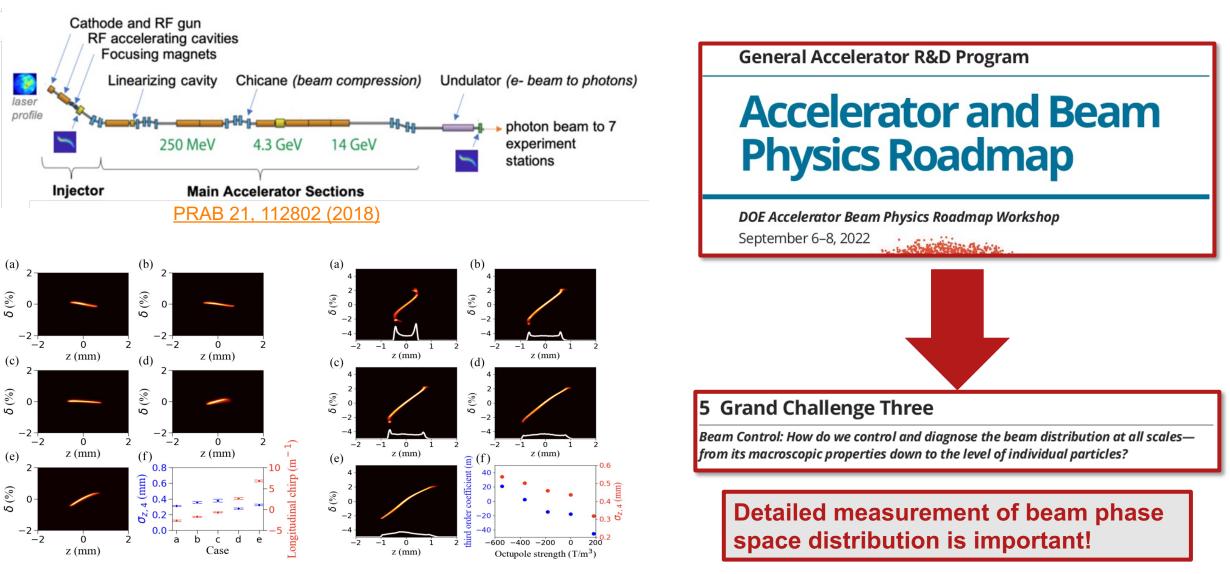
# **Manipulating Beams in Phase Space**



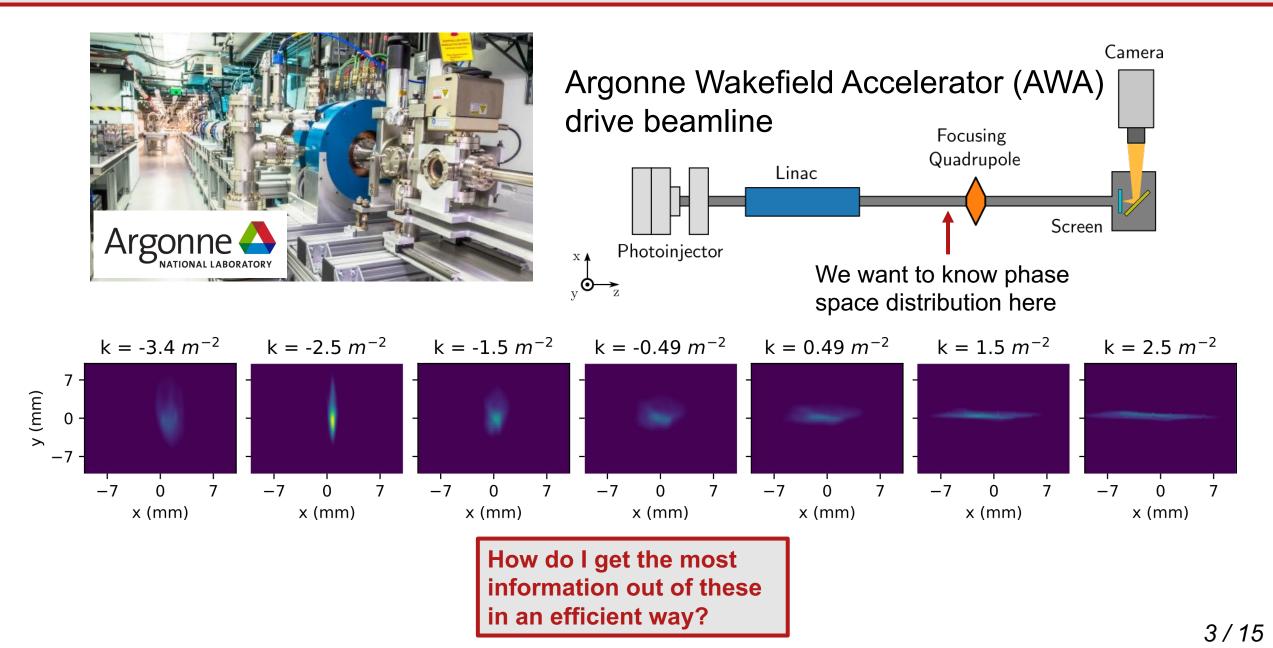


PRL 129, 224801 (2022)

