



MAX-PLANCK-INSTITUT
FÜR PHYSIK



Hosing of a long relativistic particle bunch induced by an electron bunch

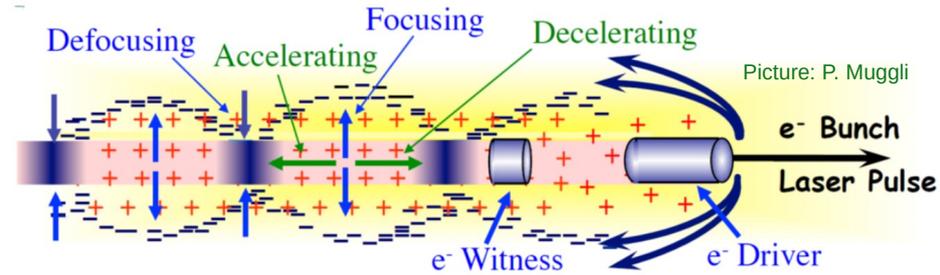
T. Nechaeva¹, L. Verra², J. Pucek¹, M. Bergamaschi¹,
L. Ranc¹, G. Zevi Della Porta^{1,2} and P. Muggli¹
on behalf of the AWAKE Collaboration

¹ Max-Planck-Institute for Physics, Munich, Germany

² CERN, Geneva, Switzerland

tatiana.nechaeva@cern.ch

Introduction: PWFA



- **Linear theory:**

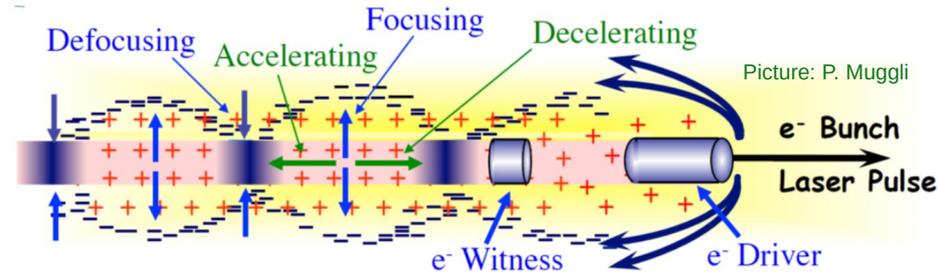
$$\sigma_t \leq 1/\omega_{pe}$$

$$\sigma_r \leq c/\omega_{pe}$$

drive bunch

$$E_{WB} = \frac{m_e c \omega_{pe}}{e} \propto \sqrt{n_{pe}}$$

Introduction: PWFA



Gonsalves et al., Phys. Rev. Lett., 122 084801 (2019)	Blumenfeld et al., Nature 445 741 (2007)
~40 fs laser pulse, ~40 J	~60 fs e ⁻ bunch, ~50 J
$n_{pe} \sim 3 \cdot 10^{17} \text{ cm}^{-3}$	$n_{pe} \sim 2.7 \cdot 10^{17} \text{ cm}^{-3}$
<u>~39 GeV/m</u>	<u>~52 GeV/m</u>
short drivers	

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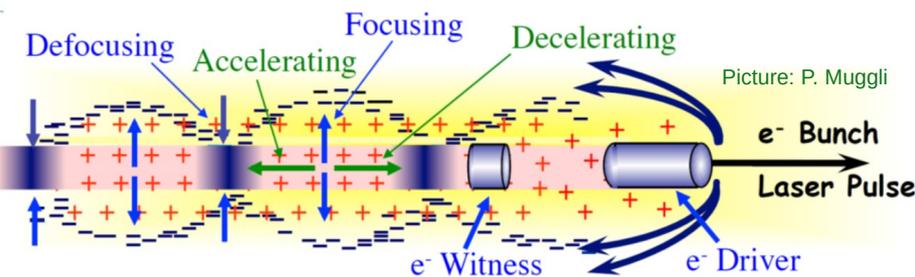
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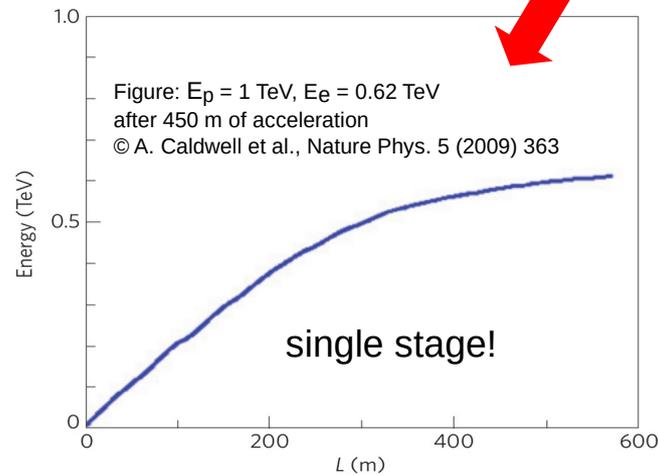
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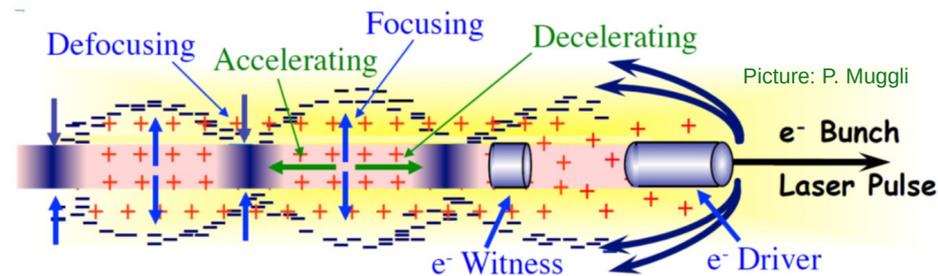
SPS p⁺ bunch → **19.2 kJ**

LHC p⁺ bunch → **135 kJ** →

- High energy
- Drives wakefields for long distance →
- No need for staging



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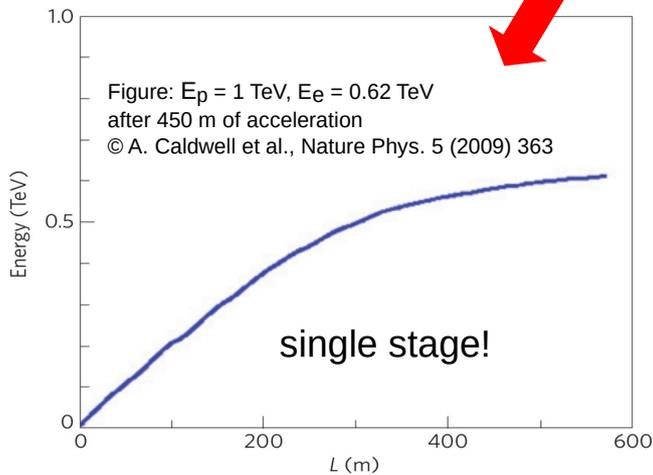
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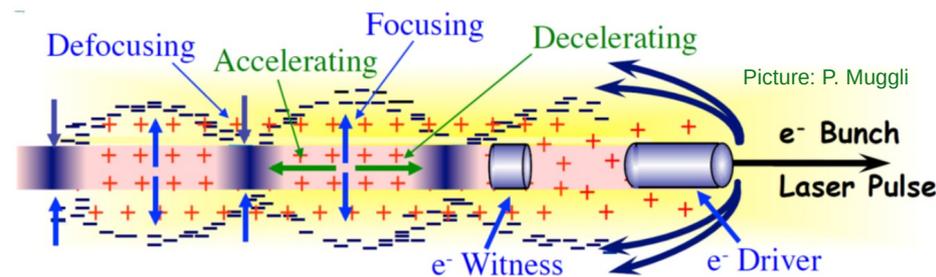
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However: $\sigma_t \sim 220 \text{ ps} \rightarrow$ **long driver** →
 $n_{pe} \sim 10^9 \text{ cm}^{-3} \rightarrow E_{WB} \sim \text{MV/m}$



Introduction: PWFA



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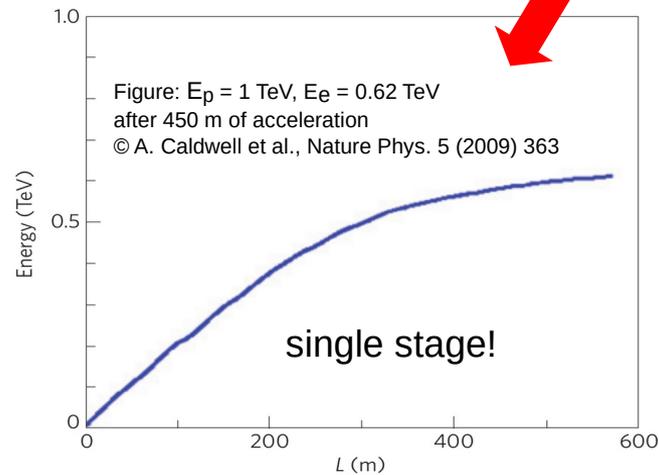
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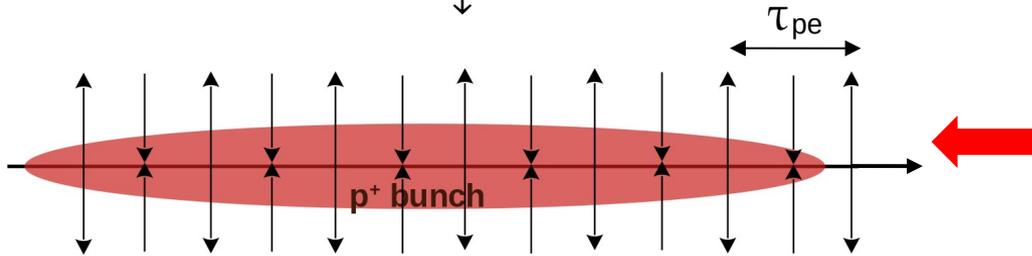
Self-modulation!

