

Status report of nonlinear Inverse Compton Scattering study



Nonlinear ICS by $a_0 \sim 1$, CO_2 laser @ $h\nu \sim 10 \text{ keV}$: ATF-AE70 & Before

\leftrightarrow Linear ICS by YAG laser @ $h\nu \sim 100 \text{ keV}$: ATF-AE87

AAC2022yr, WG7, November 7

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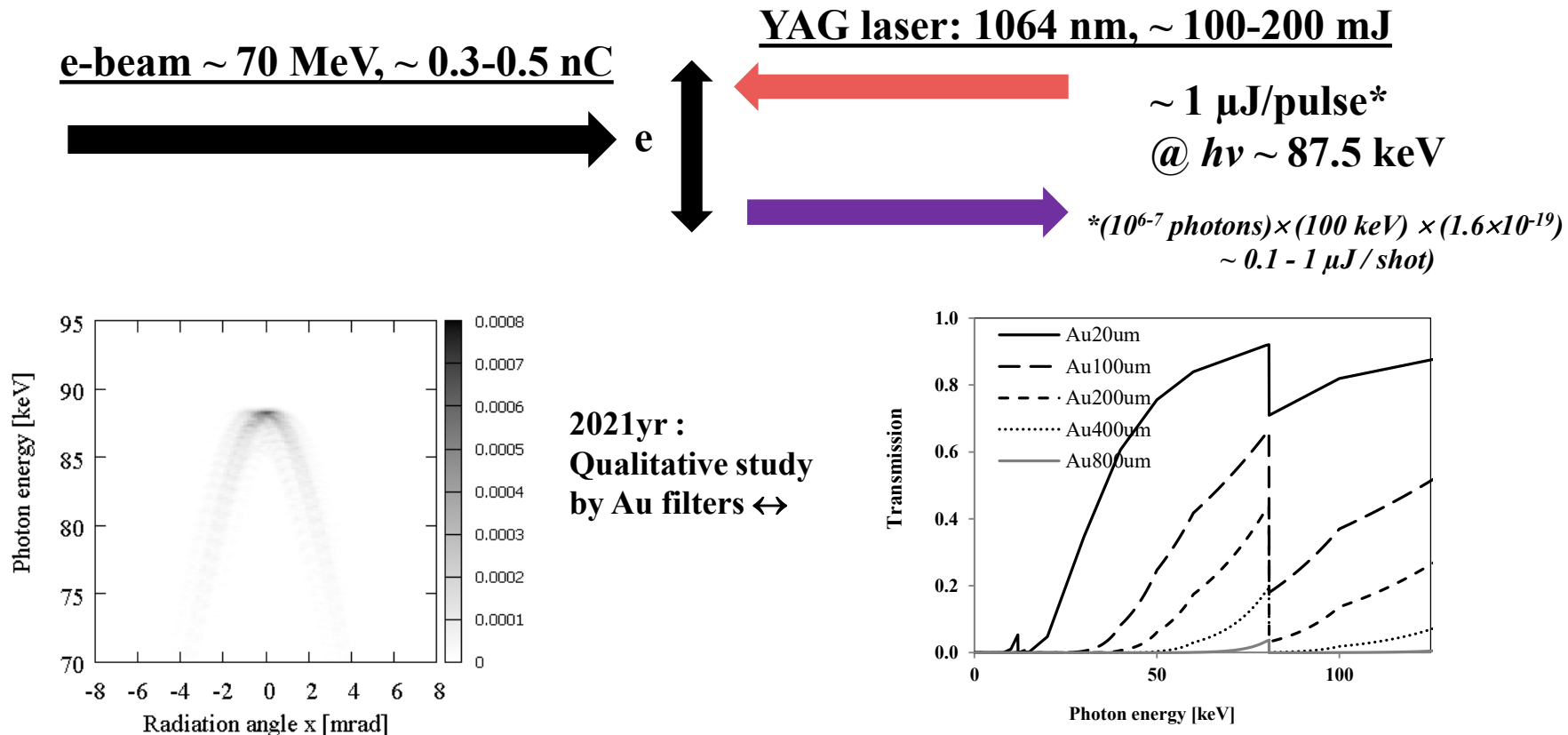
I. Pogorelsky, K. Kutsche, M. Babzien, M. Fedurin, M. Polyanskiy, M. Palmer



BNL ATF Experiment AE87: Experiment Goals

HARD X-ray ICS at $h\nu \sim 100$ keV range

- ★ Applications: Photon activation as Medicine & Radiography of high Z materials
- ★ Strong field physics: Bi-harmonic Compton interaction with ATF's CO₂ laser
- ★ Hard X-ray optics developments: DDS measurement & Focusing or Collimation
- ★ X-ray OAM investigation: Higher order harmonics by circular polarized CO₂ laser

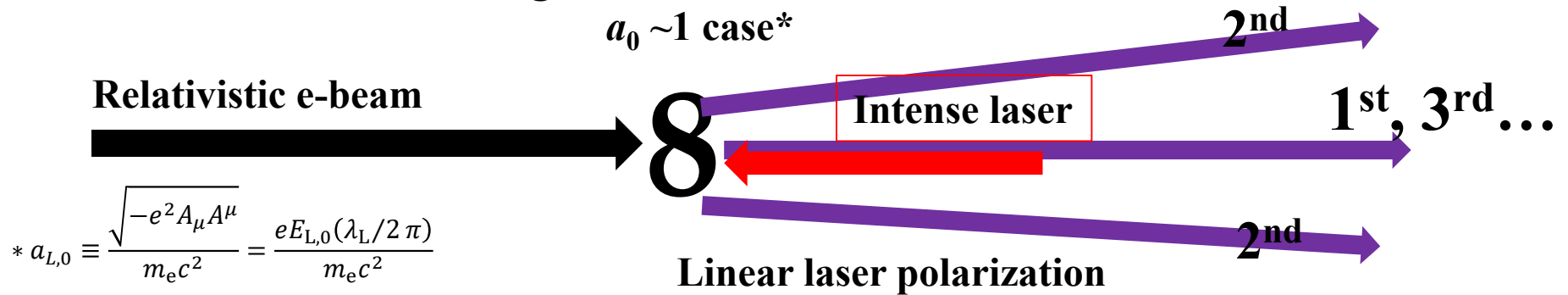


{Goals of AE87 as of now: Establish basic set up of ICS by YAG & upgraded $a_0 > 1$ CO₂ lasers}

TODAY: Overview of nonlinear Compton study by CO₂ laser in BNL ATF

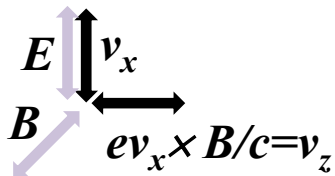
Figure-8 electron motion

$a_0 \sim 1$ case*



Nonlinear ICS: $a_L \sim 1$, Transverse motion \rightarrow Relativistic, nontrivial longitudinal oscillation**
Slow down electron's velocity, or Effective mass increase

**



★ Red-shifting and BW increase:

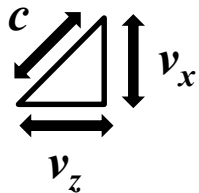
Photon absorption by electron = Mass shift

$$h\nu_{\text{X-ray}} \Rightarrow h\nu_{\text{X-ray}} / (1 + a_L^2/2 + \gamma_0^2 \Theta^2)$$

★ Harmonic generation/angular dependence:

Multi-photon process in dense photon field

$$h\nu_{\text{X-ray}} = 4\gamma^2 h\nu_L n$$



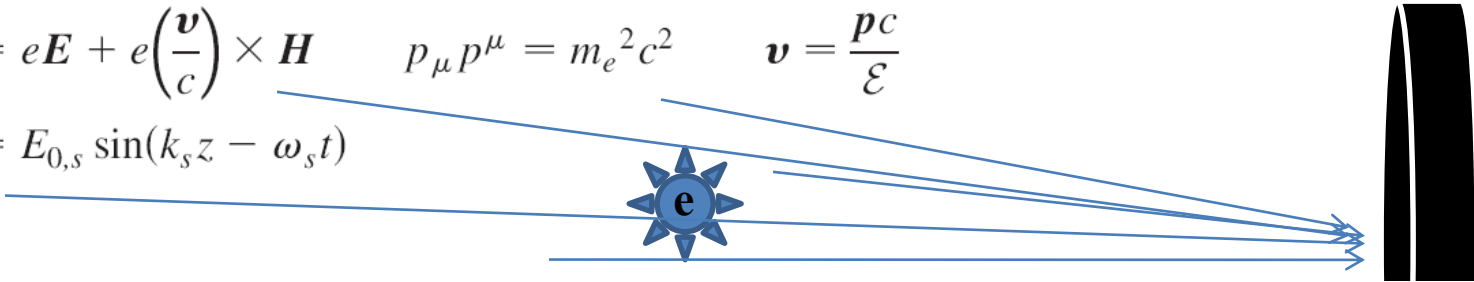
Advantage of CO₂ laser: ♦ Longer wavelength

♦ Higher photon number per intensity

♦ Narrow bandwidth emission

Numerical spectrum estimate by Lenard-Wiechert calculation approach (Using extra RAM)

$$\frac{d\mathbf{p}}{dt} = e\mathbf{E} + e\left(\frac{\mathbf{v}}{c}\right) \times \mathbf{H} \quad p_\mu p^\mu = m_e^2 c^2 \quad \mathbf{v} = \frac{p\mathbf{c}}{\mathcal{E}}$$

$$E_x = E_{0,s} \sin(k_s z - \omega_s t)$$


The diagram shows a blue star-like particle labeled 'e' moving from left to right. Several blue lines representing radiation rays originate from the particle and converge towards a vertical black rectangle on the right labeled 'screen'. The particle is positioned between two horizontal blue lines representing the laser field.

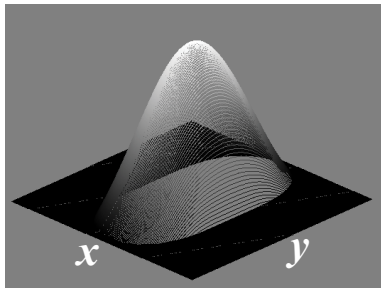
$$E_{\text{LW}} = \frac{m_e}{e} \frac{r_e}{R} \frac{\mathbf{n} \times \{(\mathbf{n} - \mathbf{v}/c) \times \mathbf{w}\}}{(1 - \mathbf{n} \cdot \mathbf{v}/c)^3}$$

$$E_{\text{LW},x}(\omega) = \left| \int_{-\infty}^{\infty} E_{\text{LW},x}(t) e^{i\omega t} dt \right|$$

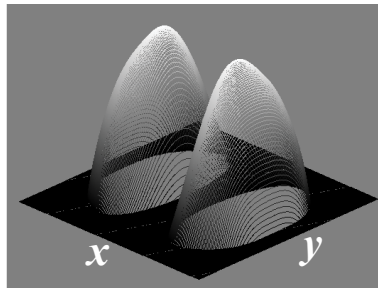
A thick black curved arrow points from the frequency-domain equation to the time-domain equation.

screen

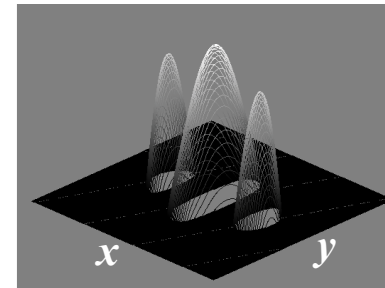
Example: Radiation distribution of single particle scattering, $a_0 \sim 0.6$, Linear polarization, ATF-AE70