# **Manipulating Beams in Phase Space**



#### **Phase space distribution measurements**



focusing lens

converging

beam

beam

waist

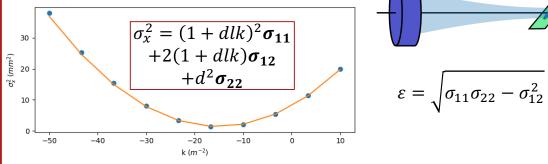
diverging

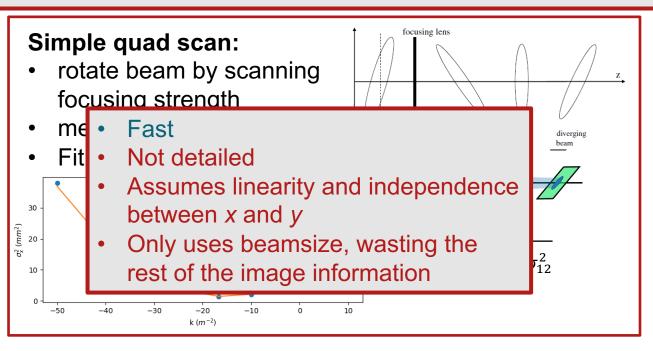
beam

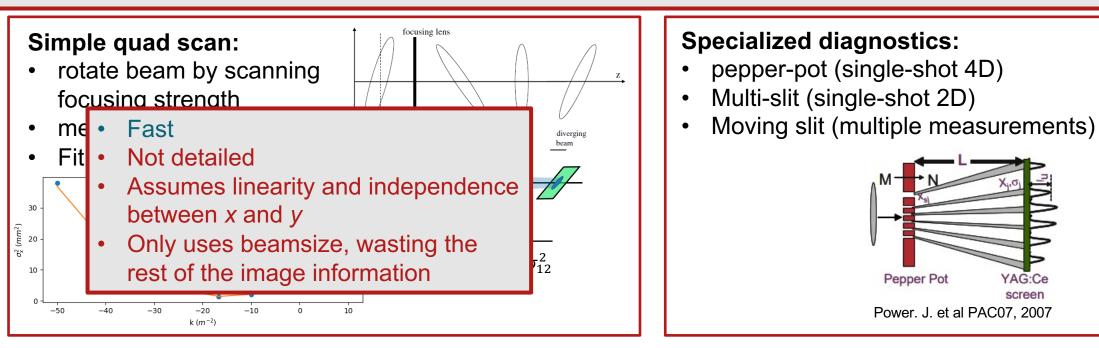
diverging beam

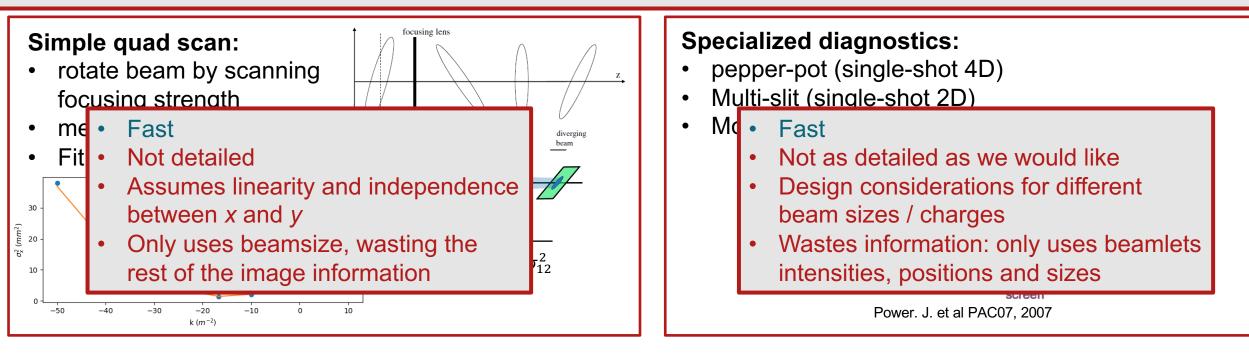


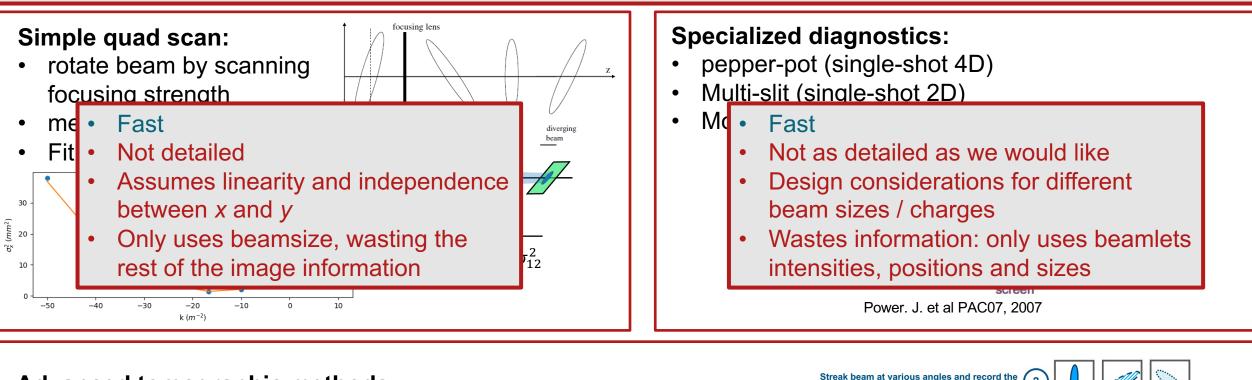
- rotate beam by scanning focusing strength
- measure the beam size
- Fit and solve for  $\varepsilon$