Self-Modulation

Long driver



(over)dense plasma

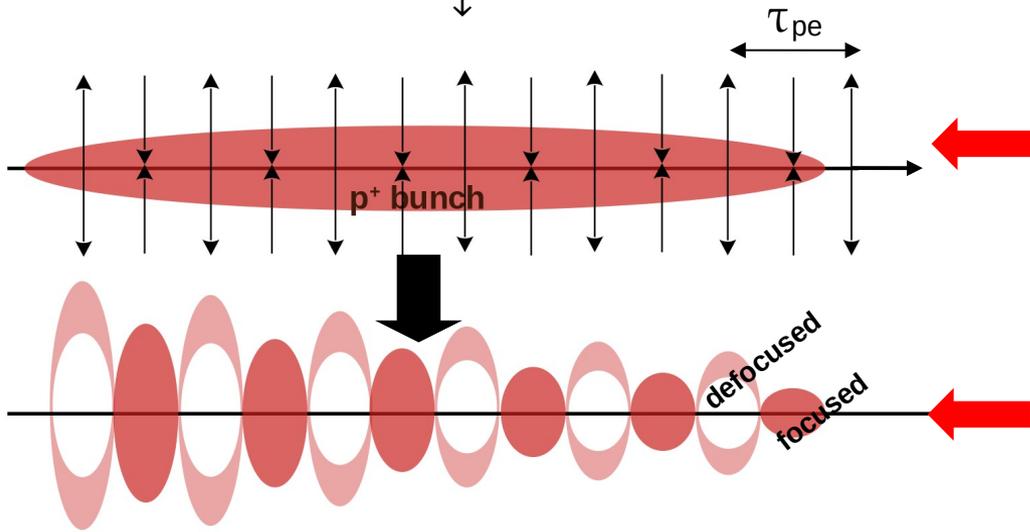


- Initial transverse wakefields →
- Periodic focusing/defocusing force →

Self-Modulation

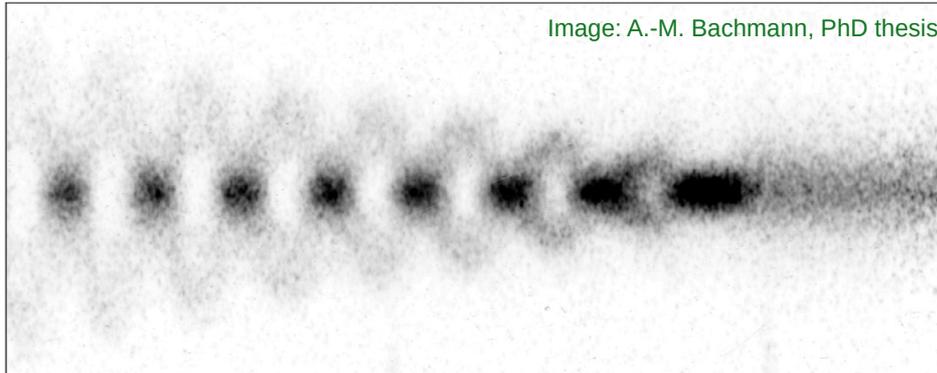
Long driver

(over)dense plasma



- Initial transverse wakefields →
- Periodic focusing/defocusing force →
- Bunch density modulation →
- Train of micro-bunches → period $\sim \tau_{pe}$
- Micro-bunch length $< \tau_{pe}$ →

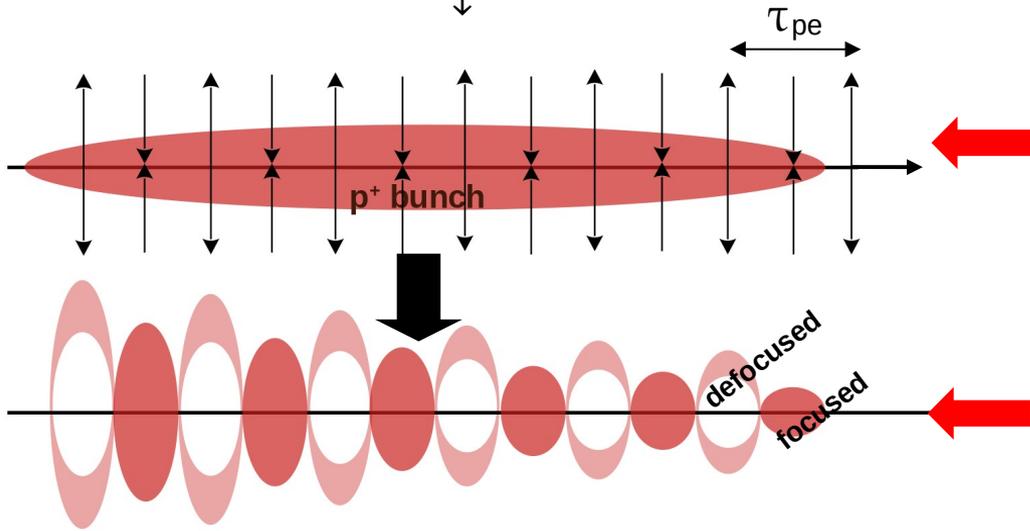
Image: A.-M. Bachmann, PhD thesis



Self-Modulation

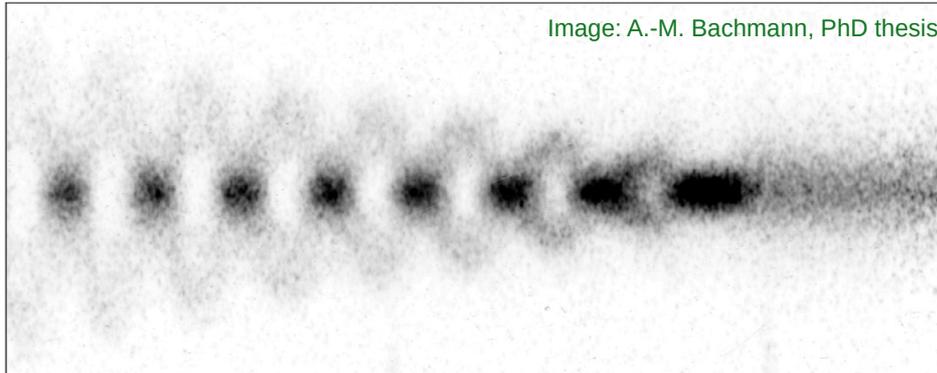
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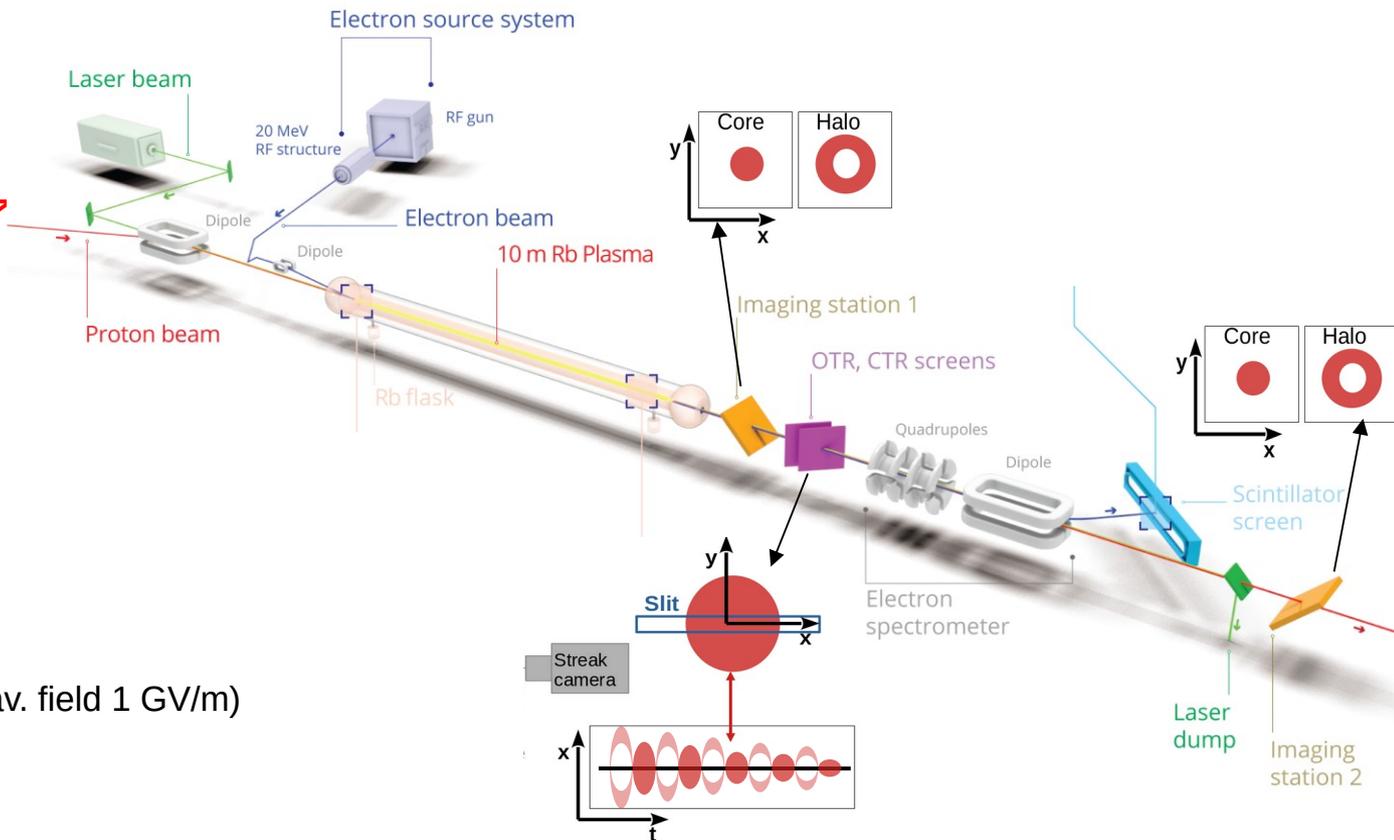
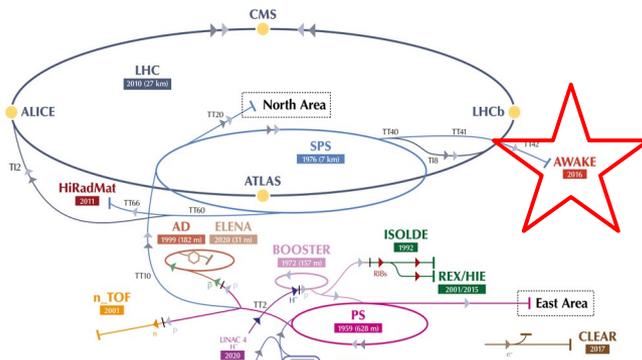
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- **Resonant driving of large amplitude wakefields**