1st ($h\nu < 7.6 \text{ keV}$)
Cone angle $\Theta \sim 1/\gamma$

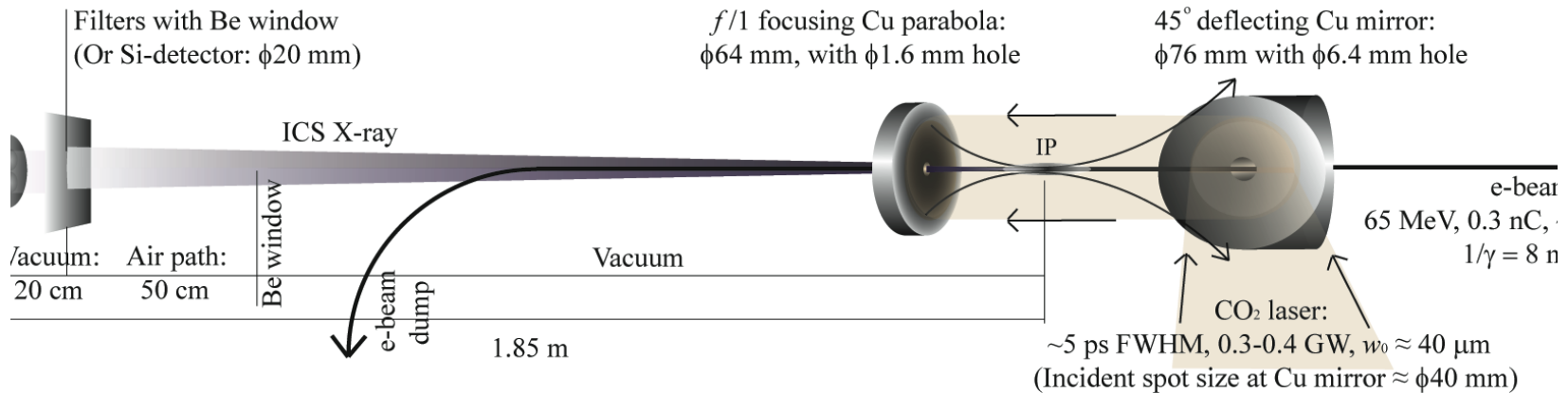


2nd ($7.6 < h\nu < 15.2 \text{ keV}$)
 $\Theta \sim 1/2\gamma$
 $I_{\text{peak},2\text{nd}} / I_{\text{peak},1\text{st}} \sim a_L^2/4$



3rd ($15.2 < h\nu < 22.8 \text{ keV}$)
 $\Theta \sim 1/3\gamma$
 $I_{\text{peak},3\text{rd}} / I_{\text{peak},2\text{nd}} \sim 3a_L^2/4$

AE70 experiment in BNL-ATF, 2014yr



BNL-ATF Beam parameters (as of 2014yr):

✦ CO₂ laser: $a_L \approx 0.6$ to 1.0

(~0.4-0.8 TW, > 3 J), FWHM $\approx 3.5 - 5.0$ ps,
10.6 μm , $w_0 \approx 40 \mu\text{m}$, $Z_R \approx 500 \mu\text{m}$

✦ Electron beam: $E = 65 - 70$ MeV

$Q \approx 0.3$ nC, $\sigma_z \approx 300 \mu\text{m}$, $\sigma_x \approx 30 \mu\text{m}$, $\varepsilon_N \approx 1$ mm mrad, $\beta \approx$ a few cm

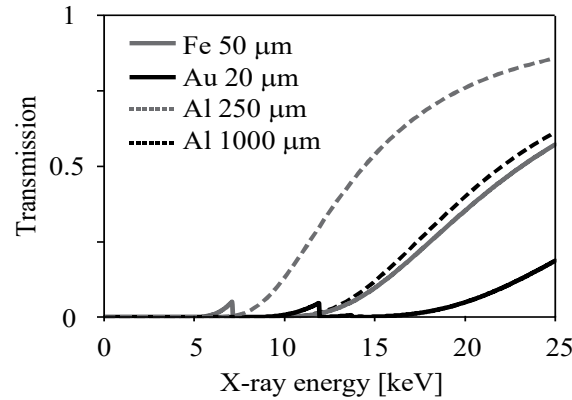
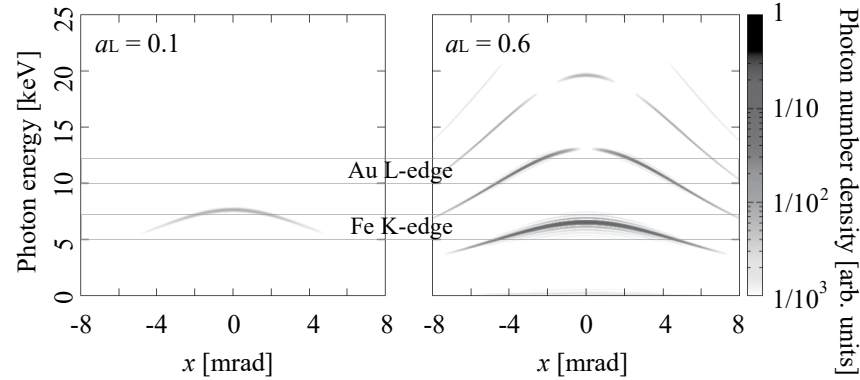
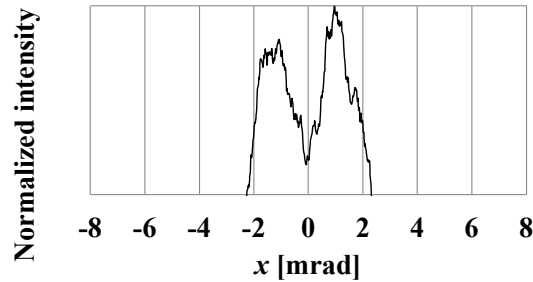
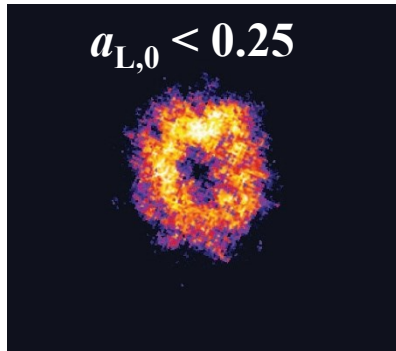
★ Compton edge: $h\nu = 4\gamma^2 E_L \approx 7 - 10$ keV

★ Photons / pulse: $N_\gamma \approx 10^9$ (★ World record ★)

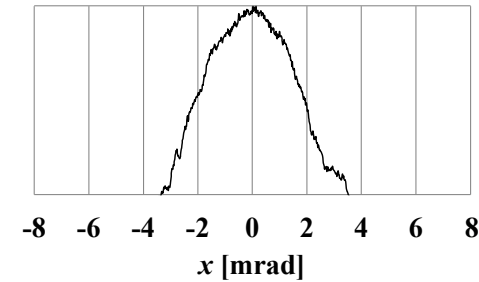
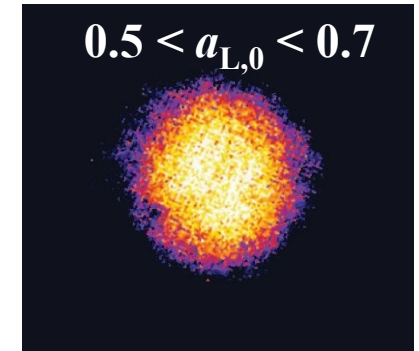


Observed red-shift (*Direct evidence of the figure-8 motion*)

7.6 keV < Fe k-edge
Off-axis component



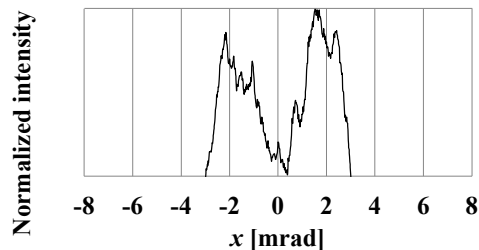
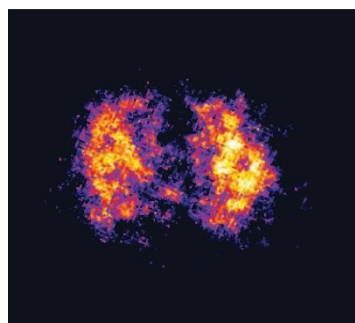
Red-shifting
to 5-6 keV



$$h\nu_{\text{ICS}, 1}^{\text{st}} = 4\gamma^2\nu_L/(1+a_{L,0}^2/2) \rightarrow \therefore 0.5 < a_{L,0} < 0.7$$

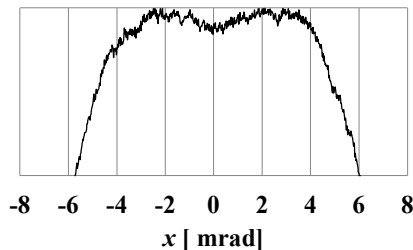
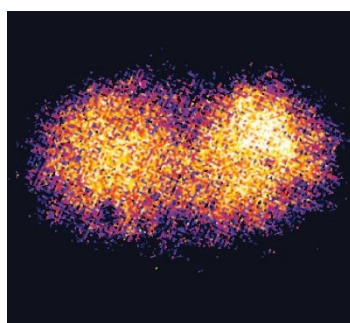
Angular distribution of harmonic radiation (*Linear polarization case*)

Au L-edge (12 keV)



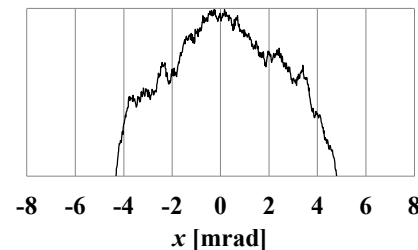
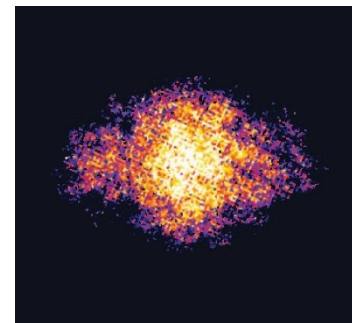
Narrow band 2nd

Al 250 μm > 10 keV



2nd + 3rd

Al 1000 μm > 15 keV

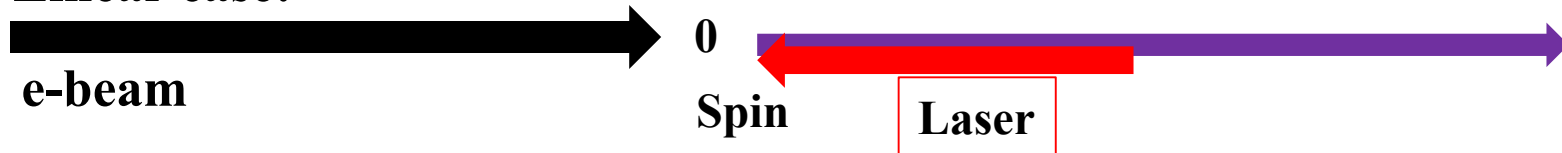


3rd (On-axis & lobes)