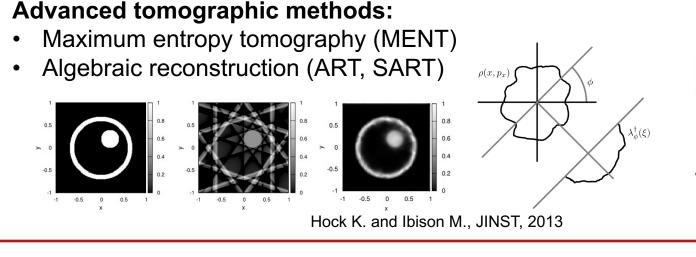


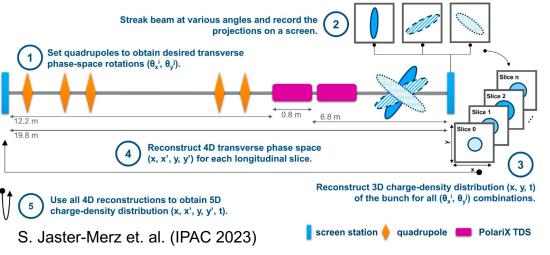


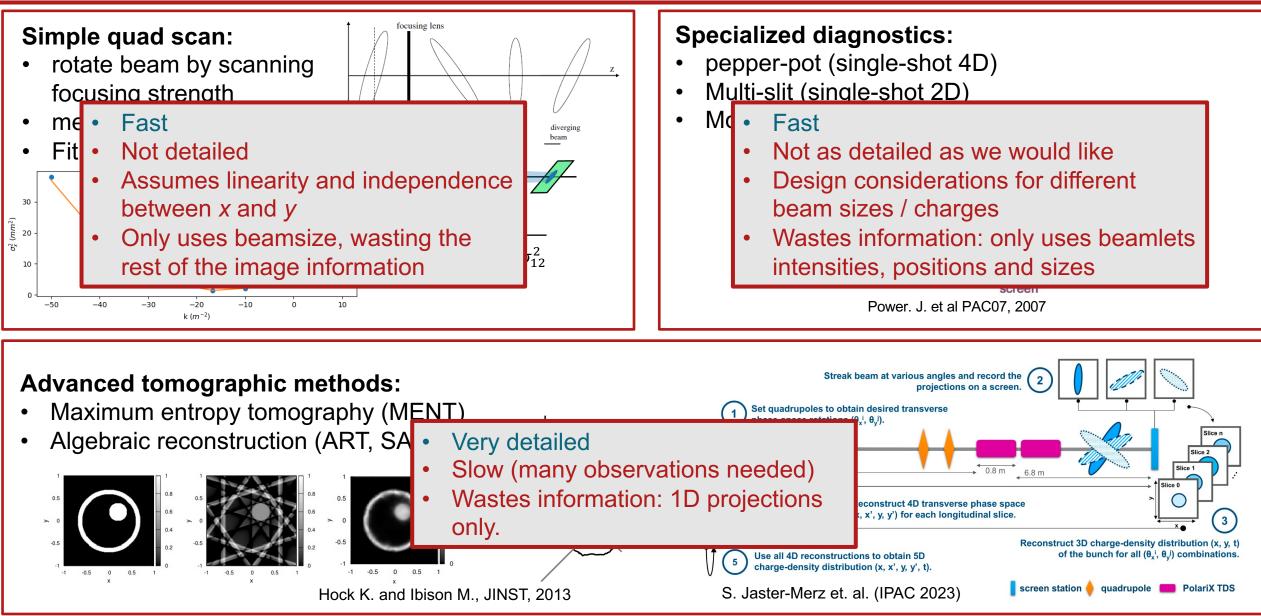




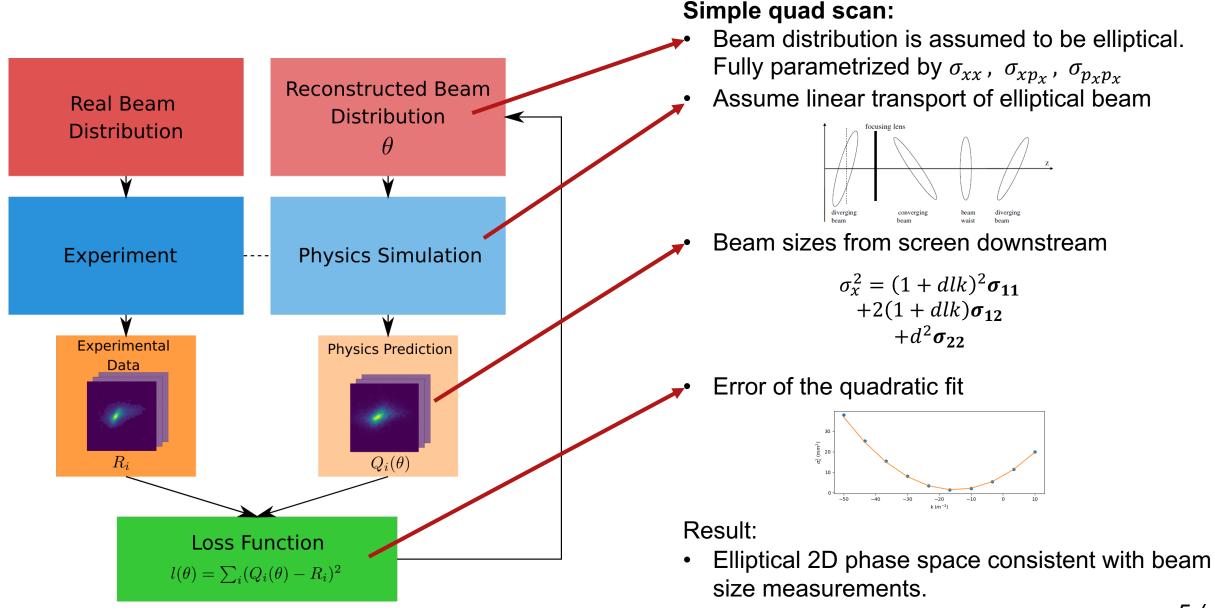




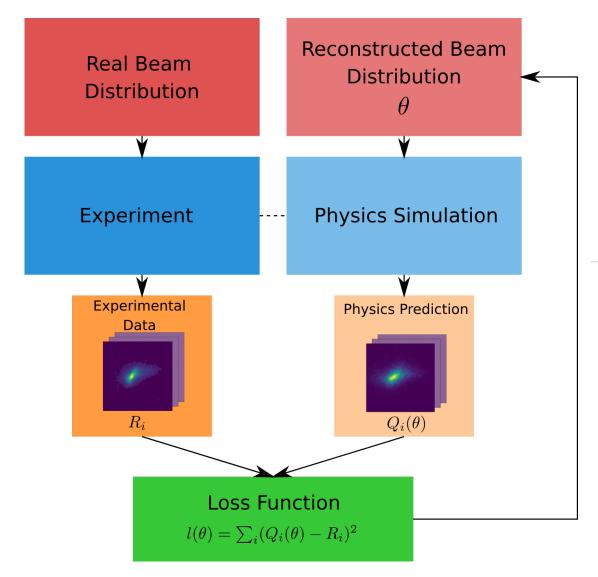




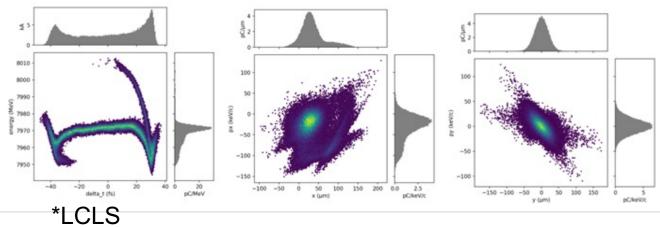
# Phase Space Fitting as optimization problem



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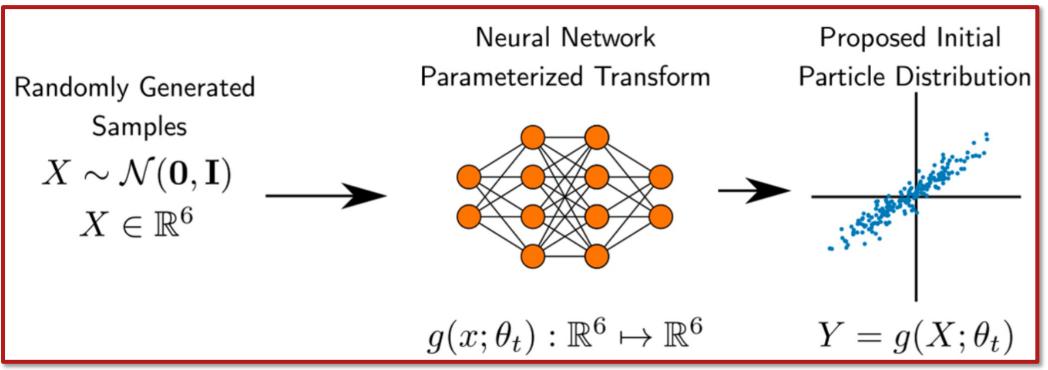
We want more detail:



- How do we **parametrize** the beam 6D phase-space distribution in a a **flexible** and **learnable** way?
- How do we run simulations that support optimization of extremely high dimensional problems (~1k parameters)?

# **Neural Network Parameterization of Beam Distributions**

- 6D phase space distribution parametrization that is
  - flexible
  - learnable



Fully connected NN with ~ O(1k) parameters

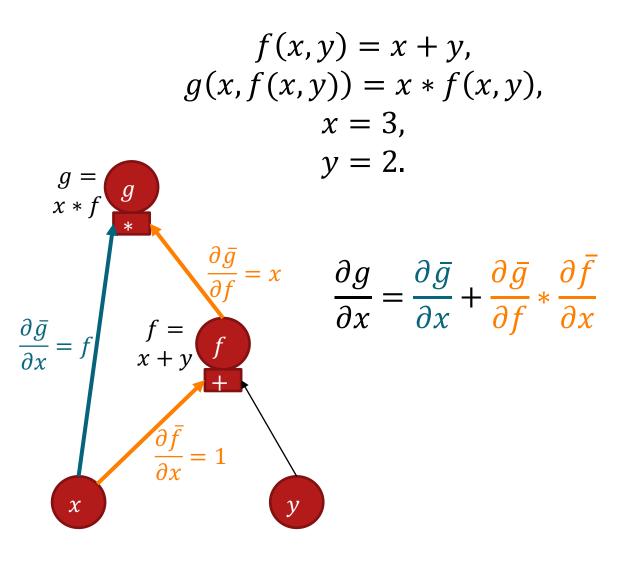
# **Differentiable Simulations (Automatic Differentiation)**

Keep track of derivative information during every calculation step using the chain rule and memory.

Fast and accurate highdimensional gradients

Enables gradient-based optimization of model with respect to all free parameters.

Easily optimize models with >10k free parameters.