Image: A.-M. Bachmann, PhD thesis



AWAKE Experiment

The CERN accelerator complex
Complexe des accélérateurs du CERN

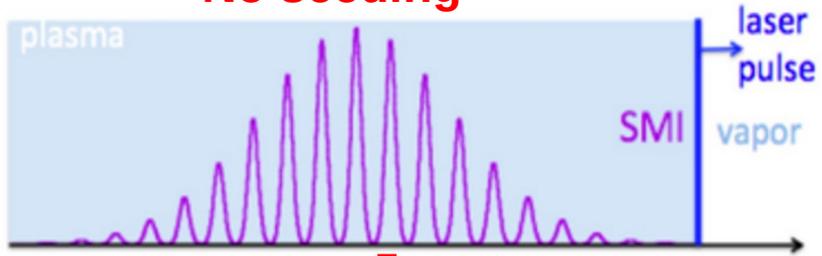


Goals:

- Study SM of the p^+ bunch
- Study e^- bunch acceleration (with av. field 1 GV/m)
- External injection
- Bunch quality preservation at 10mm-mrad
- Scalability (two stages – modulator and accelerator)
- First HEP application → fixed target experiment

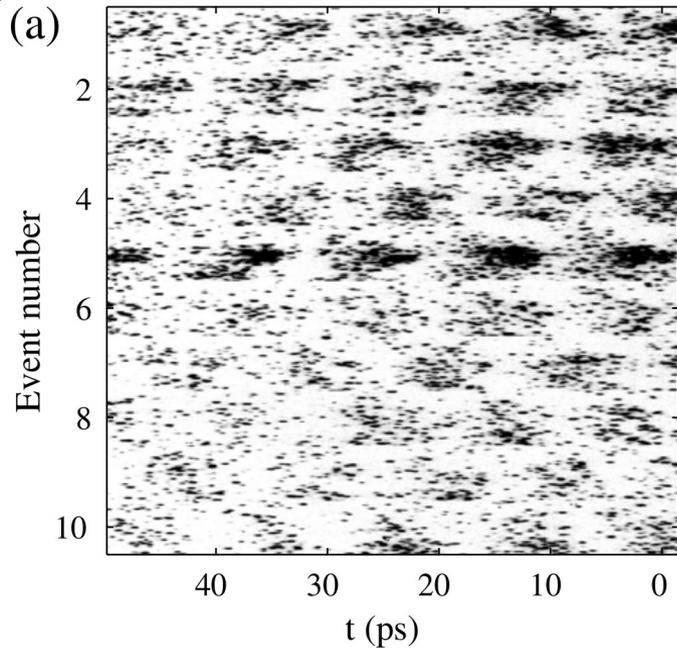
Self-modulation: instability \rightarrow seeded

No seeding

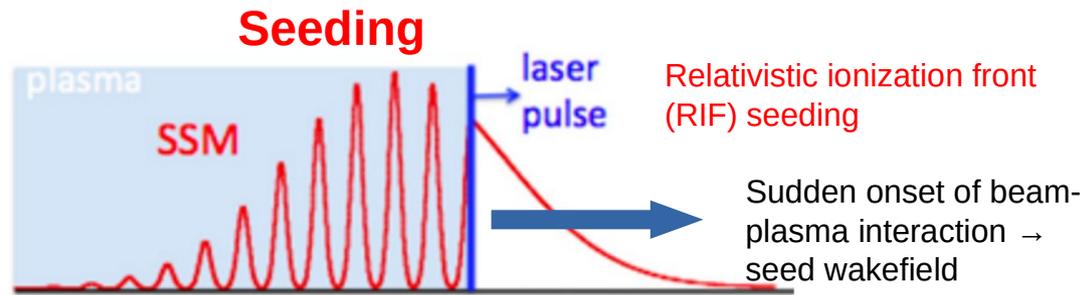
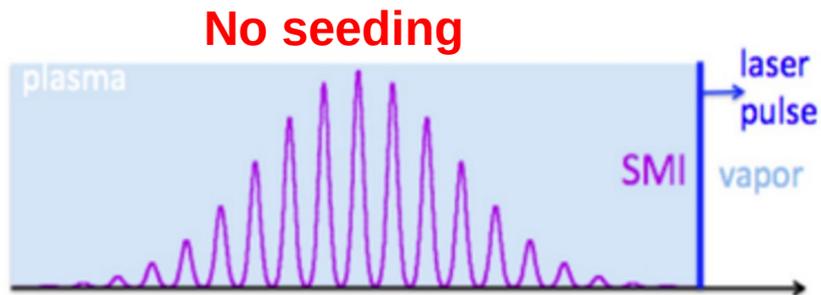


F. Batsch et al., Phys. Rev. Lett. 126, 164802 (2021)

Single events

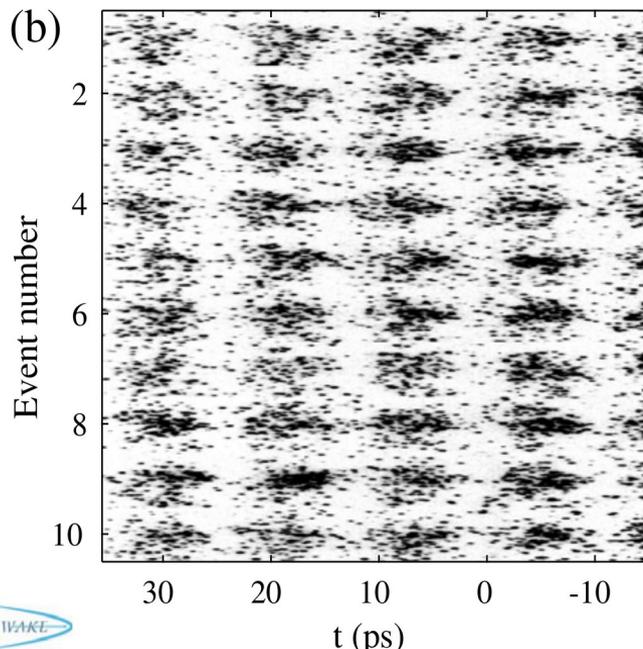
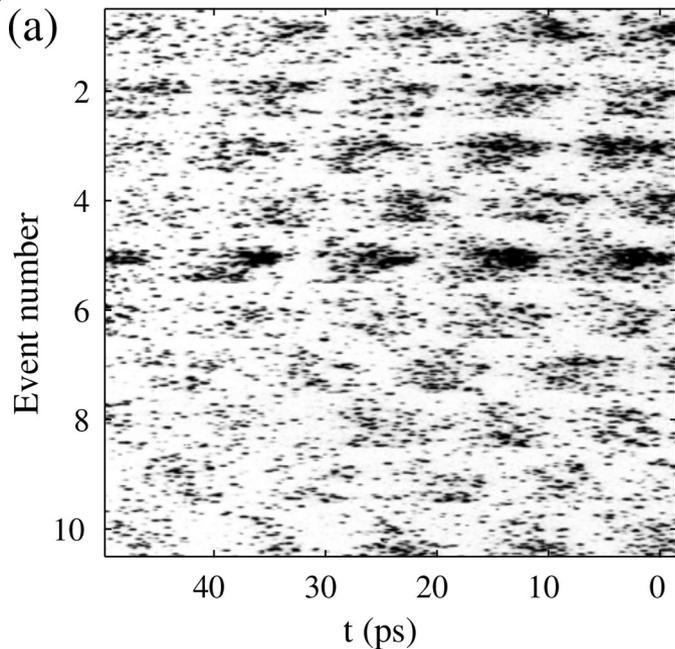


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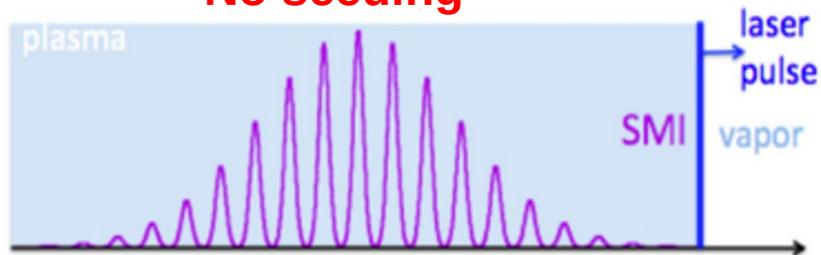


\rightarrow Reproducible outcome!