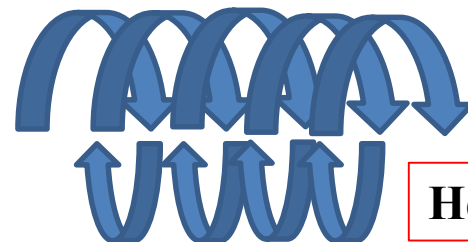
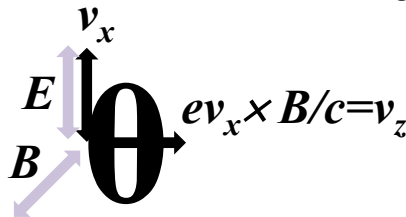
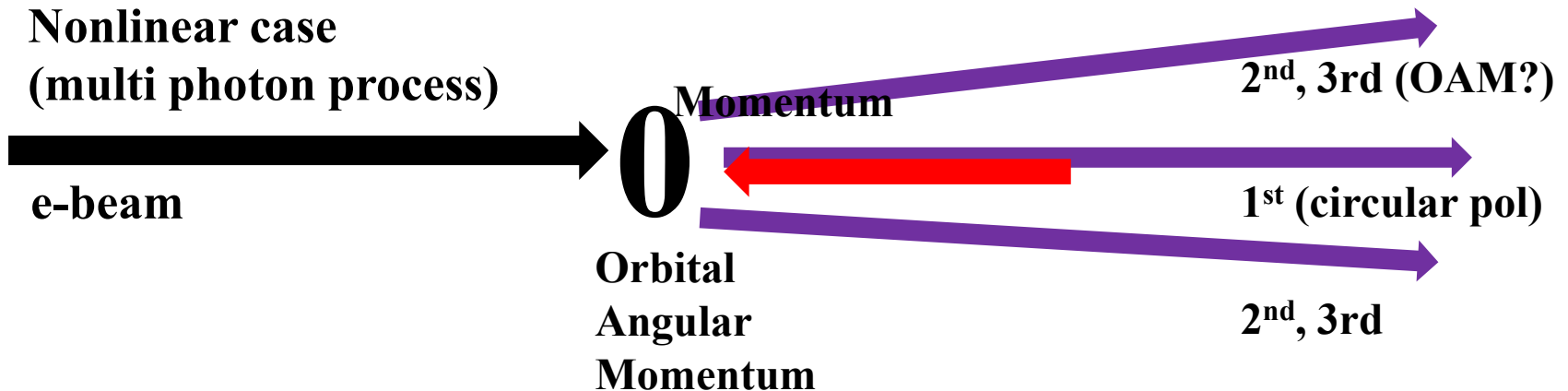
★ On axis components of 3rd harmonics \leftrightarrow Direct evidence of the longitudinal motion

ICS of circular polarized laser – OAM X-Gamma ray ?

Linear case:



Nonlinear case
(multi photon process)



Helical motion

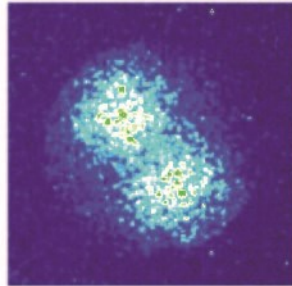
NOTE: OAM X-ray can be also generate by FEL & Linear ICS by OAM laser

OAM X-ray generation by non linear ICS

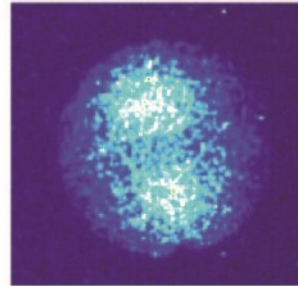
1/4 wave plate between regenerative and TW amplifier

Al 250 μm :

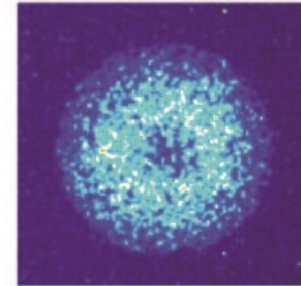
Linear, 2nd



Elliptical, 2nd

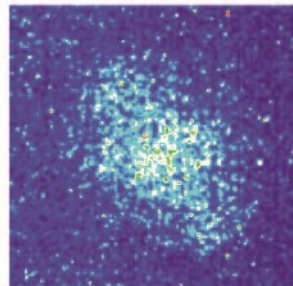


Circular, 2nd

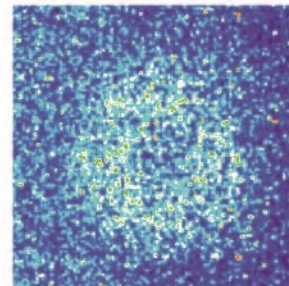


Al 1000 μm :

Linear, 3rd



Circularlar, 3rd



Gamma-ray vortices can be generated by only ICS

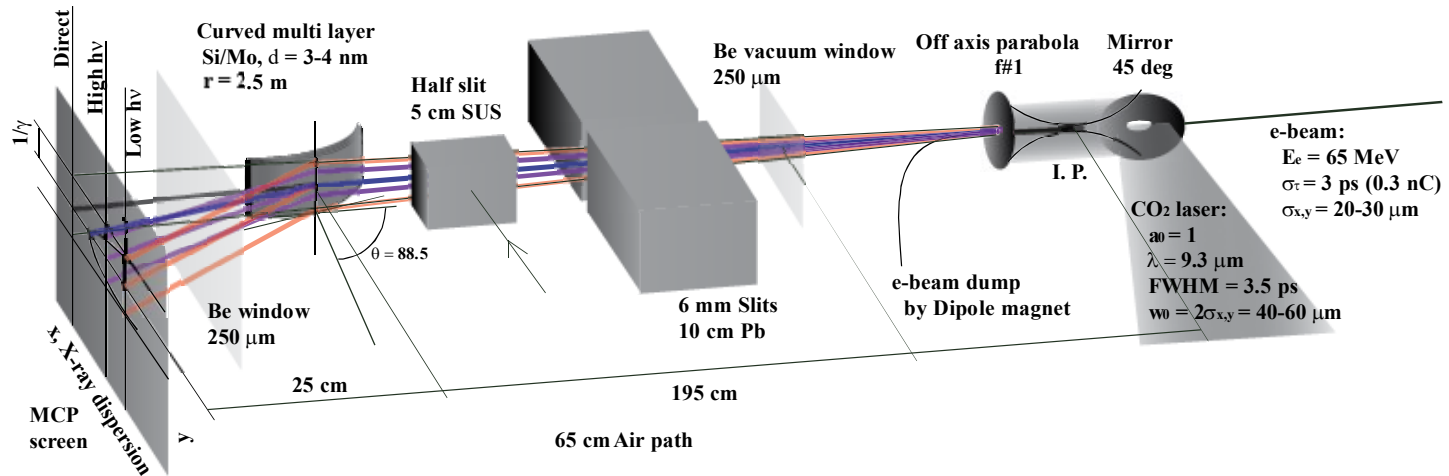
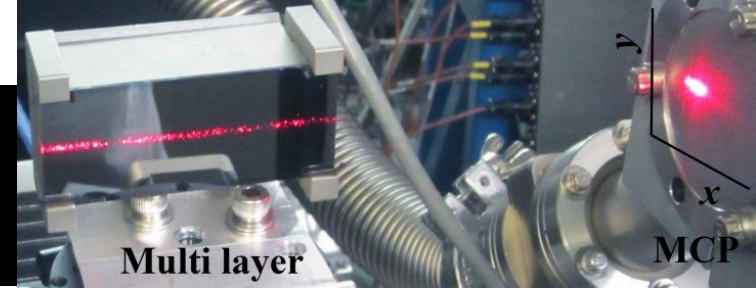
{Strong demands in Nuclear Photonics community:

REF Y. Taira, T. Hayakawa, M. Katoh, Scientific Reports volume 7, 5018 (2017)}

→ Detailed spectrum distribution needs to be measured at 30 keV range.

Details of the ICS X-ray spectrum:

Mo/Si curved Multi-layer spectrometer



MCP image

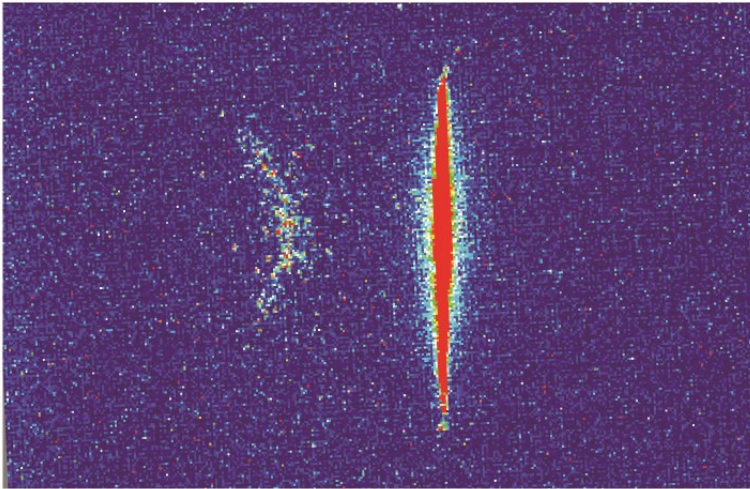
☆ Mo-Si Multi (45) layer thickness: $d \approx 3.3 \text{ nm}$

☆ Bragg angle:
 $\sim 25 \text{ mrad}$

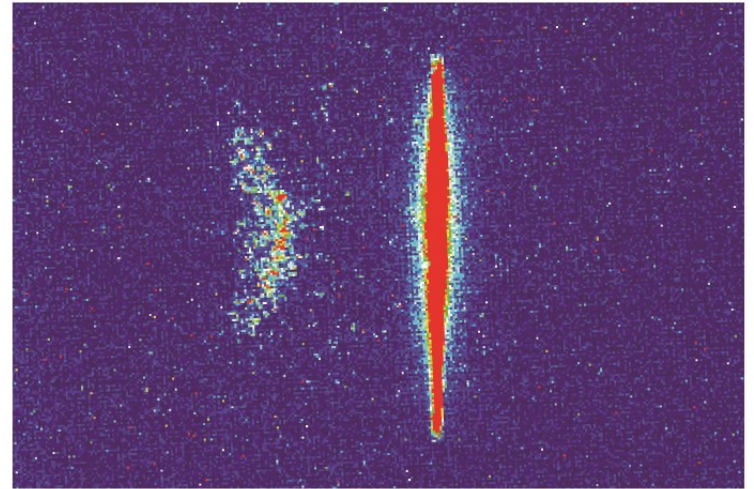
☆ Angle acceptance :
 $\sim 50 \text{ mrad}$

☆ Reflectivity $\sim 15\%$ @ NSLS X15A (Z. Zhong)

Projection of deflected ICS X-ray in a single shot

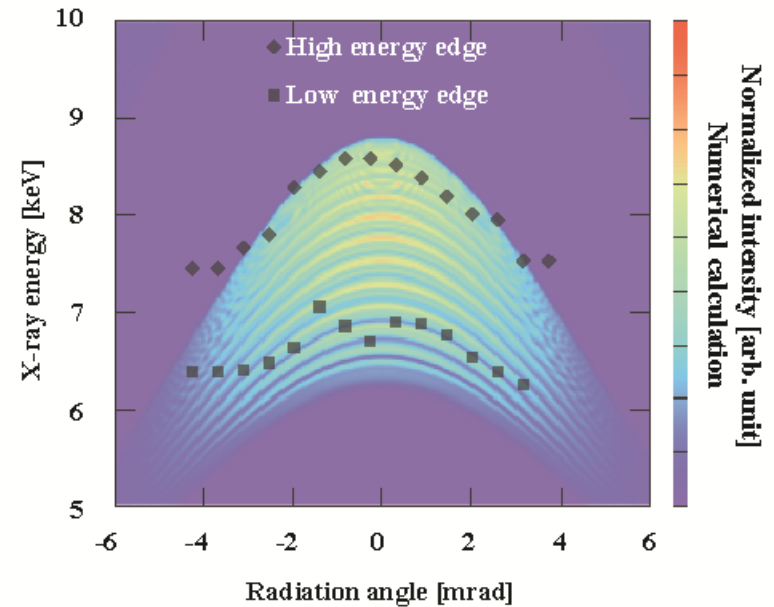
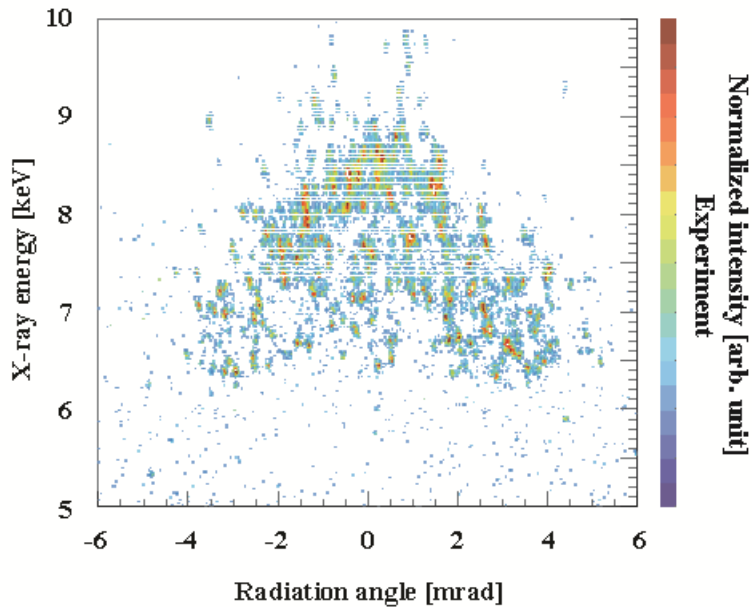