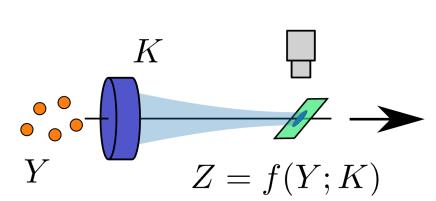
# **Differentiable Simulations (Automatic Differentiation)**

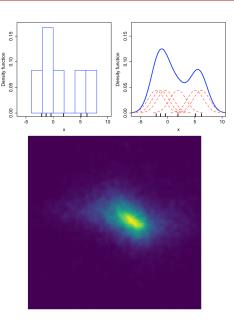
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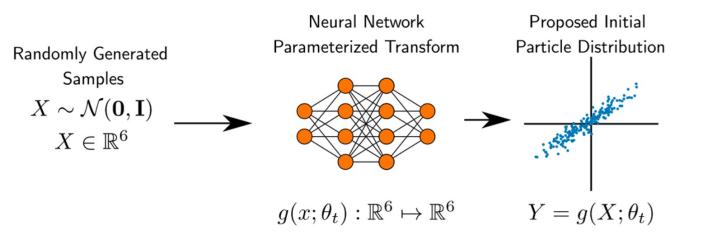
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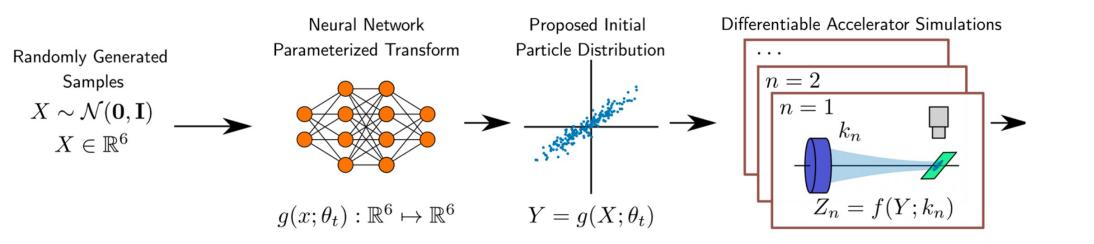


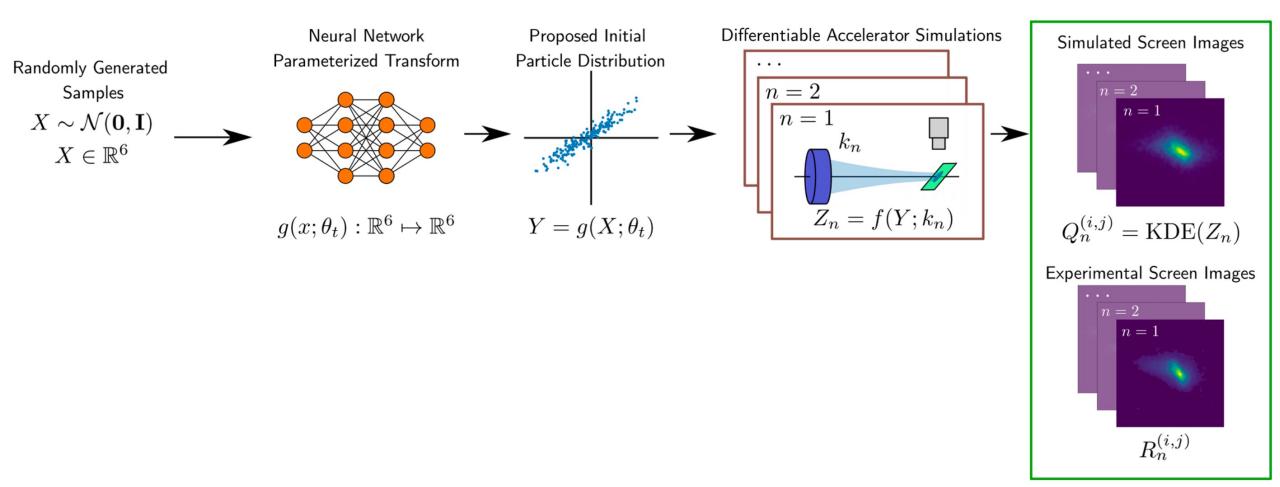


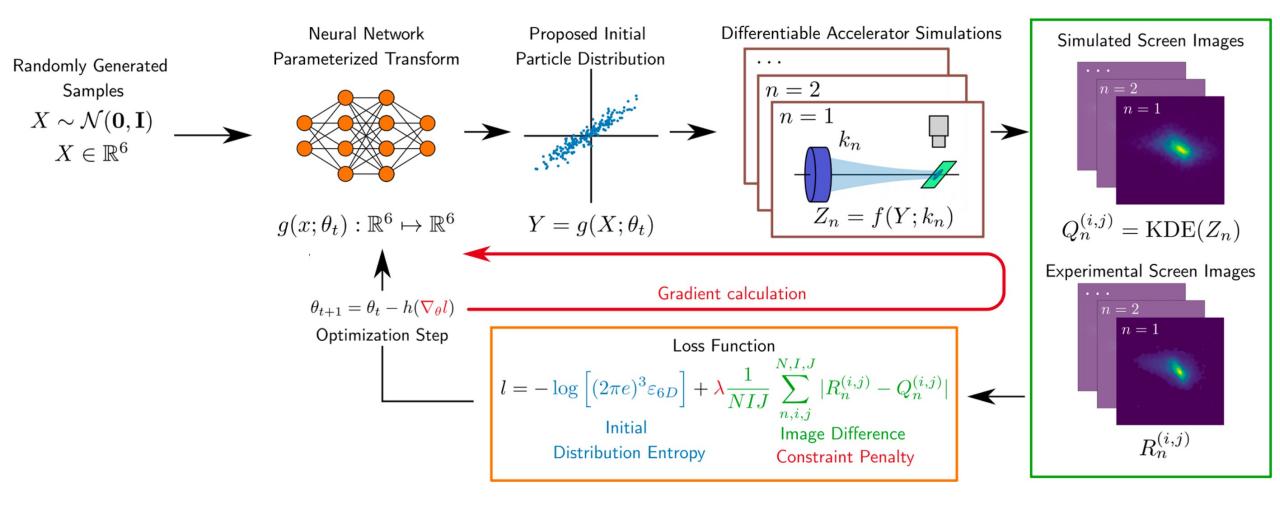
$$\frac{\partial Z}{\partial Y}, \frac{\partial Z}{\partial K}, \frac{\partial \sigma_Z}{\partial K}, \dots$$

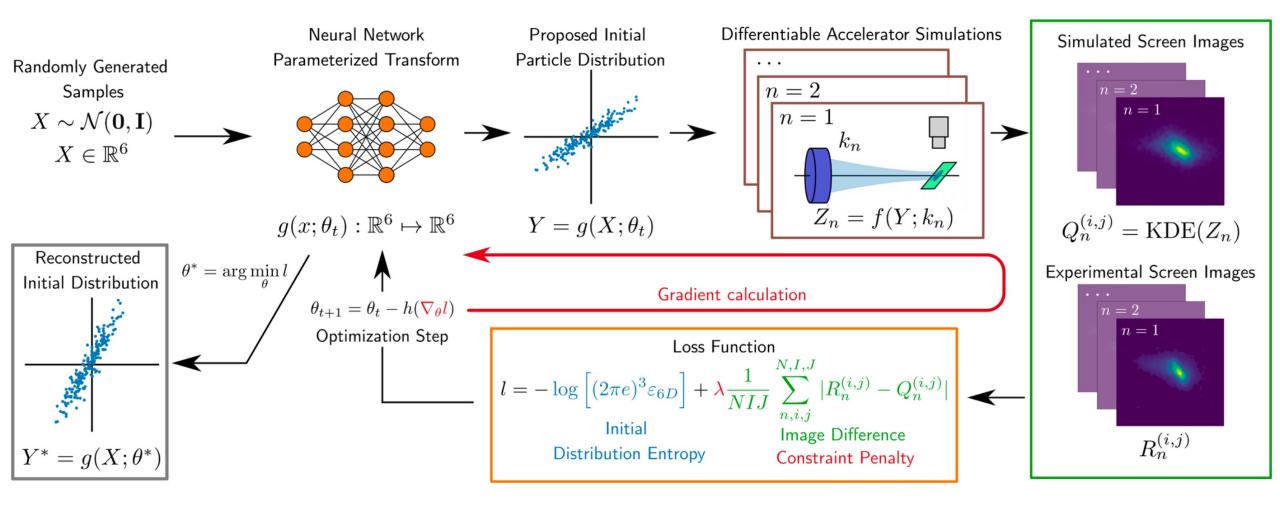
$$Q^{(i,j)} = \text{KDE}(Z)$$
$$\frac{\partial Q^{(i,j)}}{\partial Y}, \frac{\partial Q^{(i,j)}}{\partial K}$$