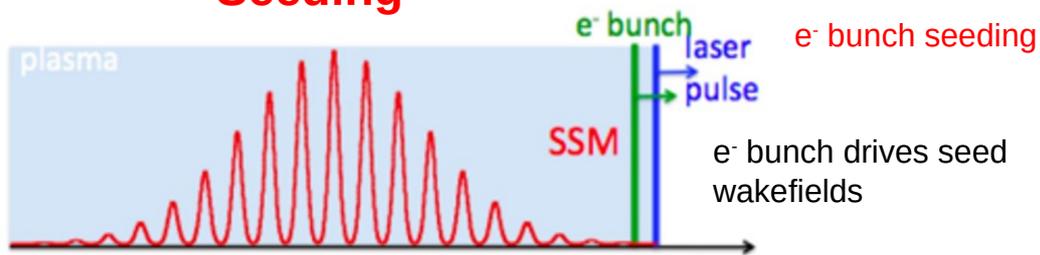
$\Delta t / \tau_{pe} \sim 6\%$,
 $\tau_{pe} = 2\pi / \omega_{pe}$

Self-modulation: instability \rightarrow seeded

No seeding

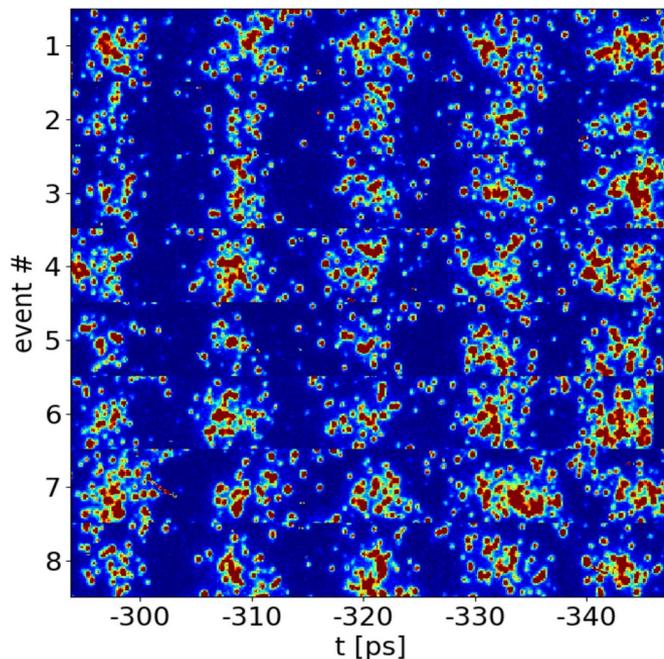
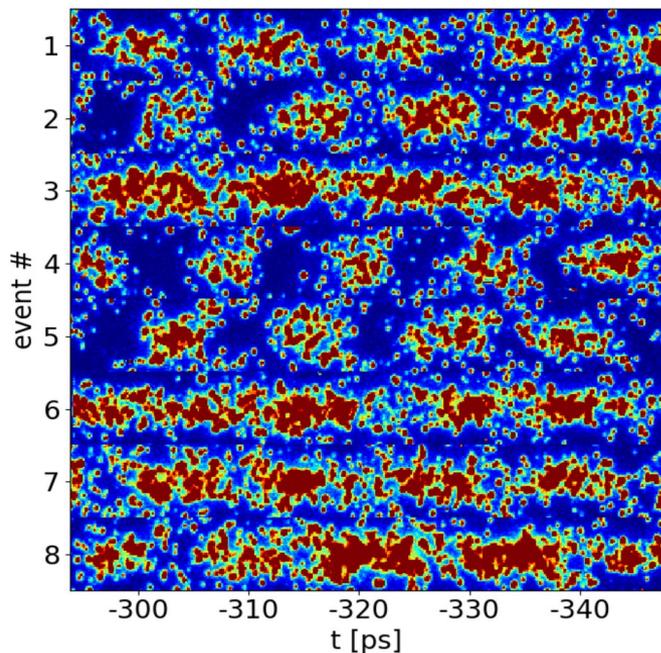


Seeding



L. Verra et al., Phys. Rev. Lett. 129 024802 (2022)

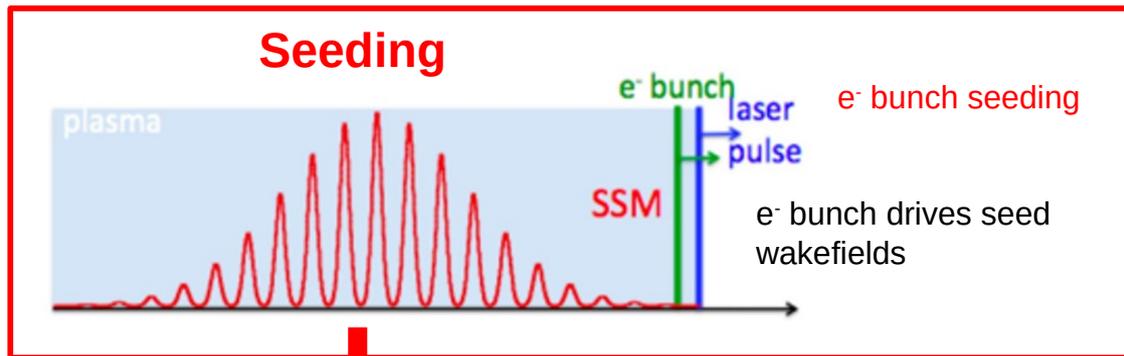
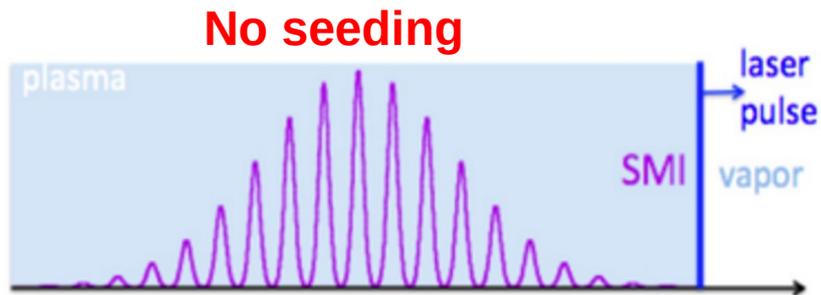
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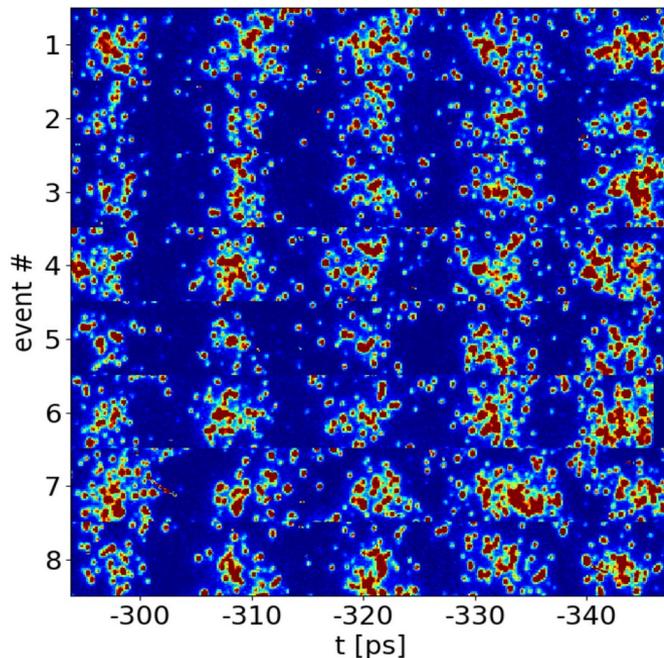
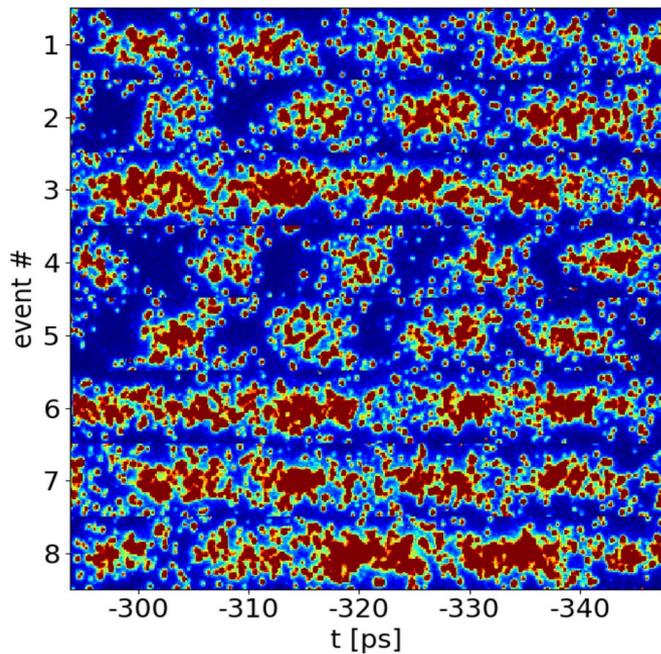
$$\Delta t / \tau_{pe} \sim 7\%,$$
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Self-modulation: instability \rightarrow seeded



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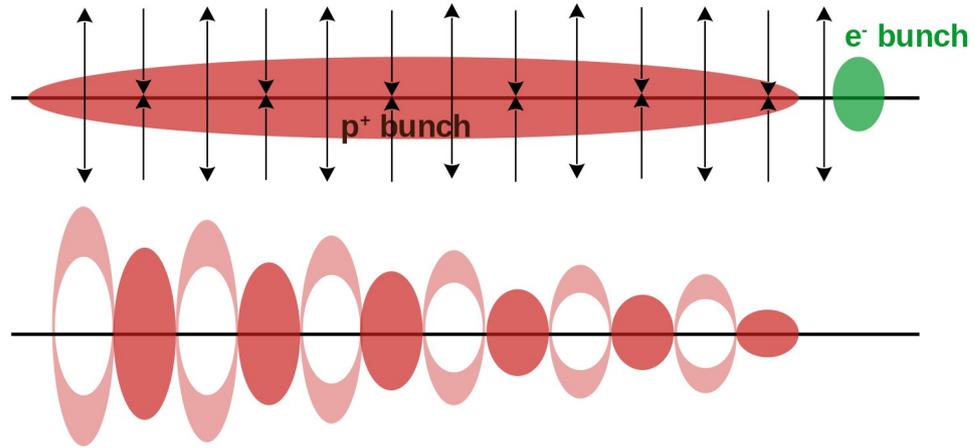
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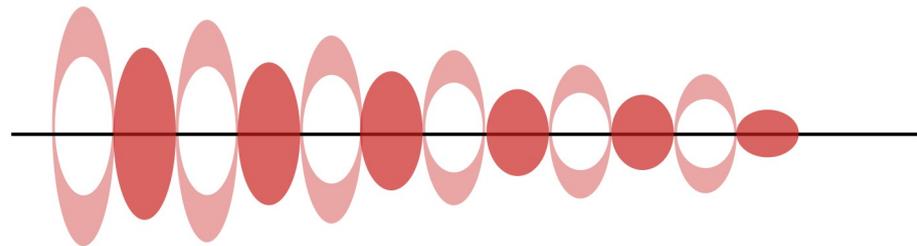
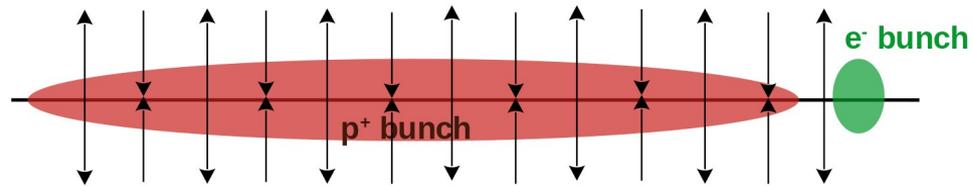
eSSM vs eSSM+Hosing



e^- and p^+ bunches aligned
force on p^+ bunch centroid = 0
force on p^+ bunch slice \rightarrow focusing/defocusing