Laser energy 1.5 J,
 $a_L = 0.7$



Laser energy 3.0 J
 $a_L = 1$

Double Differential Spectrum at $a_0 = 1$



*It figured out that Spectrum shape changes
by e-beam & laser spot size:*

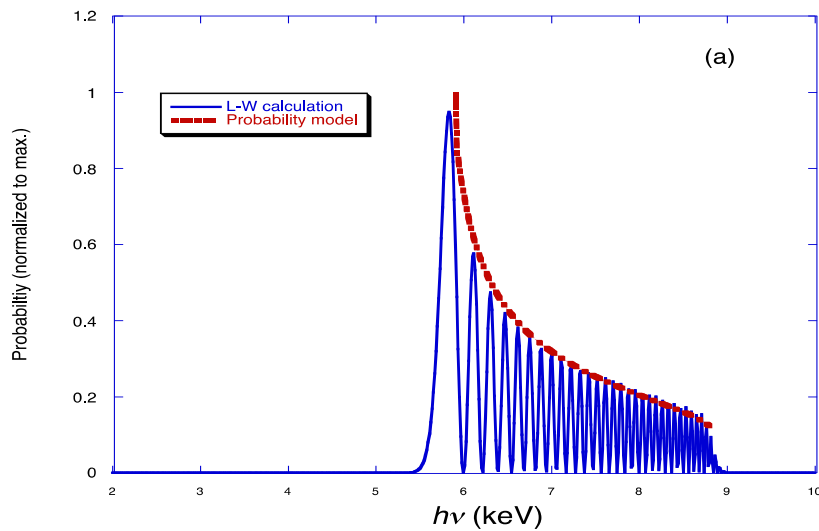


Analysis: on-axis spectral structure

Temporal effect alone

$$(\sigma_{\text{Laser}} > \sigma_{\text{electron}})$$

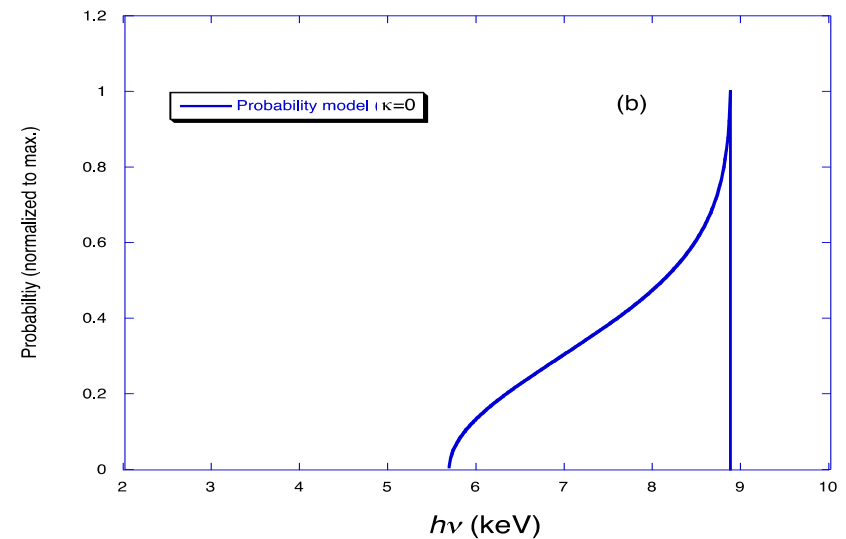
Electron see only on-axis high intense laser field



Radial effect

$$(\sigma_{\text{electron}} > \sigma_{\text{Laser}})$$

Electron see radial variation



**Scattering
Probability
Factor:**

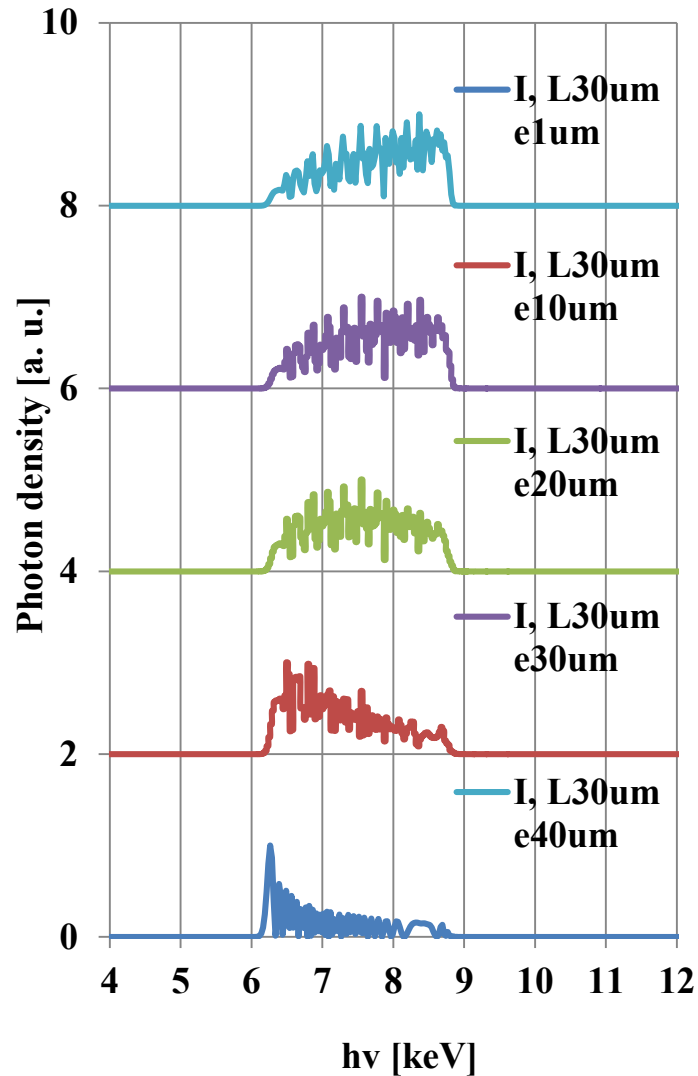
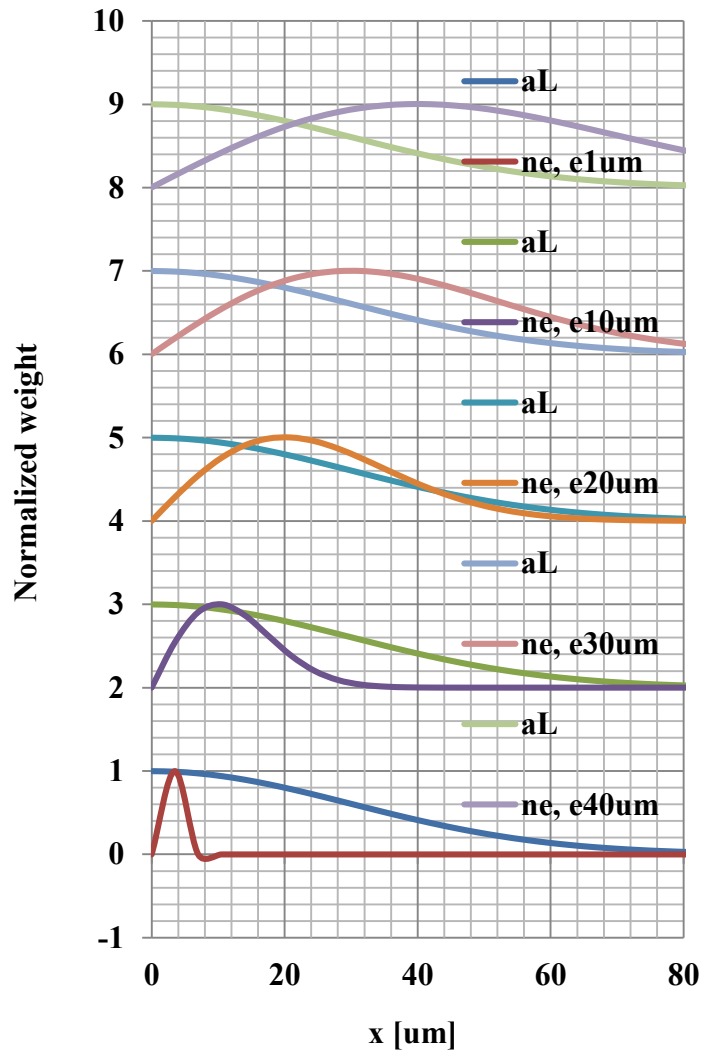
$$P_t(\Delta\lambda) \propto \frac{1}{\sqrt{\frac{\Delta\lambda_{\text{max}}}{\Delta\lambda}}}$$

$$P_r(\Delta\lambda) \propto \left(\frac{\Delta\lambda_{\text{max}}}{\Delta\lambda} \right)^{\kappa-1}$$

$$\kappa = \left(\frac{\sigma_L}{\sigma_e} \right)^2$$

Numerical example

Beam size effect:



Approximation:

Radial weight

$$I_{x\text{-ray}}(r) \propto a_L^2(r) N_e$$

$$N_e \propto n_e r dr$$

Longitudinal effect neglected

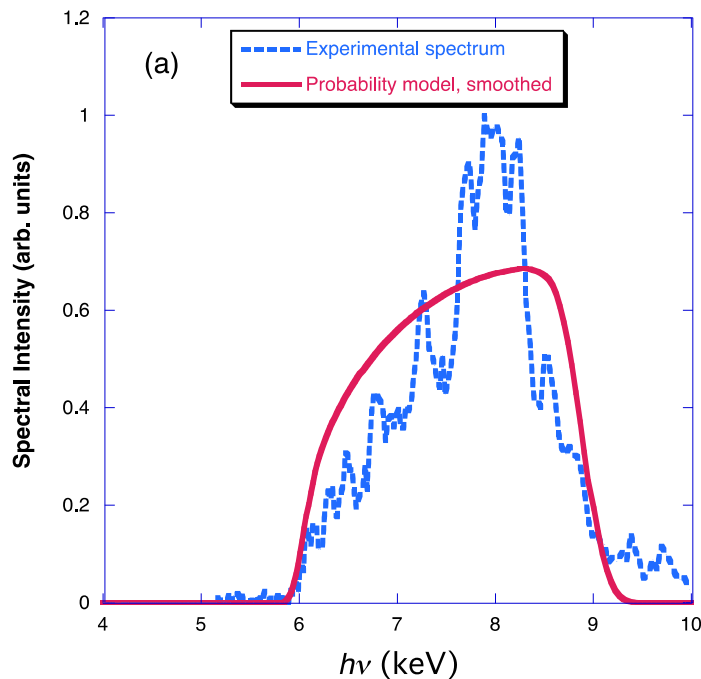
$$\beta_e = 3 \text{ cm} \gg$$

$$Z_R = 0.5 \text{ mm}$$

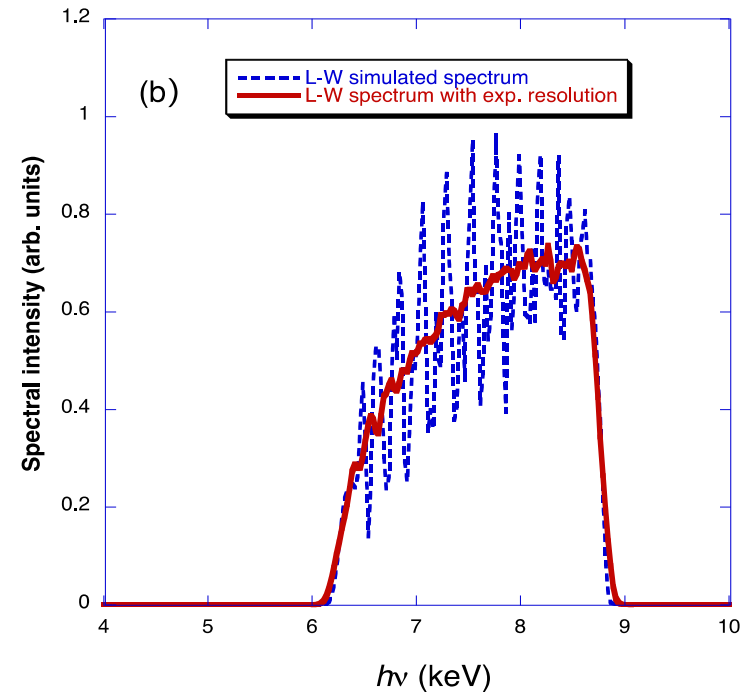
Conclusion of on-axis spectrum analysis, BNL-AE70 experiment :

★ Spectral shape agrees with model, deduce $\sigma_e \approx \sigma_L \approx 20\text{-}30\mu\text{m}$

★ On-axis emission; Total BW=33% with $a_0 = 1$.

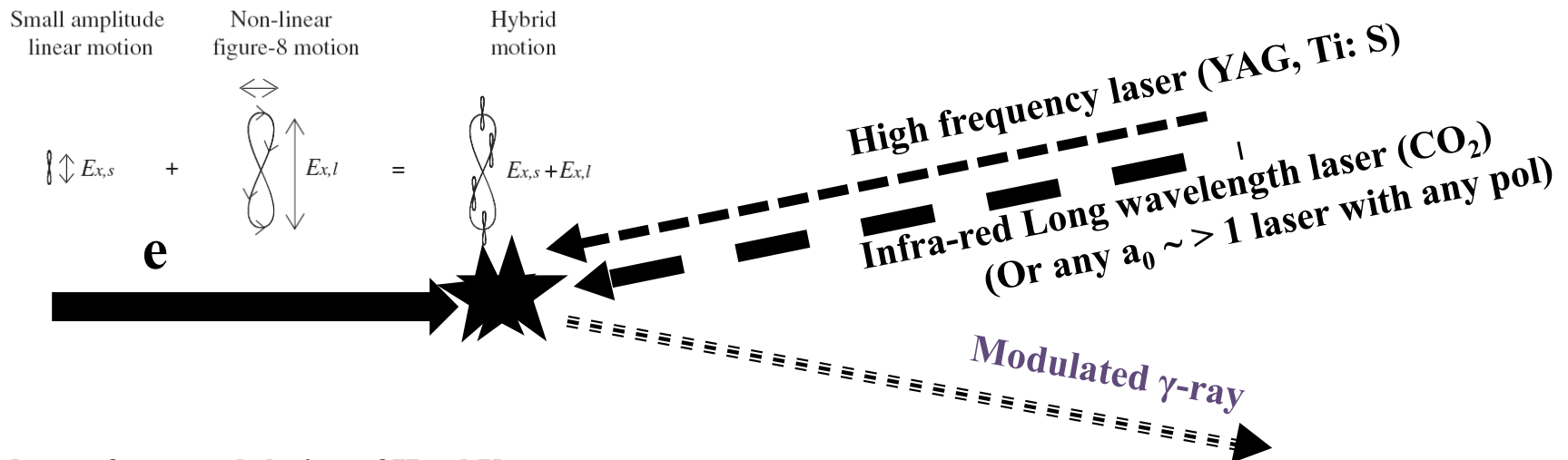


Data and analytical probability model



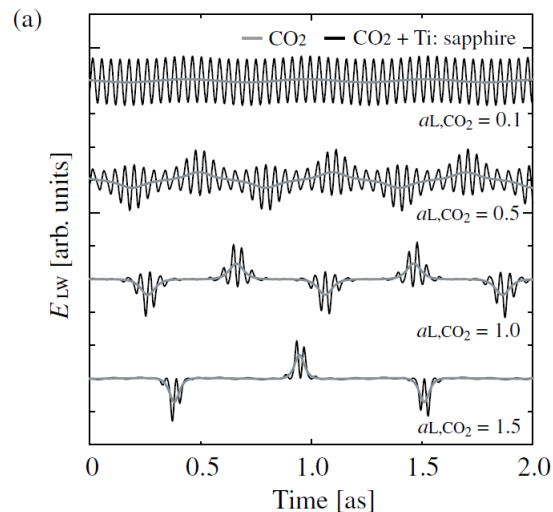
Lenard-Wiechert model
(showing interference)

NEXT → Bi-harmonic nonlinear Compton experiment



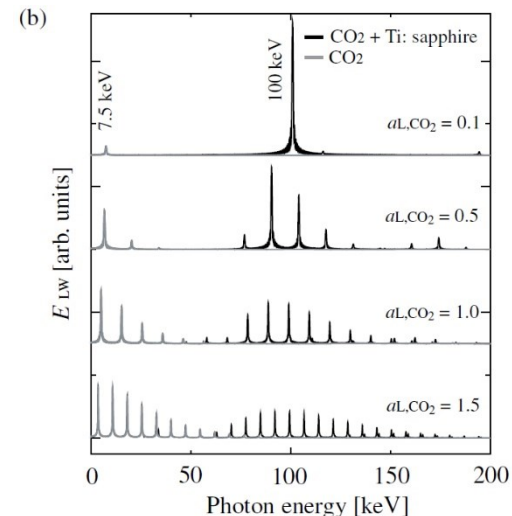
**Pulsed waveform modulation of Hard X-ray component
at less than $< 10^{-18}$ s time scale {A few cycle X-Gamma RAY}**

Observation of Red-Blue shifts & $h\nu_{L,YAG} \pm h\nu_{L,CO_2}$



Numerically calculated Lienard-Wiechert potential $E_{LW,x}(t_{screen})$ on $(x, y, z) = (0, 0, 0)$

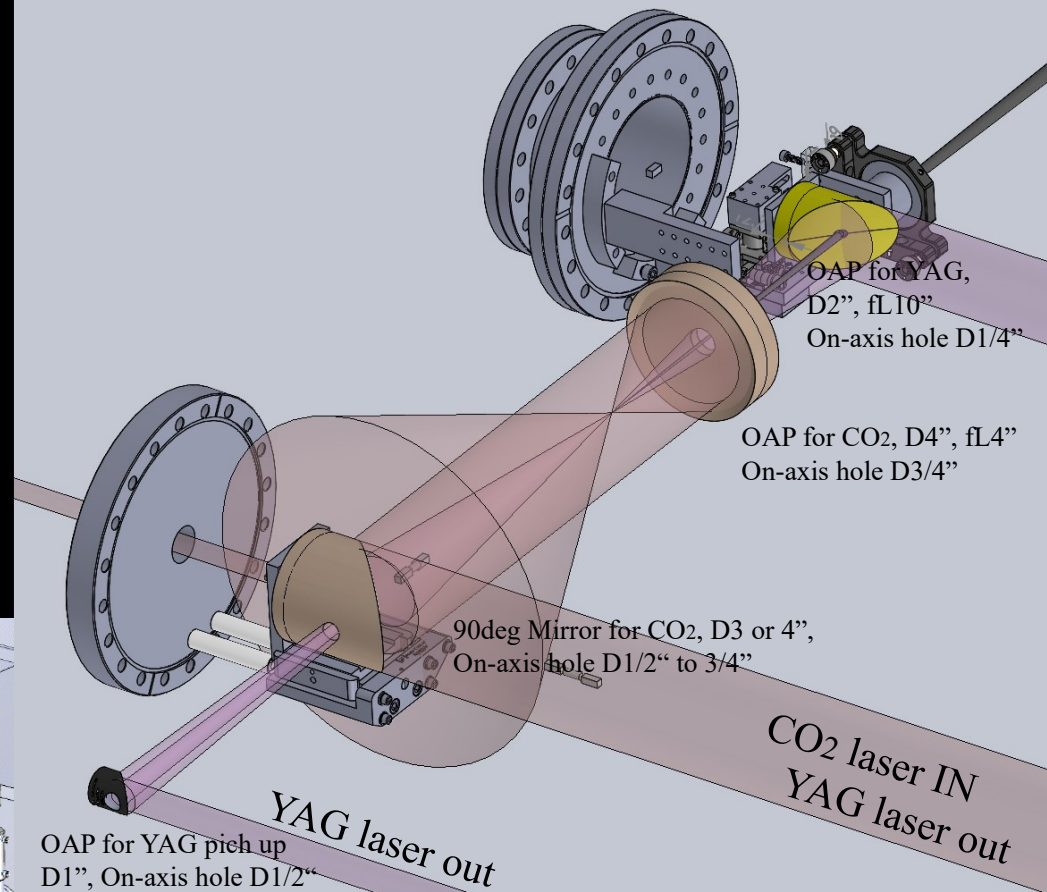
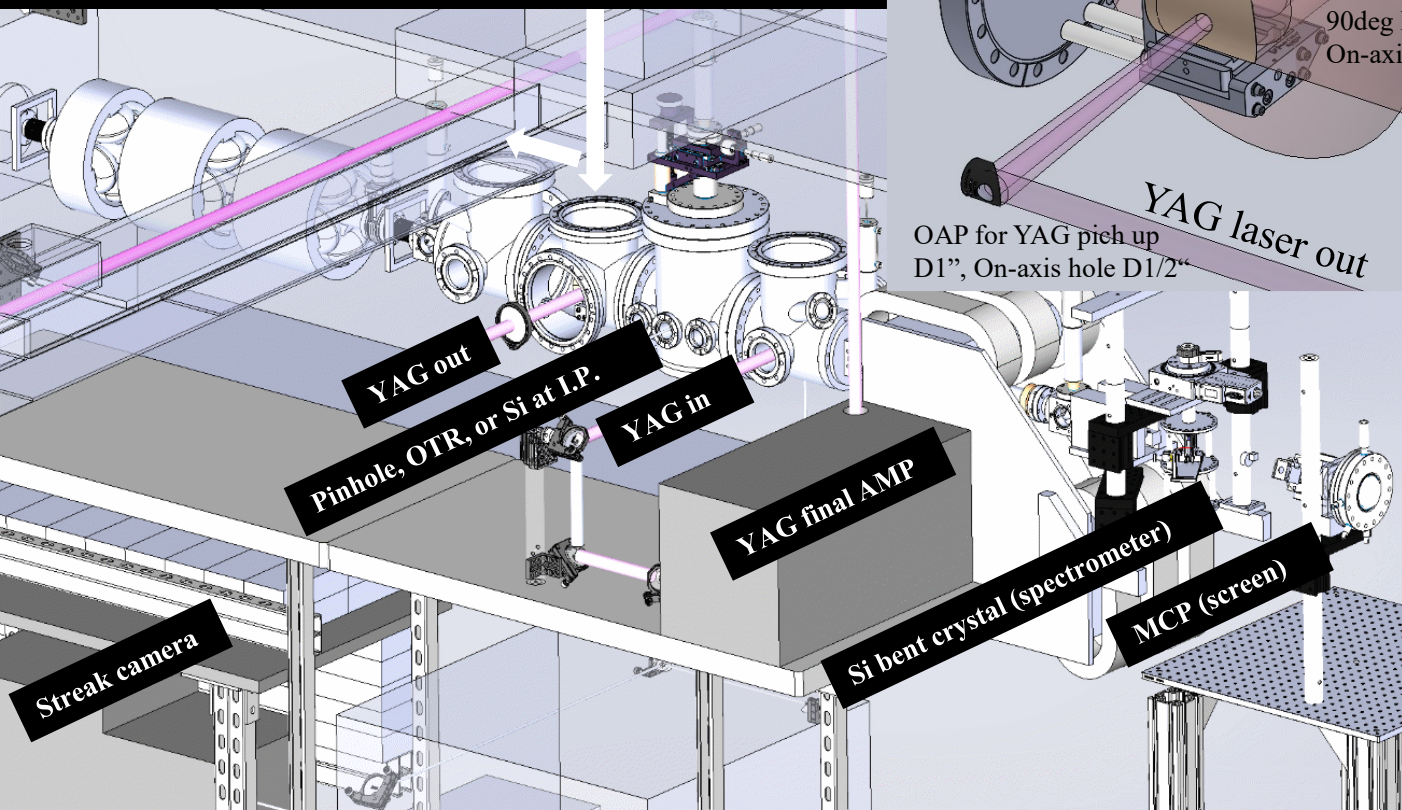
Fourier transform →