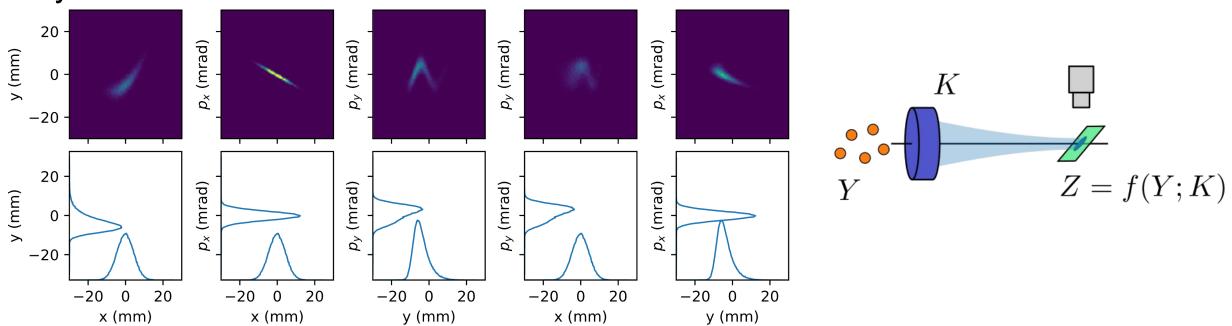




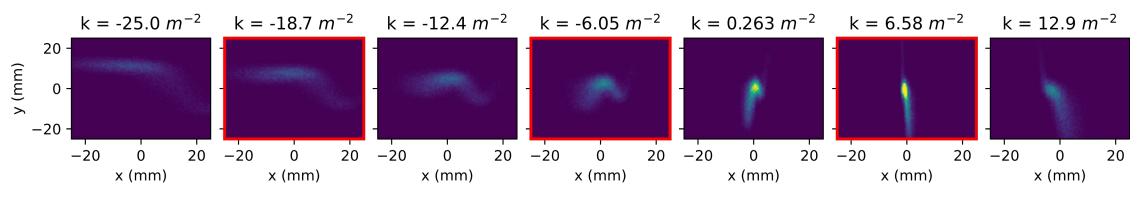


# **Synthetic Example**

Synthetic beam distribution in simulation

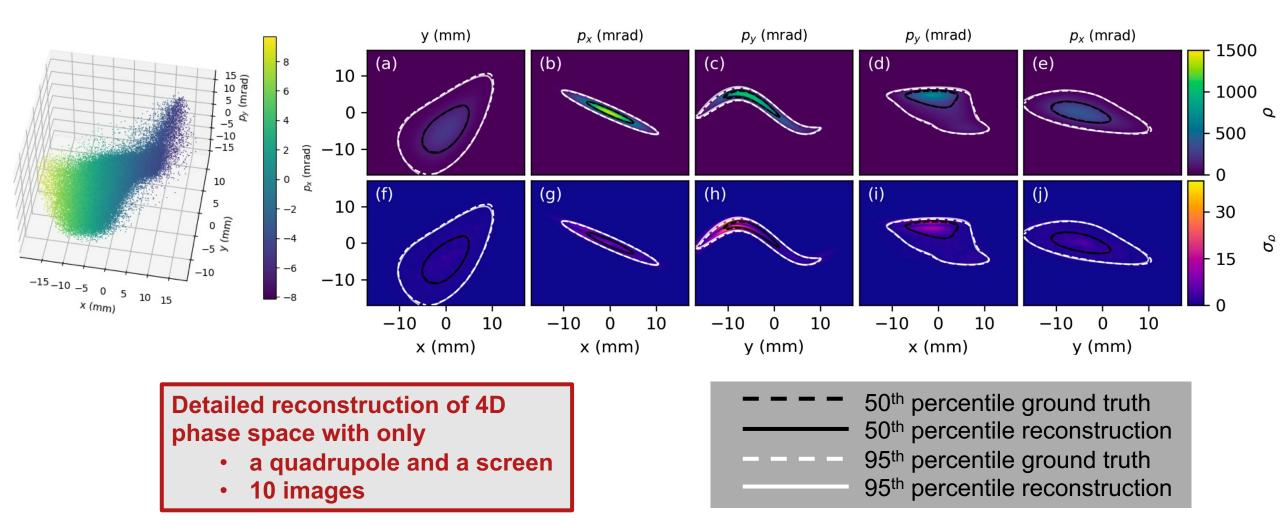


#### Screen images



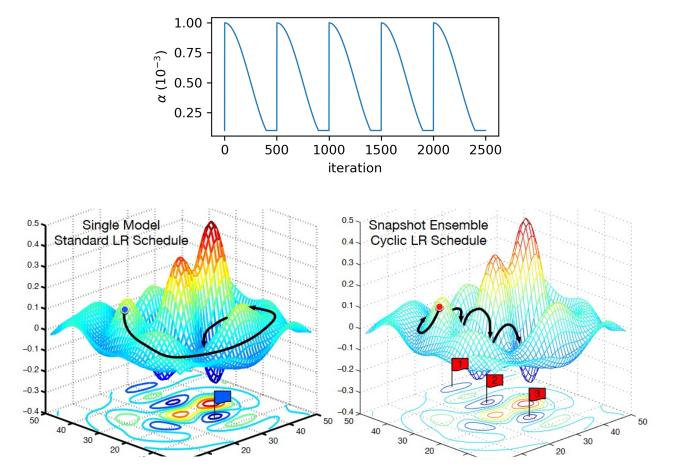
9/15

## **Synthetic Example Reconstruction**



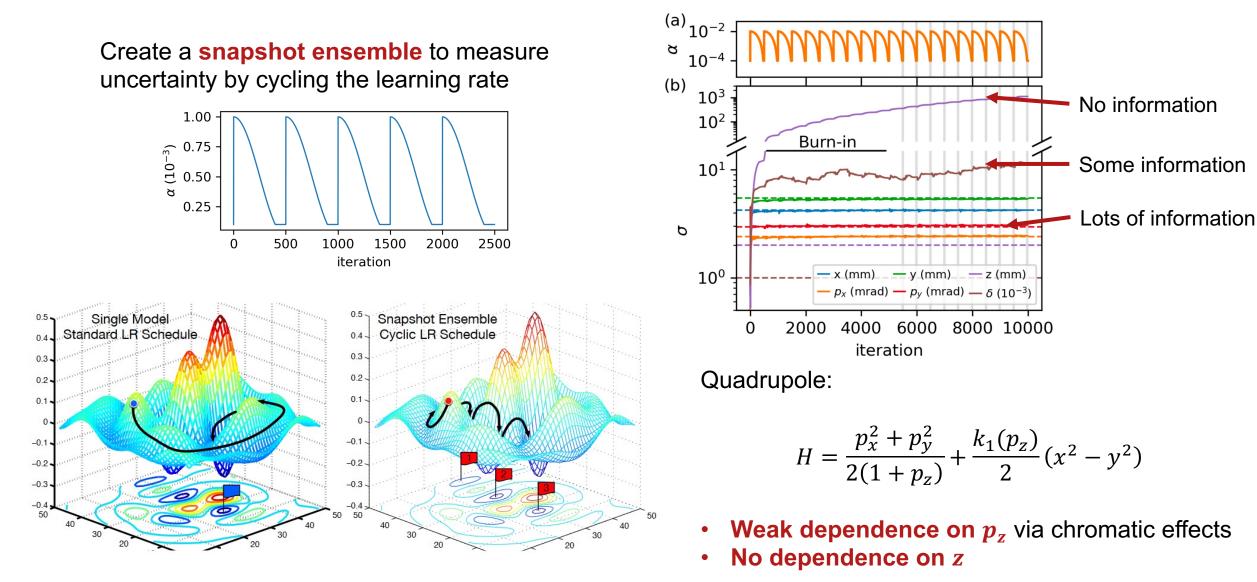
# **Measuring Model Uncertainty**

Create a **snapshot ensemble** to measure uncertainty by cycling the learning rate