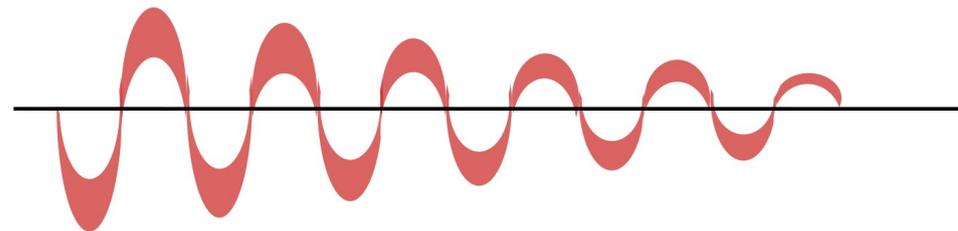
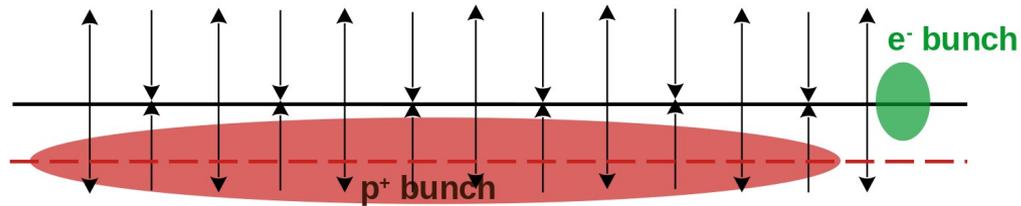
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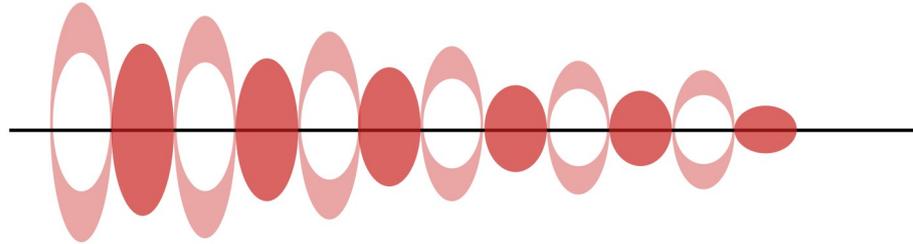
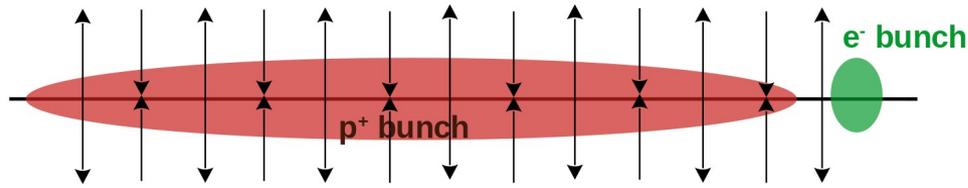
eSSM



e⁻ and p⁺ bunches misaligned
 force on p⁺ bunch centroid ≠ 0 → hosing-- **centroid position oscillation**
 force on p⁺ bunch slice → focusing/defocusing

Hosing + eSSM
 ↓ ↓
 one plane plane ⊥ hosing

eSSM vs eSSM+Hosing

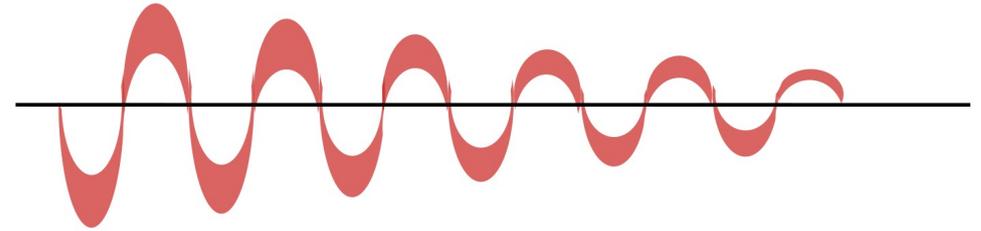
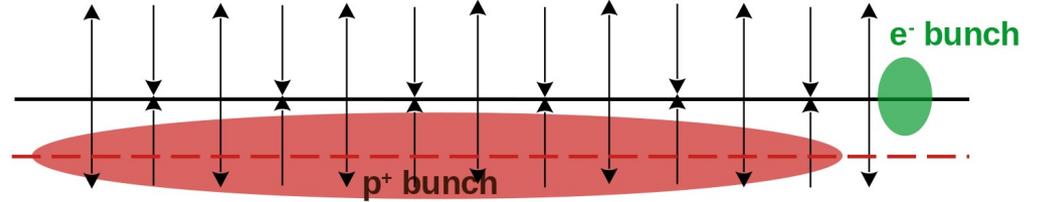


e^- and p^+ bunches aligned
 force on p^+ bunch centroid = 0
 force on p^+ bunch slice \rightarrow focusing/defocusing



eSSM

- Hosing occurs in the plane of misalignment
- eSSM \rightarrow plane \perp hosing
- Hosing and eSSM caused by the same wakefields \rightarrow
- Both processes are reproducible



e^- and p^+ bunches misaligned
 force on p^+ bunch centroid $\neq 0 \rightarrow$ hosing -- **centroid position oscillation**
 force on p^+ bunch slice \rightarrow focusing/defocusing



Hosing + eSSM

\downarrow \downarrow
 one plane plane \perp hosing

Hosing in PWFA

- Hosing is **detrimental for acceleration process** →
- Important to study for the future PWFA →
- **Know how to suppress**
- Many studies on suppression

Mitigation of the onset of hosing in the linear regime through plasma frequency detuning

Mariana Moreira,^{1,*} Patric Muggli,^{2,3} and Jorge Vieira¹
¹GoLP/Instituto de Plasmas e Fusão Nuclear, Instituto Superior Técnico, Universidade de Lisboa, 1049-001 Lisboa, Portugal
²Max Planck Institute for Physics, D-80805 Munich, Germany
³CERN, CH-1211 Geneva, Switzerland

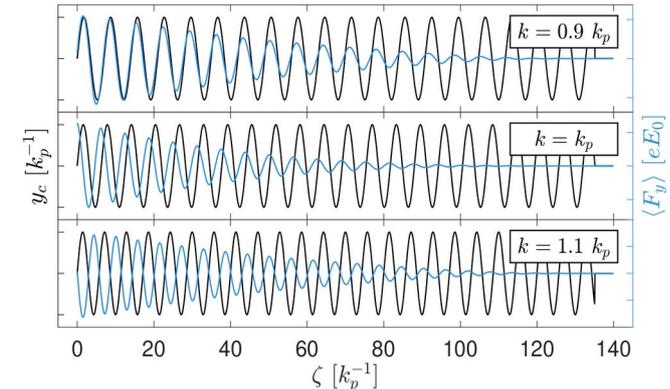


Figure: Initial centroid (black) and average transverse force (blue) for three different seed wavenumbers, obtained from 2D OSIRIS simulations at $z = 0$.
M. Moreira, P. Muggli, J. Vieira, arXiv: 2207.14763v1 (2022)

Towards experimental investigation of hosing instability mitigation at the PITZ facility

G Loisch *et al* 2020 *J. Phys.: Conf. Ser.* **1596** 012003

PHYSICAL REVIEW LETTERS **121**, 264802 (2018)

Suppression of Beam Hosing in Plasma Accelerators with Ion Motion

T. J. Mehrling,^{*} C. Benedetti, C. B. Schroeder, E. Esarey, and W. P. Leemans
Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA

PRL **112**, 205001 (2014)

PHYSICAL REVIEW LETTERS

week ending
23 MAY 2014

Hosing Instability Suppression in Self-Modulated Plasma Wakefields

J. Vieira,^{1,3,*} W. B. Mori,² and P. Muggli³

¹GoLP/Instituto de Plasmas e Fusão Nuclear, Instituto Superior Técnico, Universidade de Lisboa, 1049-001 Lisboa, Portugal

²Department of Physics and Astronomy, University of California Los Angeles, California 90095, USA

³Max-Planck-Institut für Physik, 80805 München, Germany

(Received 13 December 2013; published 21 May 2014)