Experimental plans of AE87

Bi-harmonic Compton laser optics set up:

Input of CO₂ laser and YAG laser are opposite
CO₂ laser final optic has D 1/2 or 3/4 inch hole



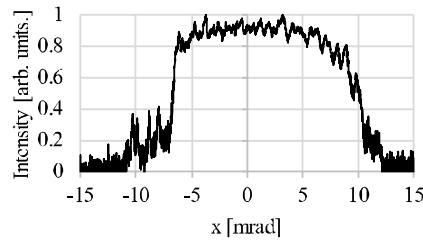
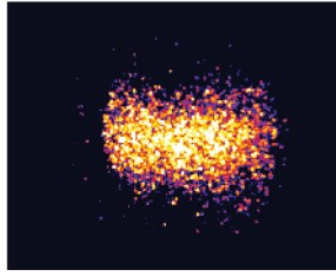
So far,
YAG-ICS at $h\nu$ 87.5
keV generated
last year:



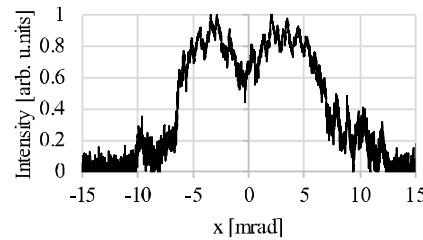
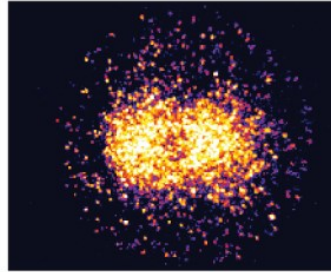
Return to AE87 → Result: Observed attenuation of 87.5 keV Hard X-ray in a single shot (10^5 - 10^{6-7} photons / shot)

Experiment

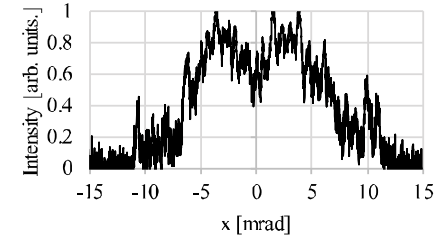
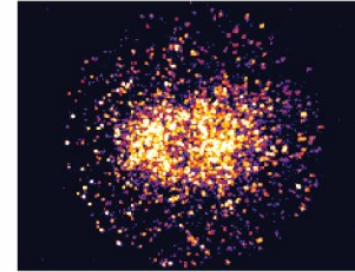
★ No-Filter



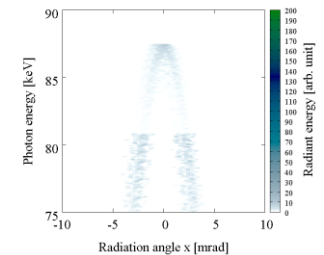
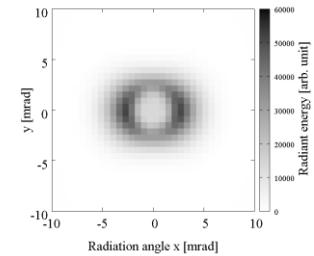
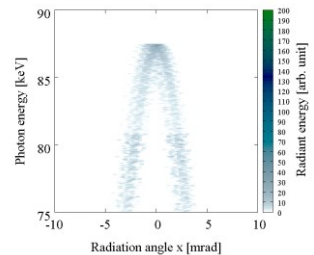
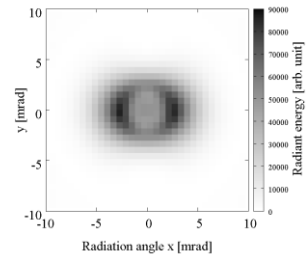
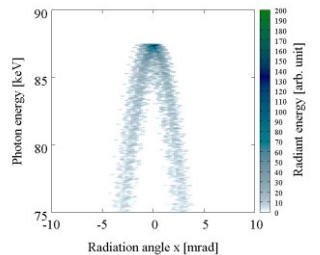
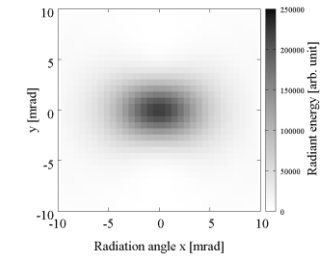
★ Au-100 μ m



★ Au-200 μ m

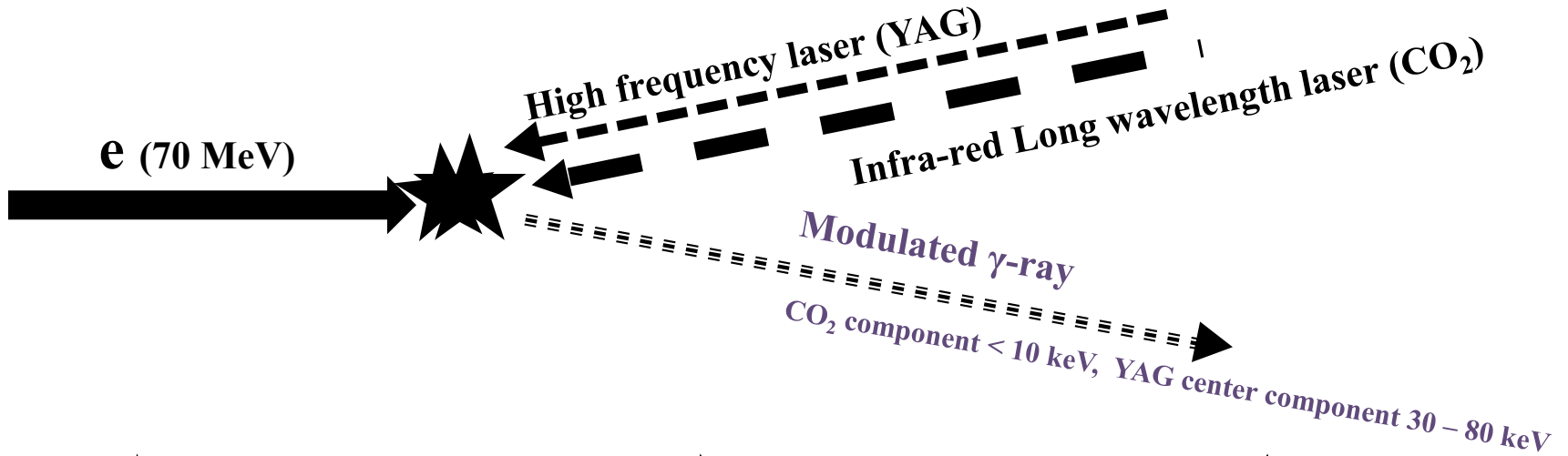


Numerical

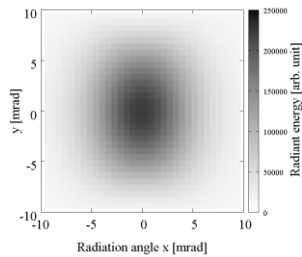


Sufficient contrast of radiation pattern of YAG laser ICS observed in a single shot

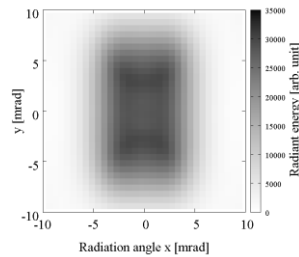
Numerical estimate of bi-harmonic spectrum by ATF parameter (Nonlinear Compton V2)



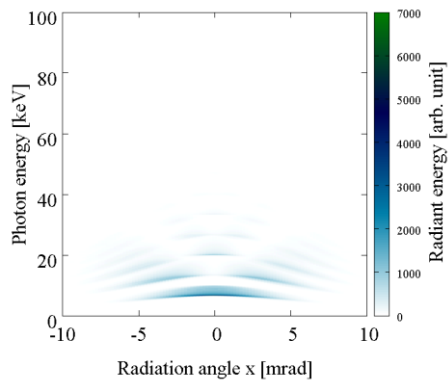
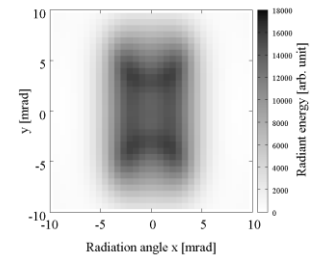
★ No-Filter