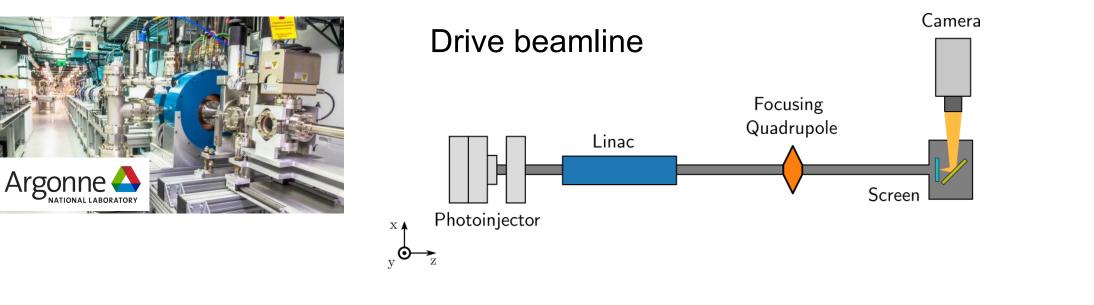
Huang G. et al., ICLR 2017

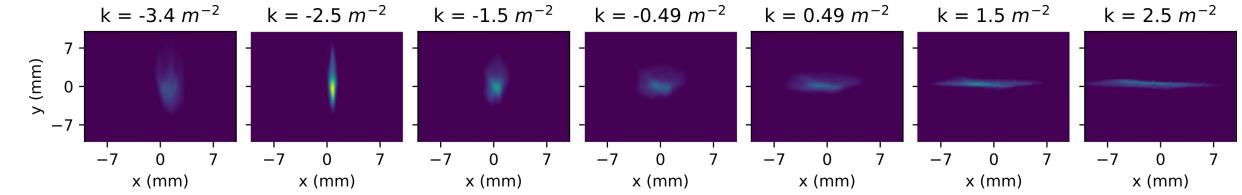
# **Measuring Model Uncertainty**



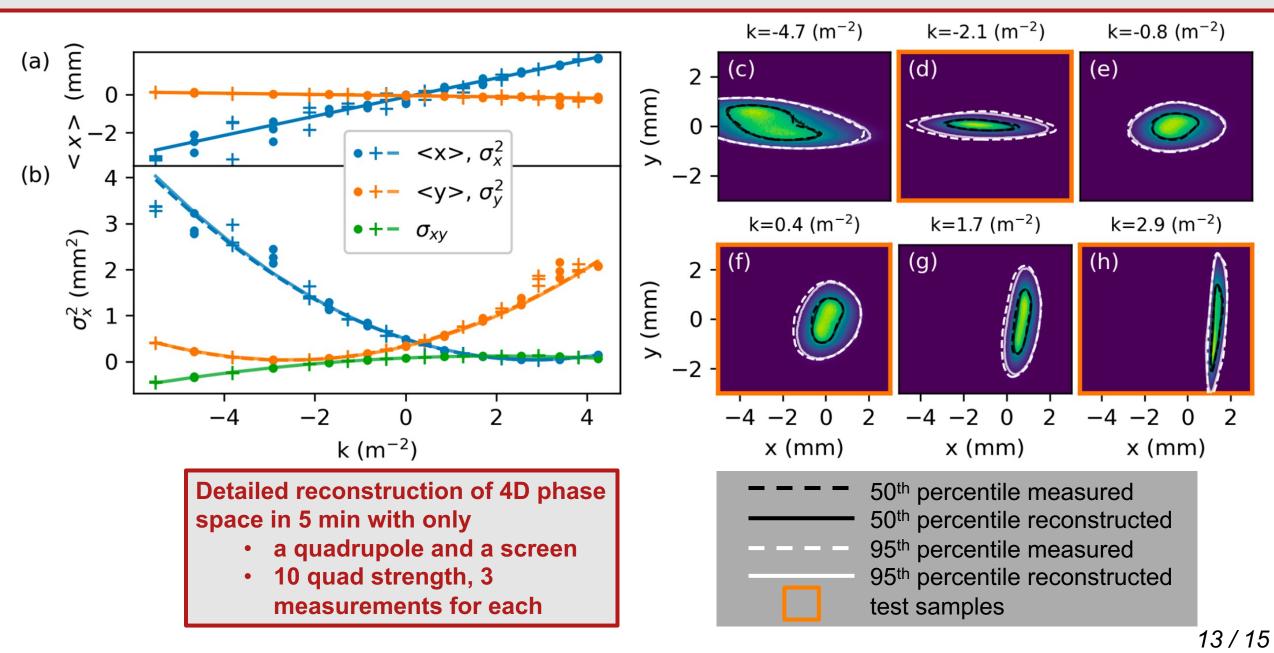
Huang G. et al., ICLR 2017

# **Tomography Example from AWA**



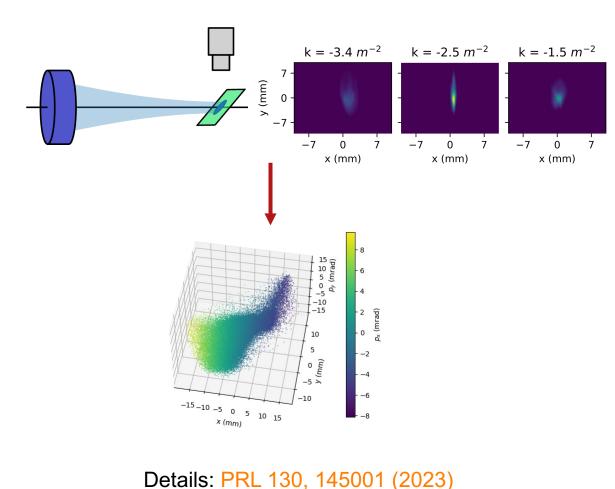


#### **AWA Reconstruction Results**



# Conclusions

- 4D detailed phase space reconstruction from few measurements and without special diagnostics
- Neural Network beam parametrization and differentiable simulations are not limited by dimensionality.
- Potentially extensible to 6D with the addition of longitudinal diagnostics.
- Can incorporate heterogeneous measurements:
  - More screens, BPMs, ...
  - Different types of data



# **Thanks! Questions?**

#### SLAC:

- Ryan Roussel
- Auralee Edelen
- Christopher Mayes
- Daniel Ratner

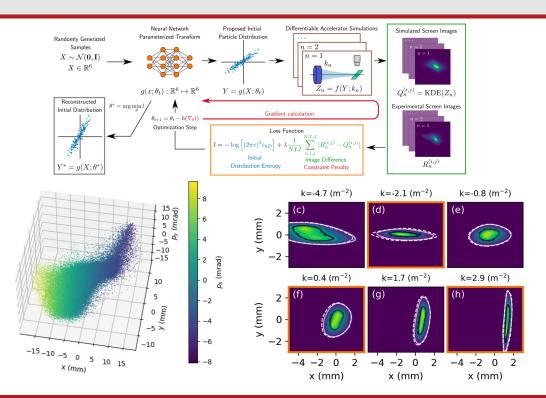
#### UChicago:

• Juan Pablo Gonzalez-Aguilera

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- Seongyeol Kim
- John Power
- Eric Wisniewski



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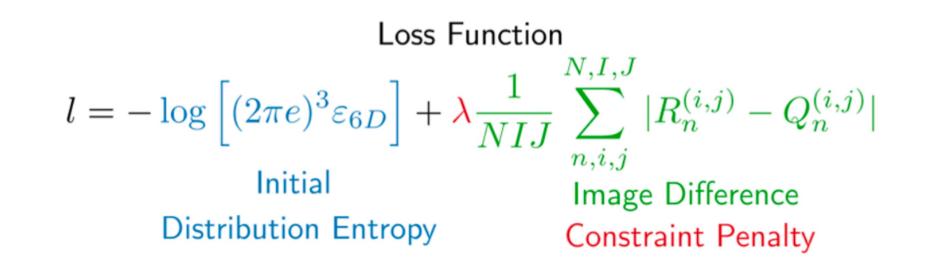


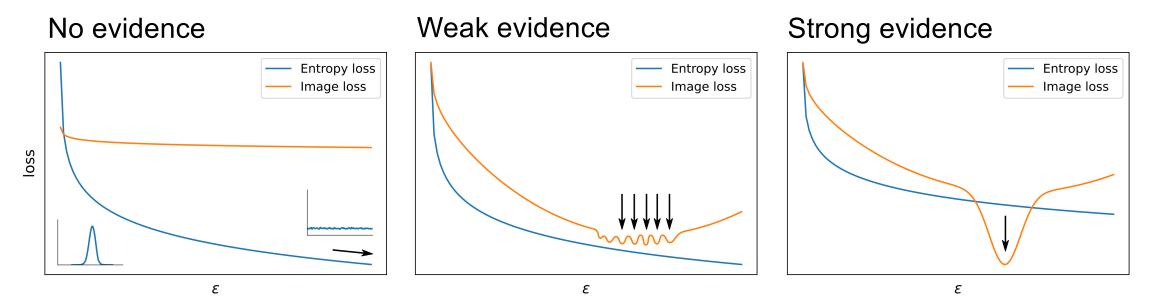






#### **Backup: Maximum Entropy Loss Function**





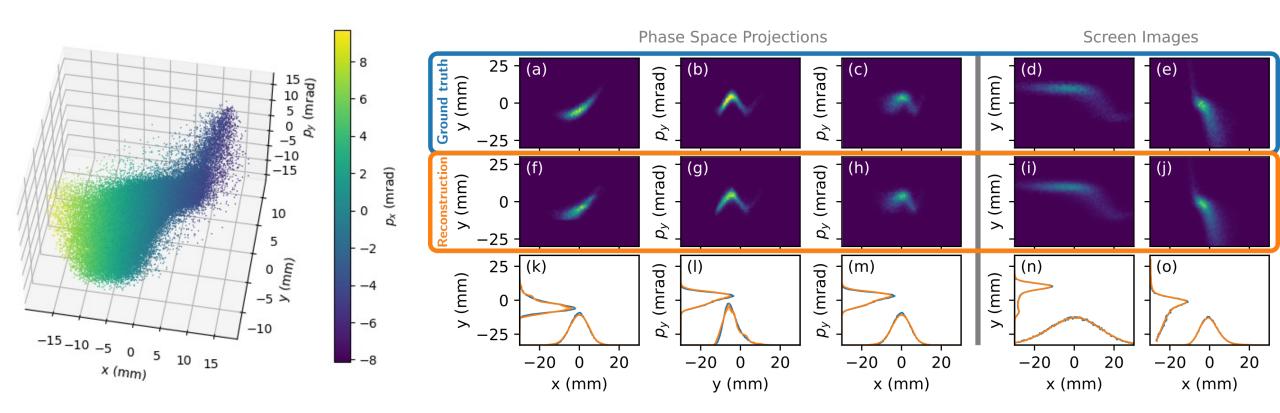
# **Backup: Maximum Entropy Tomography (MENT)**

Rotate phase space as before, but Note:  $H \propto \log(\varepsilon)$ reconstruct the distribution from 1D  $\rho(x, p_x)$ projections + maximize the beam distribution entropy Lagrange multiplier  $\rho^* = \arg\min\{-H(\rho) + \lambda f(\rho)\}$ Distribution entropy **Discrepancy with measurement** 0.8 0.8 0.5 0.5 0.6 0.6 > 0 0.4 0.4 -0.5-0.5 -0.5 0.2 0.2 -1 -0.5 0.5 0.5 0.5 -1 -0.5 -1 -0.5 -1