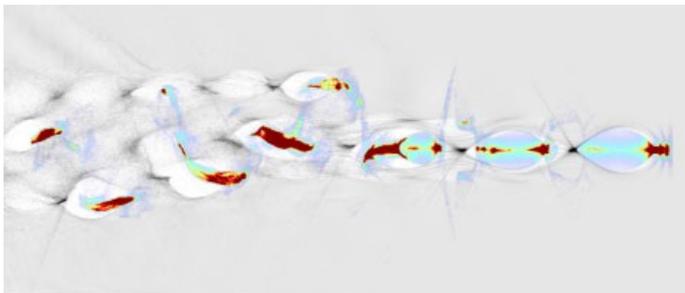
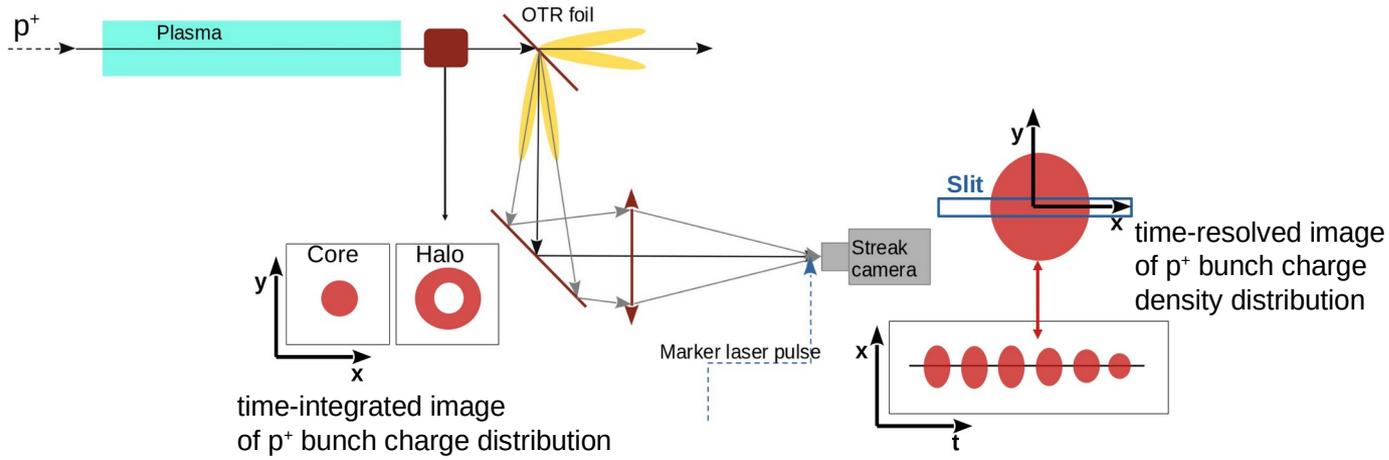
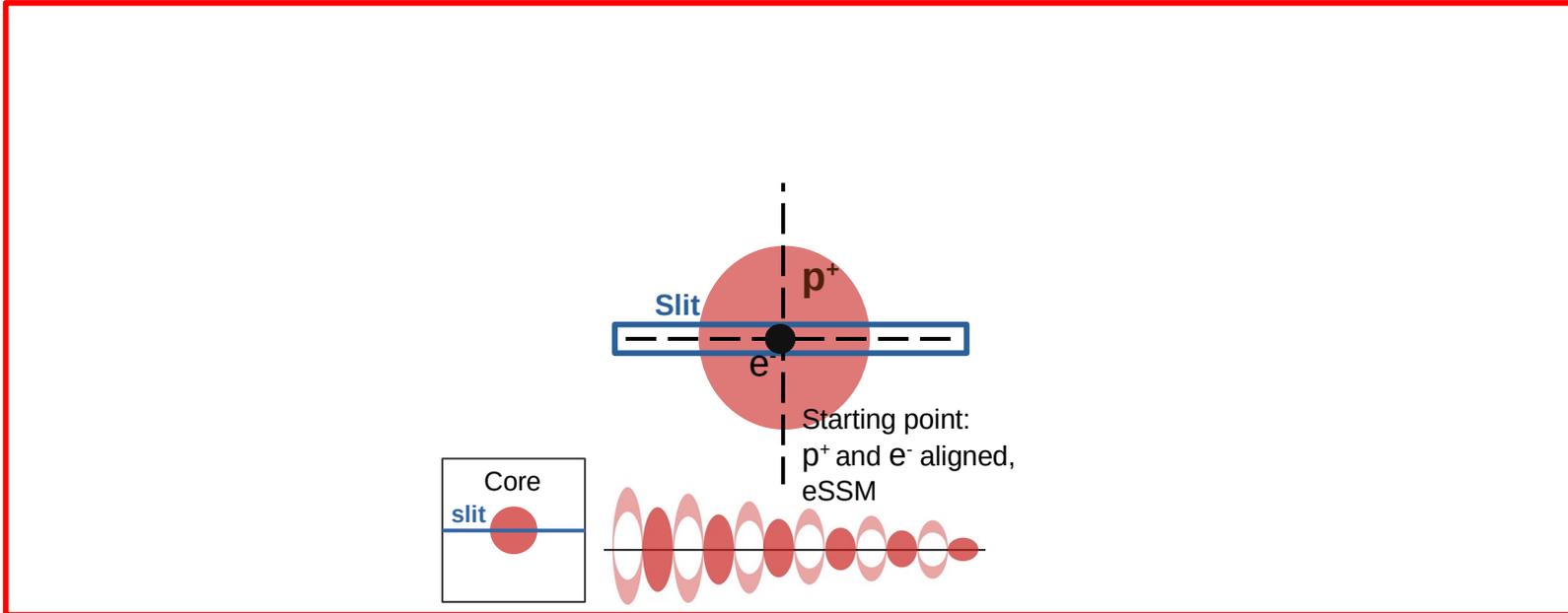
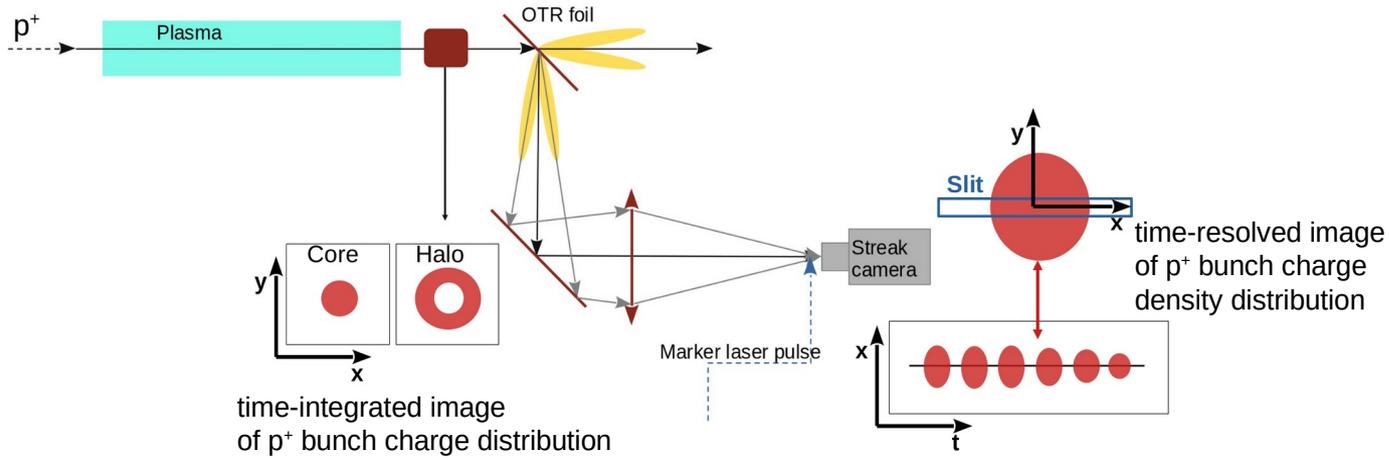


Figure: Beam breakup due to hosing growth in nonlinear blowout regime.
J. Vieira, W. Mori, P. Muggli, Phys. Rev. Lett. **112**, 205001 (2014)