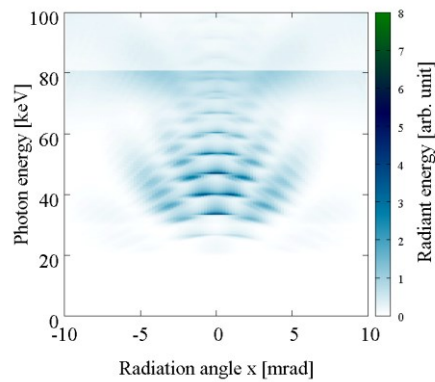
★ Au-100 μ m



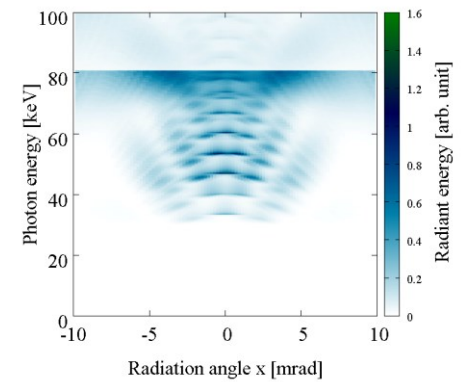
★ Au-200 μ m



Only CO_2 's component



Bi-harmonic YAG's component

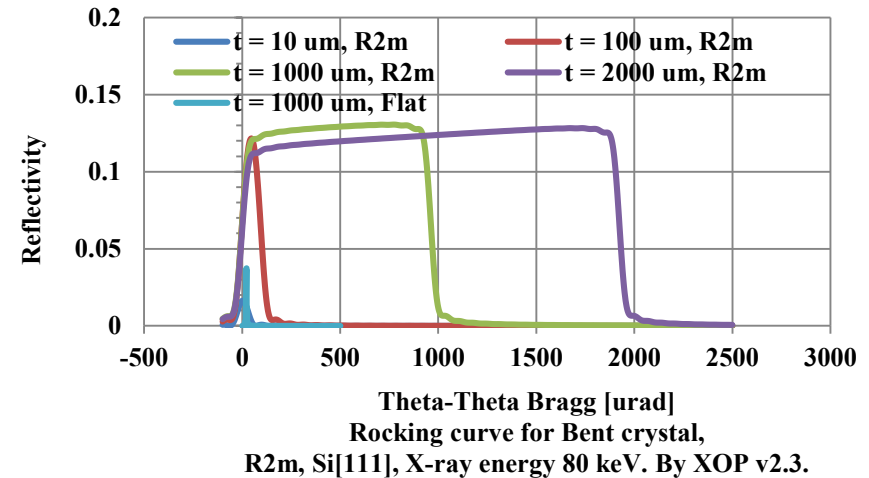
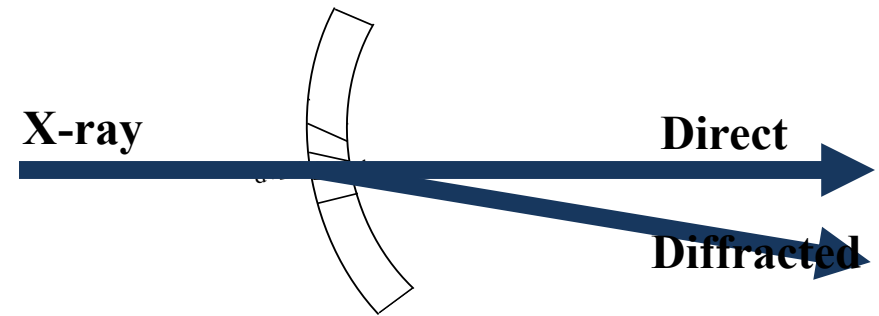
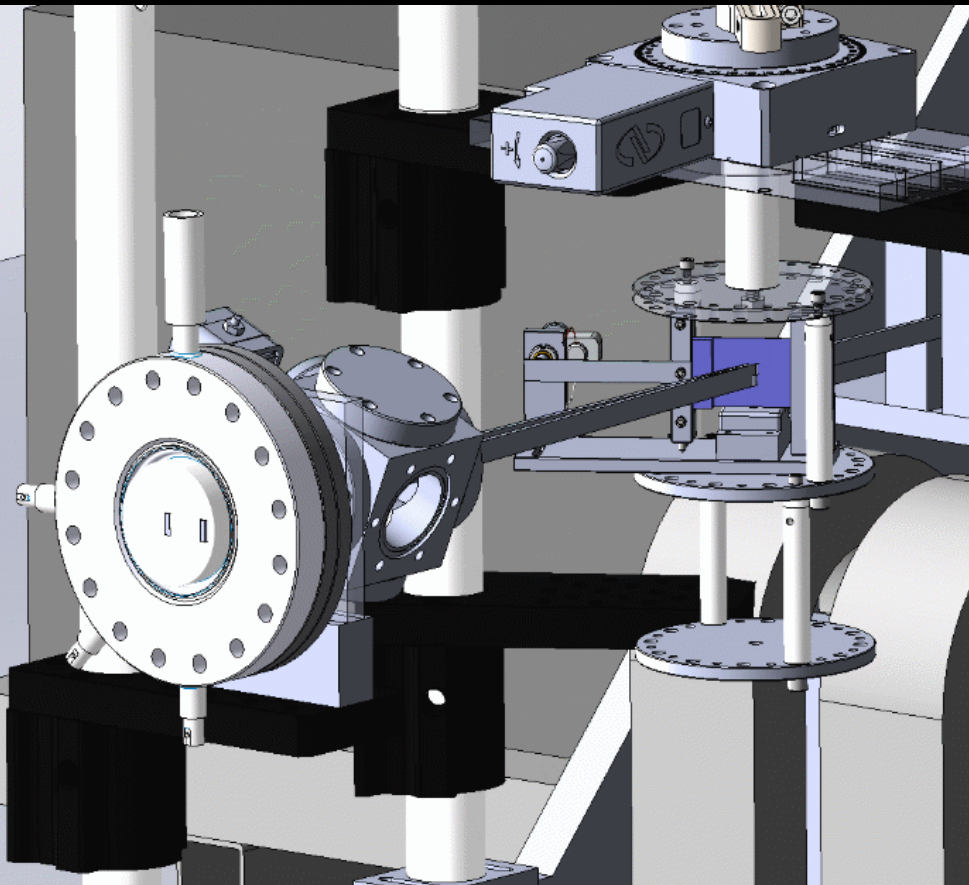


Single shot DDS measurement at X-ray energy of 87.5 keV for quantitative study

→ *Thick Laue Bent Crystal*
Efficiency > Bandwidth

(Collaboration with NSLS II 150 keV section, Z. Zhong)

Multi layer crystal: 5 – 20 keV (CO₂'s ICS component)
Thick crystal: 20 keV – 200 keV (YAG's ICS component)



- ★ Radius of curvature R: 2.5 m
- ★ Thickness: 1 mm
- ★ Bragg angle at 85keV: ~ 22 mrad
- ★ Crystal to MCP screen 0.3 m
- ★ Expected dispersion at screen: 10-20 mm:
- ★ Band width: ~ 10 keV
- ★ Reflectivity (Efficiency): ~10%

Stats: Diffraction not observed yet, as this is a hard experiment as expected

Application part math: (In appreciation of observed 87.5 keV characteristic): Examination of photon Activation with Gold Nano Particle (AuNP)

ICS X-ray energy $h\nu > 80.7 \text{ keV}$ (Au K-edge)

Enhanced does by monochromatic X-ray

Activation process:

X-ray absorption by Au K-shell



Emission of Auger electron from outer shell (~ 90% of energy)



Transfer energy to Radicals (OH etc) through water etc

Dose enhancement around surface of AuNP



Required Gold particle size, for escape of electron from NP :

100 nm ↔ Auger, L-edge 11.9-14.3 keV

10 nm ↔ Auger, M-edge 2.2-2.4 keV

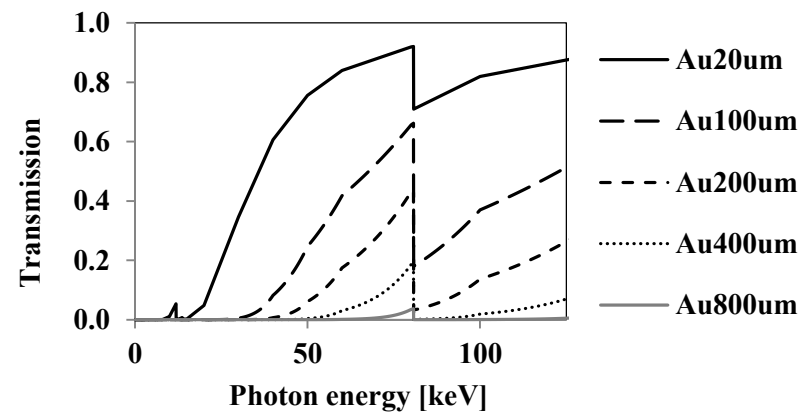
Penetration depth of keV electron in water (between AuNP)

→ ~ μm range

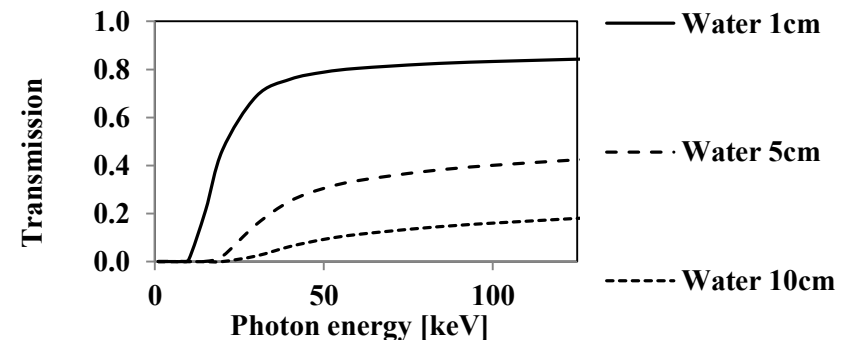
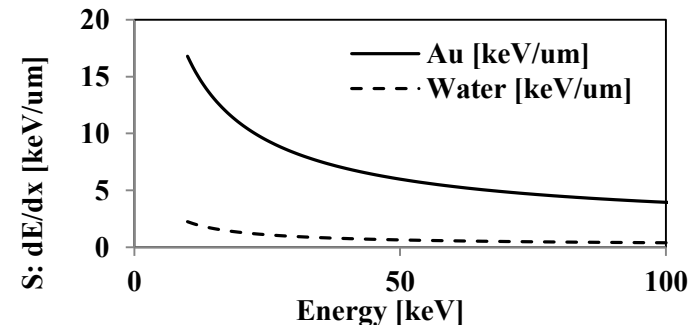
Spacing between particles

AuNP Dia 100 nm ↔ 10 μm , AuNP Dia 10 nm ↔ 1 μm ,

Because, 100 μm thick Au filter occupy 1% of volume in 1 cm thick volume of water.



Note: Density of 100 μm thick Au sheet in cubic cm of water of square volume corresponds to 194 mg / g uptake.
(Density of Au and H_2O are 19.3 g/cm^3 and 0.997 g/cm^3)



- - Hard X-ray flux requirement math- -

Assuming target dimension of $(L_{I.P. \text{ to target}} \times 1/\gamma)^2 = 1 \text{ cm}^3$,
(1 m away from I.P. at $1/\gamma = 10 \text{ mrad}$, at $\sim 60\text{-}70 \text{ MeV}$ electron beam)

Radiation dose per kg of water per shot:
 $1 [\text{Gy}] = 1 \text{ J} / (10 \text{ cm})^3 \leftrightarrow 1 \text{ mJ} / (1 \text{ cm})^3$.