Hock K. and Ibison M., JINST, 2013

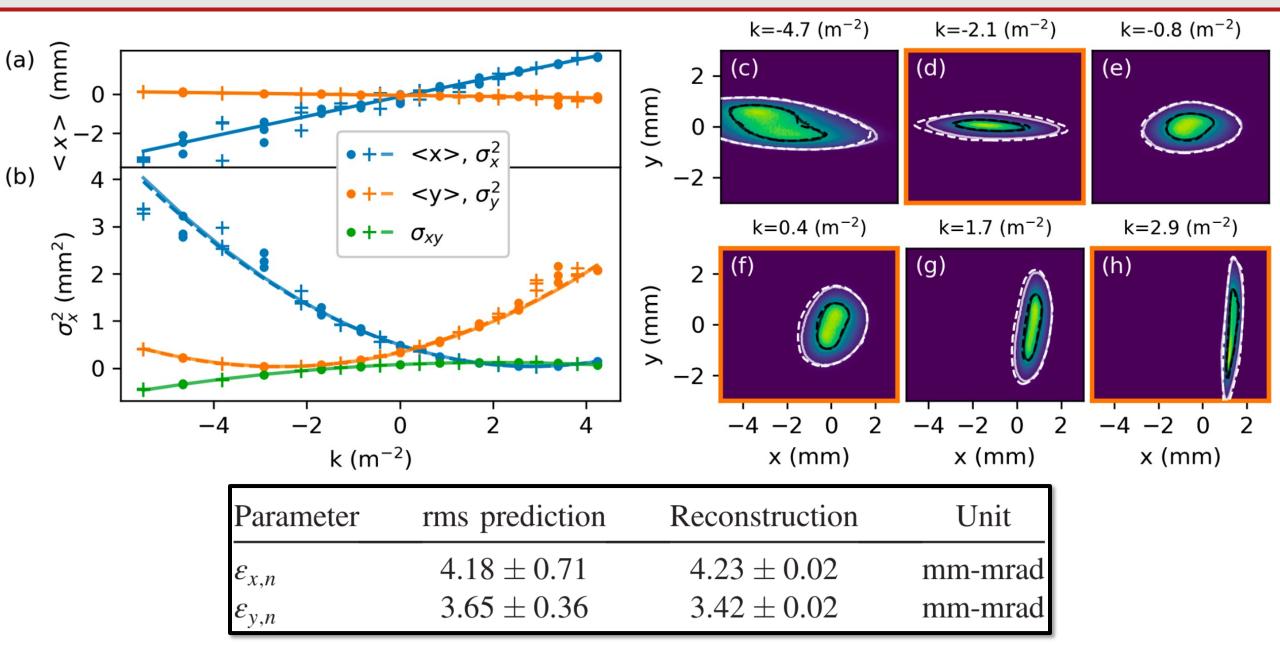
 $\lambda_{\phi}^{\dagger}(\xi)$ 

# **Backup: Synthetic Example Reconstruction**

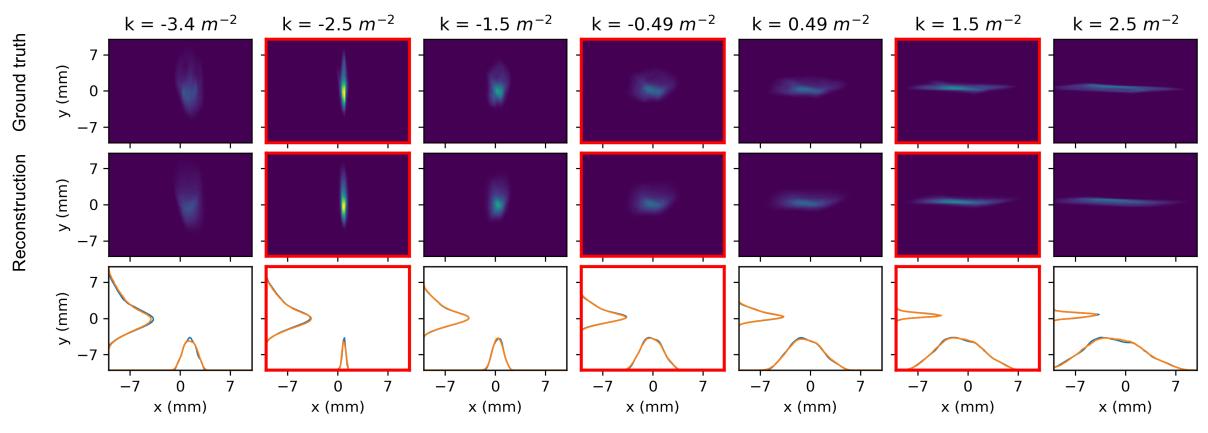


Parameter	Ground truth	rms prediction	Reconstruction	Unit
$\overline{\varepsilon}_{x}$	2.00	2.47	$2.00\pm0.01$	mm-mrad
$arepsilon_x \ arepsilon_y$	11.45	14.10	$10.84\pm0.04$	mm-mrad
$\varepsilon_{ m 4D}$	18.51	34.83 <sup>a</sup>	$17.34\pm0.08$	mm <sup>2</sup> -mrad <sup>2</sup>

#### **Backup: AWA Reconstruction Results**

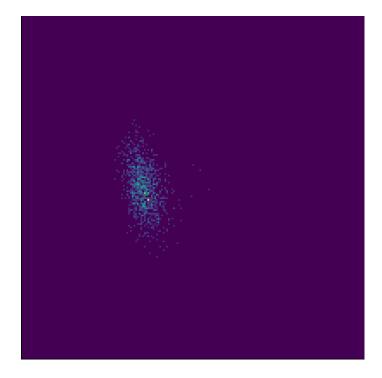


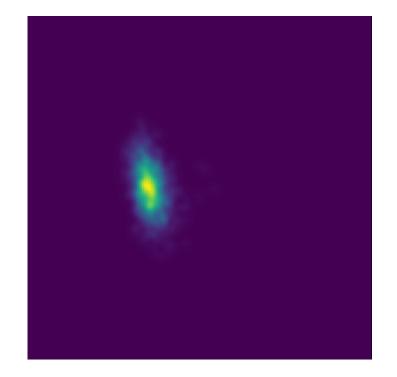
#### **Backup: AWA Reconstruction**



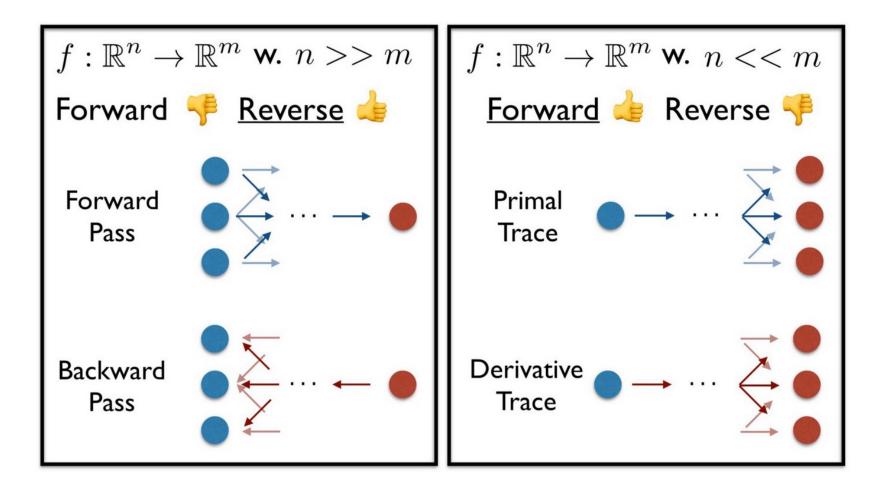
Red border denotes test samples

#### **Backup: Kernel Density Estimation (KDE)**



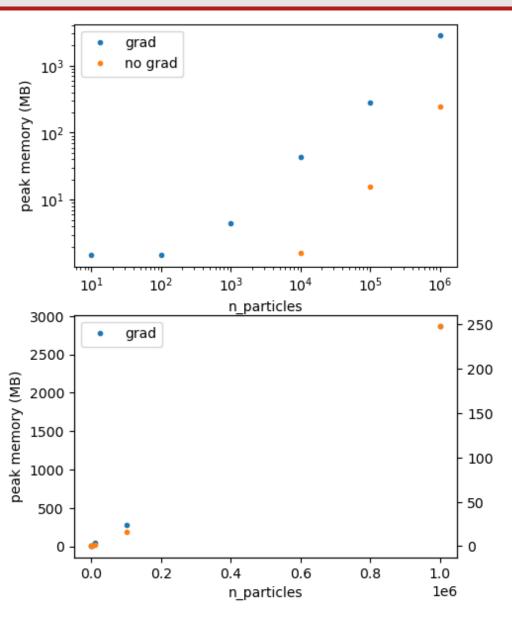


#### **Backup: Reverse vs Forward Autodiff**



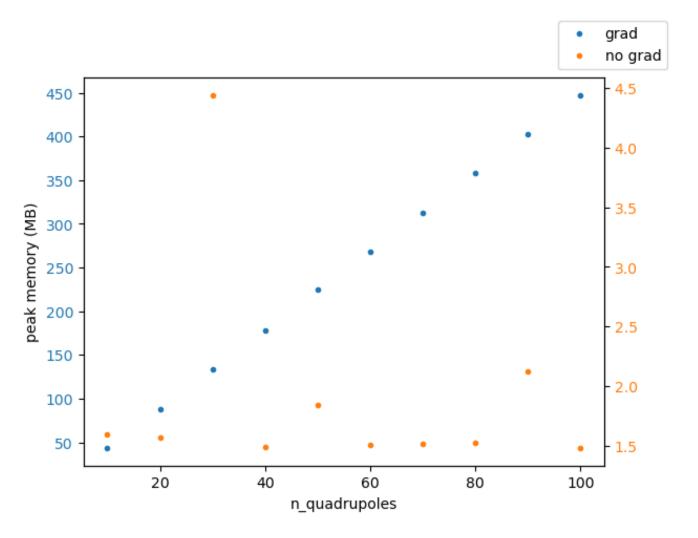
https://towardsdatascience.com/forward-mode-automaticdifferentiation-dual-numbers-8f47351064bf

# **Backup: Memory profiling**



Test 1: 10 quads separated by drifts. Peak memory vs number of particles

### **Backup: Memory profiling**



Test 2: 10<sup>4</sup> particles Peak memory vs n quads

#### **Backup: Memory profiling**