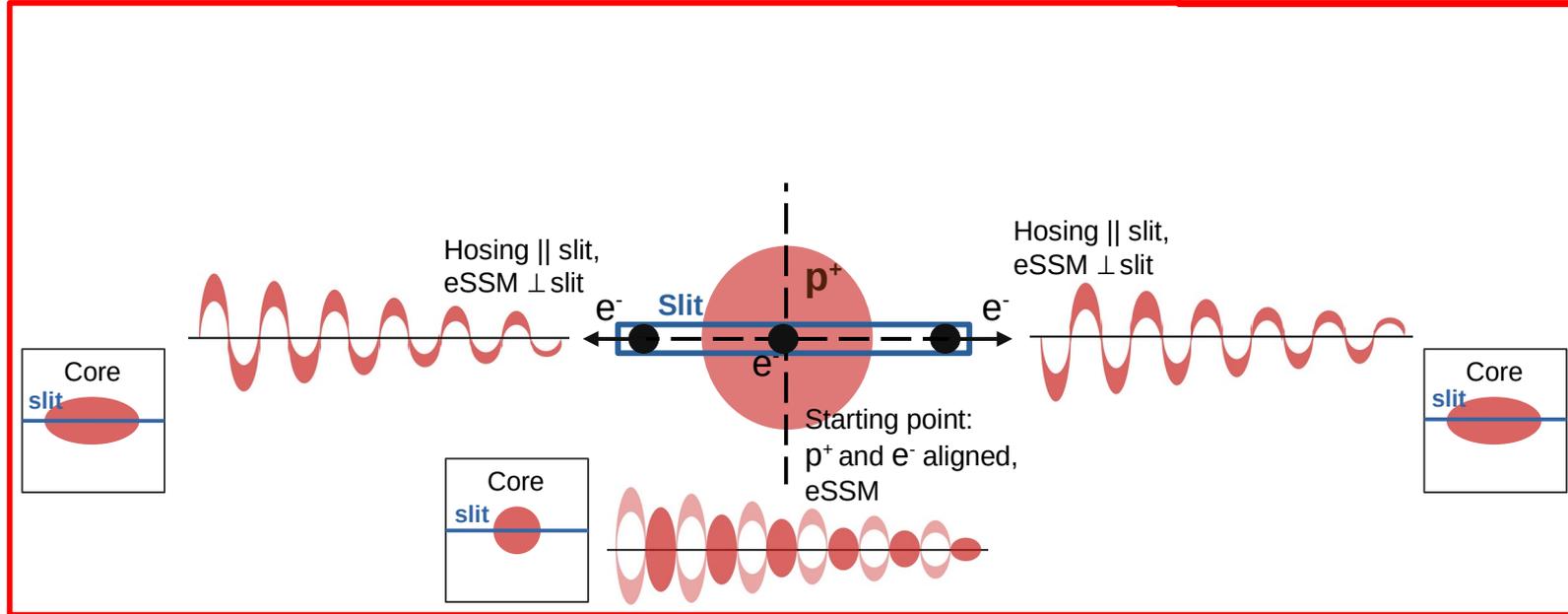
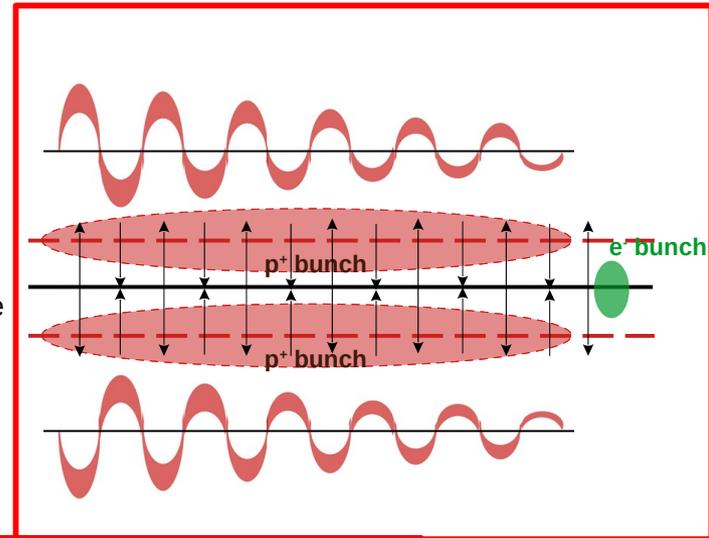
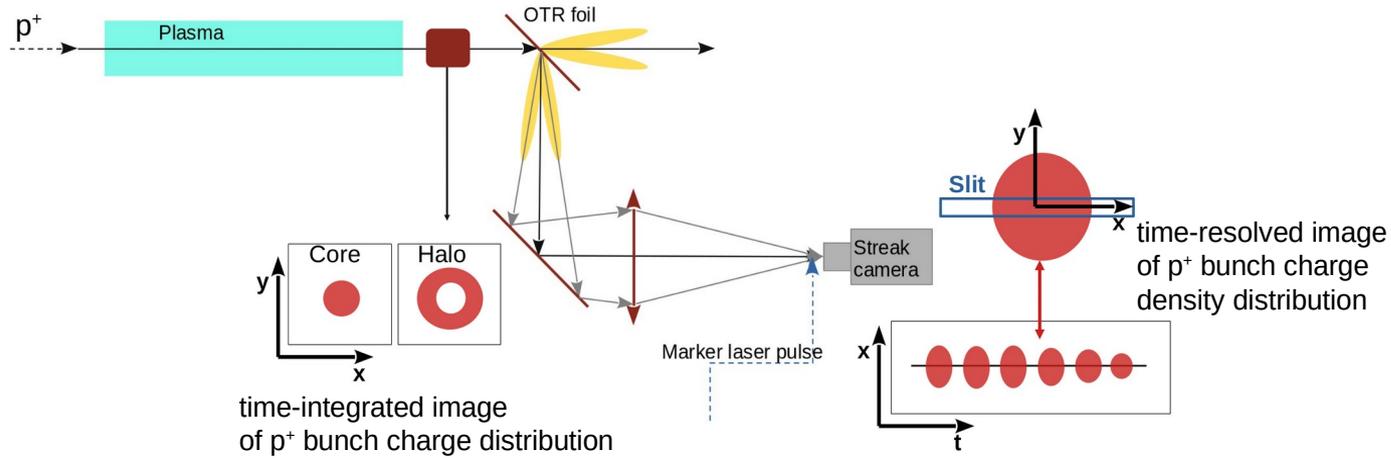
Hosing induced by electron bunch



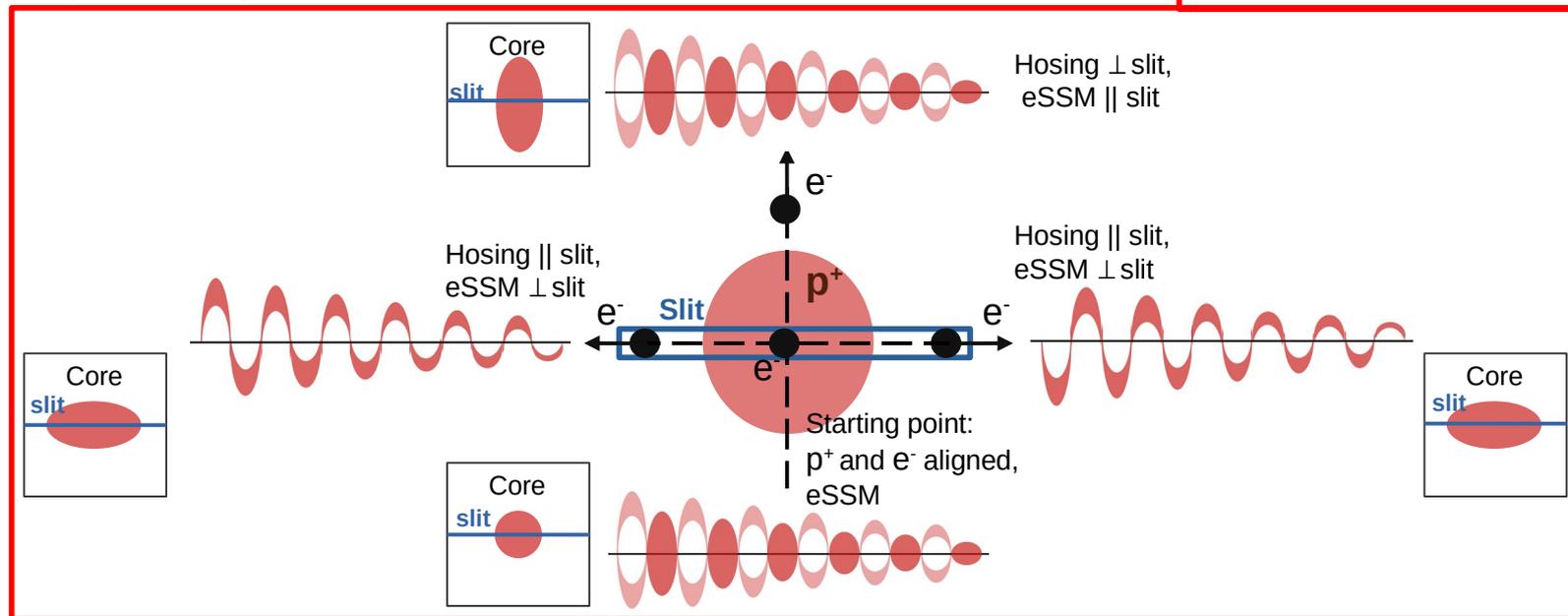
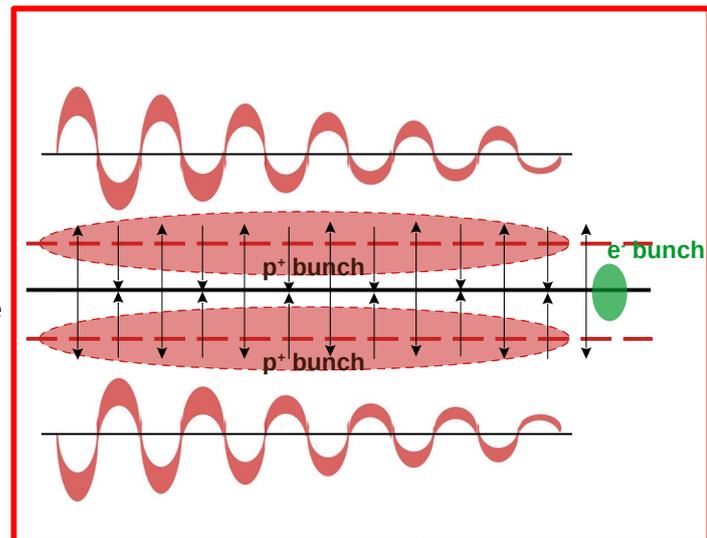
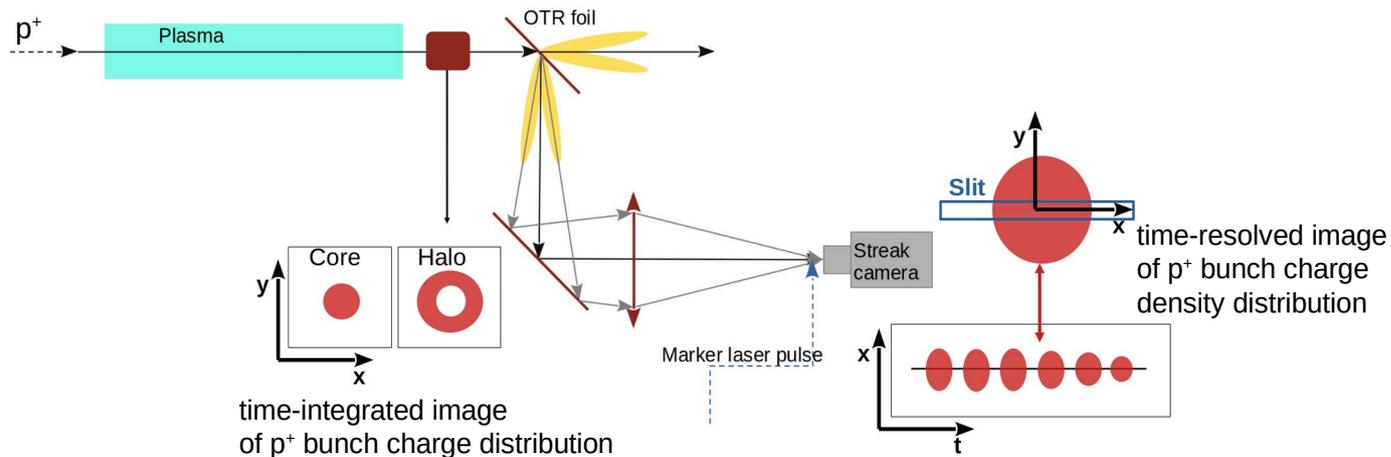
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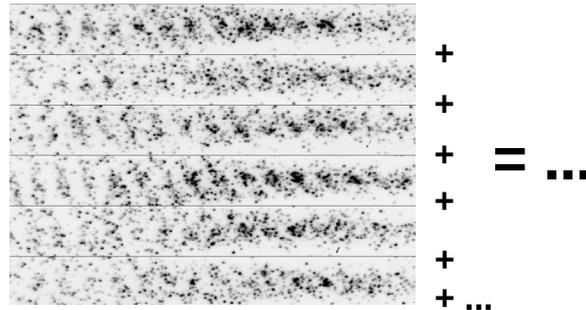
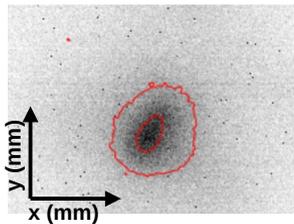
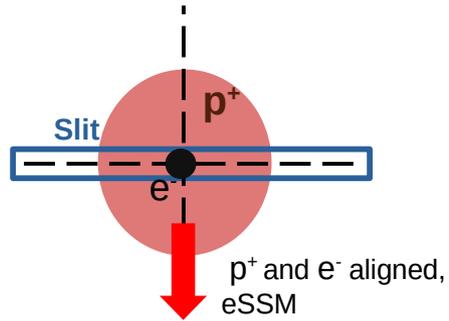
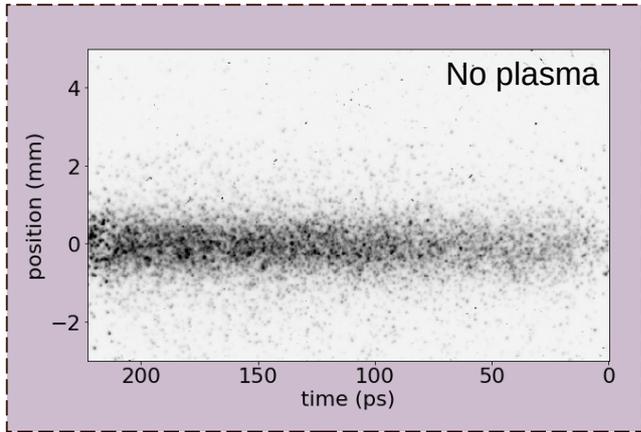