While energy per X-ray pulse:
 $(10^{6-7} \text{ photons}) \times (87.5 \text{ keV}) \times (1.6 \times 10^{-19}) \sim 0.1 - 1 \mu\text{J} / \text{shot}$

$\uparrow\downarrow$

Total irradiation shot required: $1 \text{ mJ} / 0.1 \mu\text{J} = 10.000 \text{ shot}$

Flux can be increased by further tight focus down to a several $\sigma_e \sim \mu\text{m} \rightarrow \text{X10 \& YAG laser pulse} > 1 \text{ J} \rightarrow \times 10$

NOTE: But bandwidth will be 10s % range:

$$\omega_{ICS} \approx \frac{4\gamma_0^2 \omega_L}{1 + \gamma_0^2 \theta^2 + \frac{a_0^2}{2}}, \quad \gamma_0^2 \theta^2 \leftrightarrow \gamma_0^2 \left(\frac{\Delta p_{x,y}}{p_z} \right)^2$$

$\sigma_{x,y} = 20 \mu\text{m} \rightarrow \text{beta function } \beta = 3 \text{ cm} \leftrightarrow \sigma' \sim 0.6 \text{ mrad} \leftrightarrow \text{X-ray bandwidth: } \sim 1 \%$

$\sigma_{x,y} \sim 5 \mu\text{m} \rightarrow \text{beta function } \beta \sim 1 \text{ mm} \leftrightarrow \sigma' \sim 5 \text{ mrad} \leftrightarrow \text{X-ray bandwidth: } \sim 10 \%$

$1/\gamma_0 \sim 7.3 \text{ mrad}$ for 70 MeV e-beam, Normalized emittance 2 mm mrad case

{OR, can we lower e-beam emittance more??}

Direction depending on purposes:

- ★ Narrow band X-ray production based on single shot detection
 - ★ Less narrow band high flux X-ray production
- ★ Strong field physics for Bi-harmonic & OAM production



IN PARALLEL :

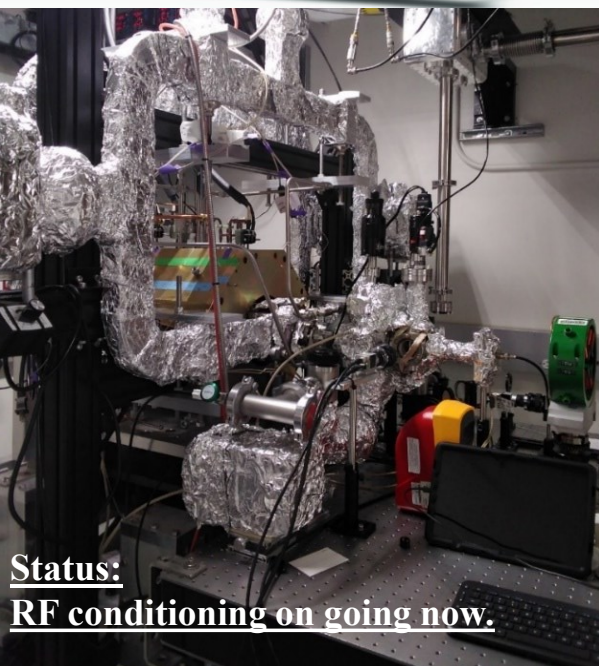
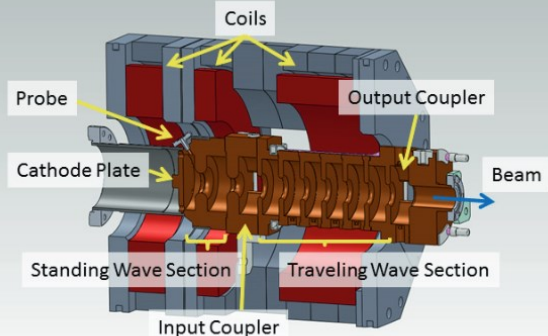
**University scale test facility
in Westwood L.A., UCLA campus:**

Based on S-band Hybrid gun:

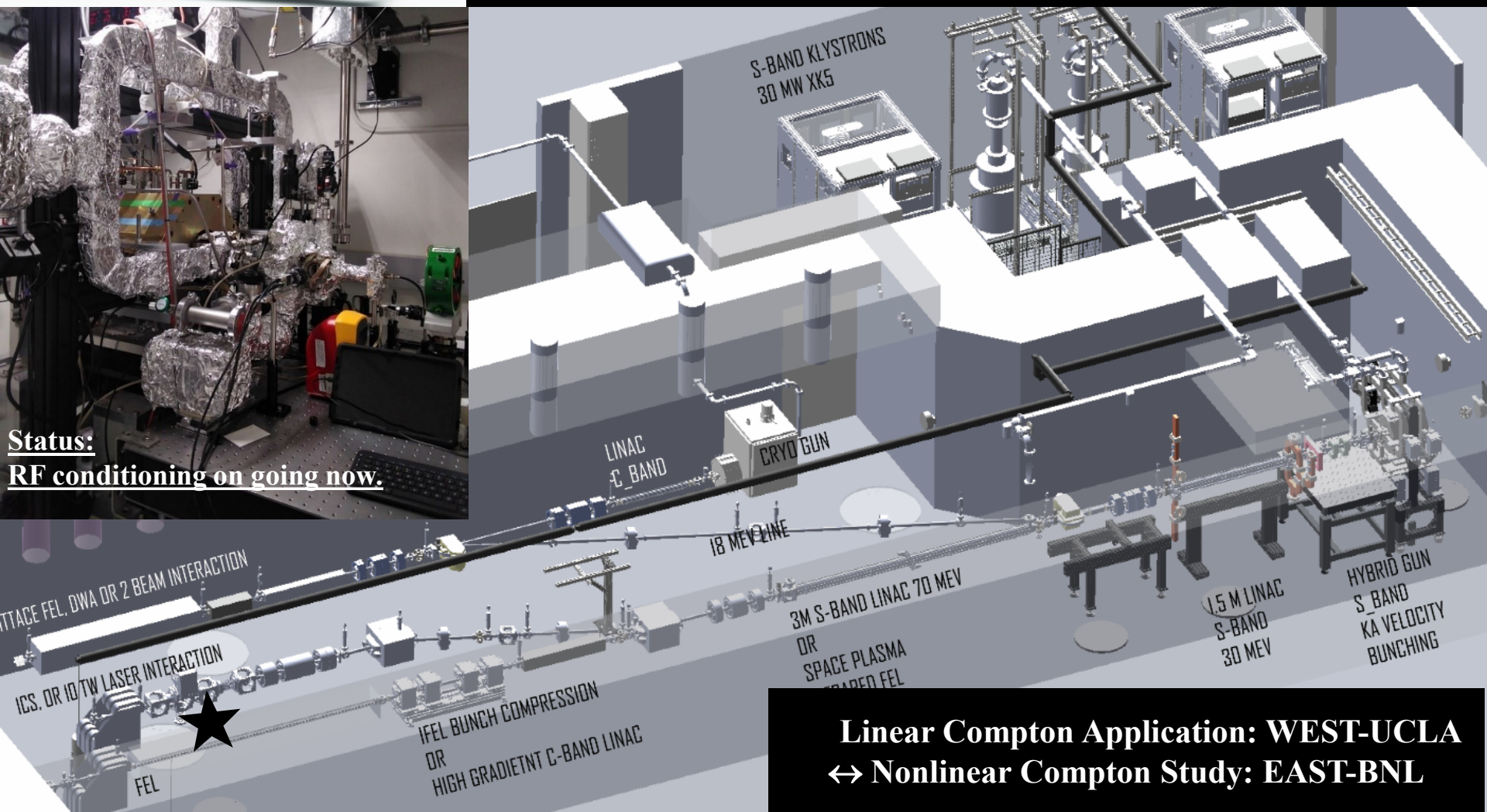
RF gun and a short linac for velocity bunching, 100s fs, in one structure

**REF: A. Fukasawa et al., "Progress on the hybrid gun project at UCLA",
Physics Procedia, vol. 52, pp. 2–6, 2014.**

& R & D of Cryo cooled high gradient ~200 MV/m, low emittance gun: Emittance $\sim 1/\gamma^2$



Status:
RF conditioning on going now.



**Linear Compton Application: WEST-UCLA
↔ Nonlinear Compton Study: EAST-BNL**

FUTURE PLAN 2022-2024yr

IN BNL ATF:

- ✂ **Set up nonlinear CO₂ ICS with upgraded ATF's multi TW CO₂ laser at $a_0 \sim 2$**
- ✂ **Observe higher order harmonics & benchmark a_0 & X-ray production per pulse**
- ✂ **Measure 30 keV CO₂ ICS X-ray spectrum by thick bent crystal spectrometer**
- ✂ **Single shot DDS measurement by Bent crystal at ~100 keV range by YAG ICS**
- ✂ **Measure spectrum of Harmonics by circular polarized CO₂ laser (ATF's Polarization rotator)**
- ✂ **Production of Bi-Harmonic X-ray, A few cycle X-ray pulse**

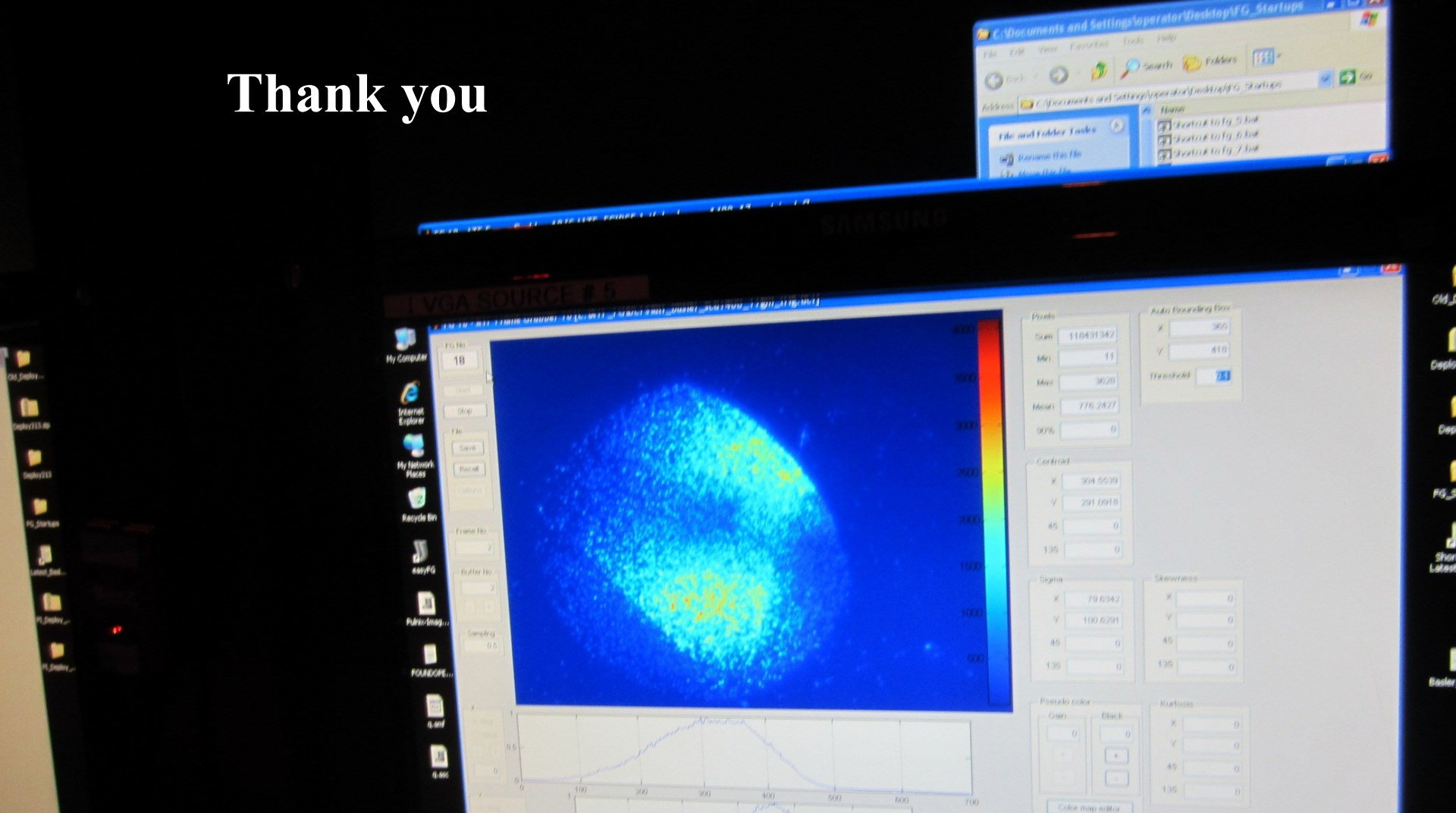
IN UCLA:

- ✂ **Keep constructing a PBPL-LINAC in Westwood**
- ✂ **Soft X-ray ICS by Ti: Sapphire laser, 20 MeV e-beam (Let's cover all spectrum range)**

Conclusion:

Inverse Compton Scattering Study seems to be simple but endless

Thank you



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