Hosing induced by electron bunch



Results

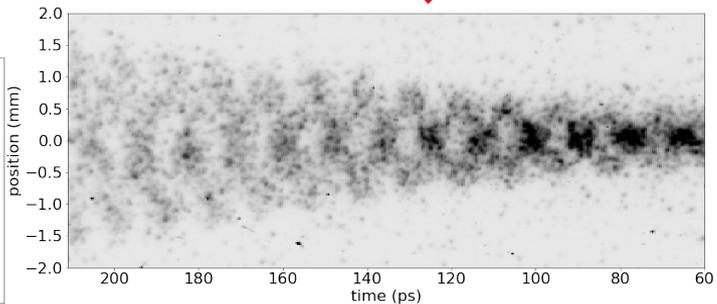
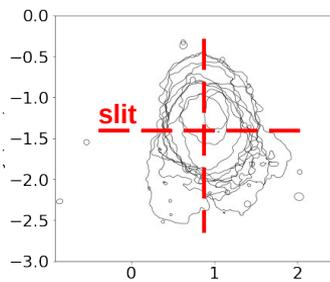
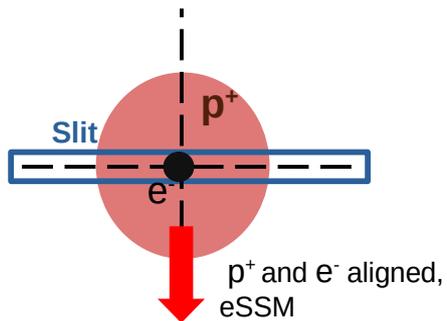
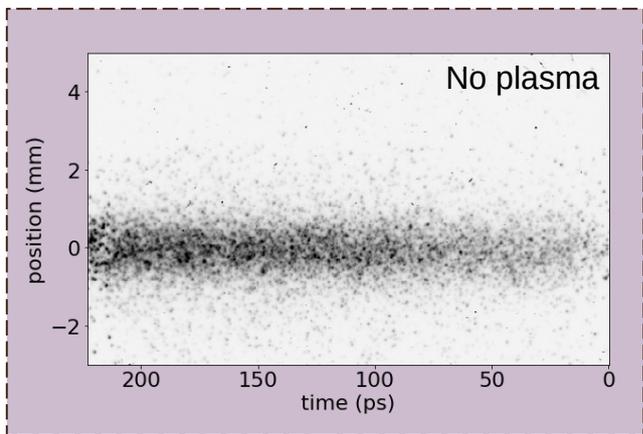
preliminary



Results

preliminary

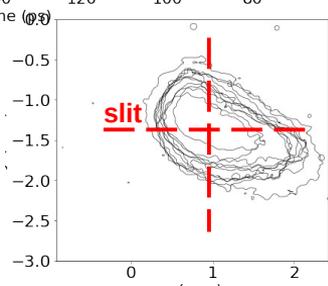
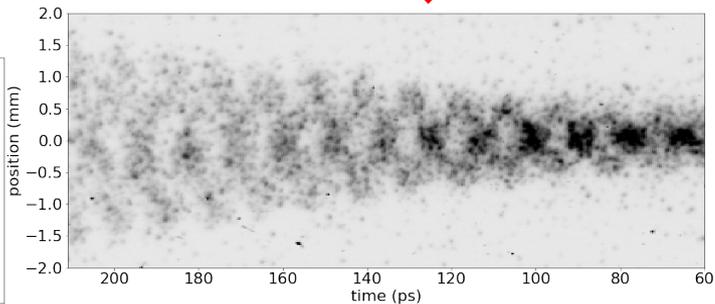
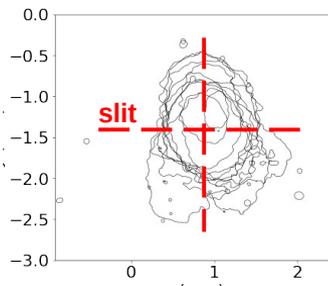
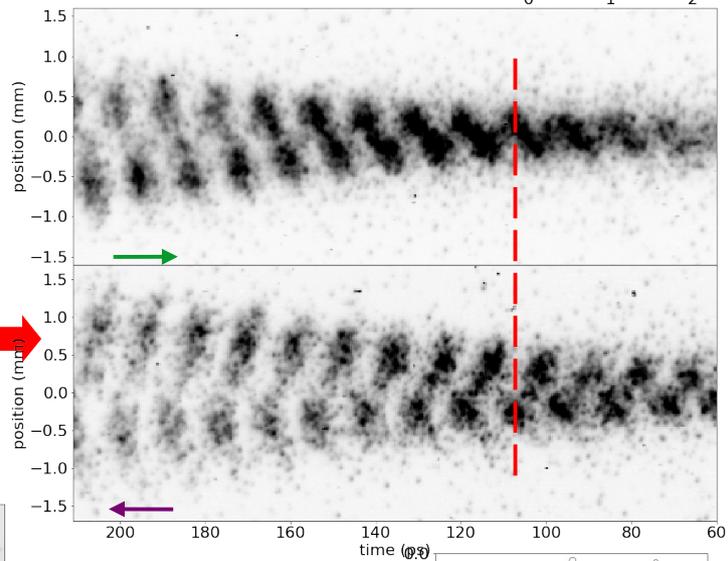
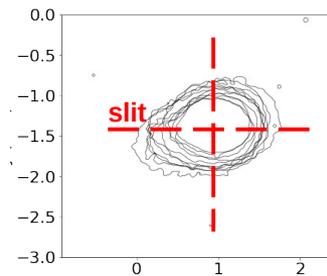
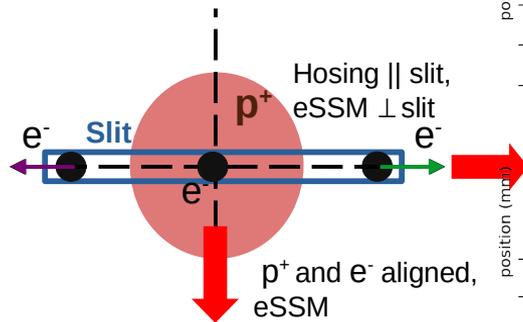
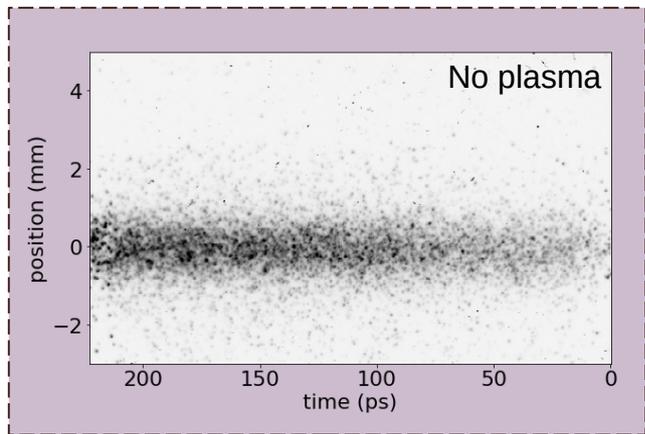
Images – averages of ~10 events



Results

preliminary

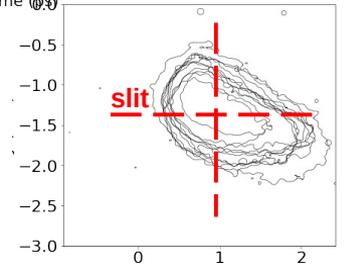
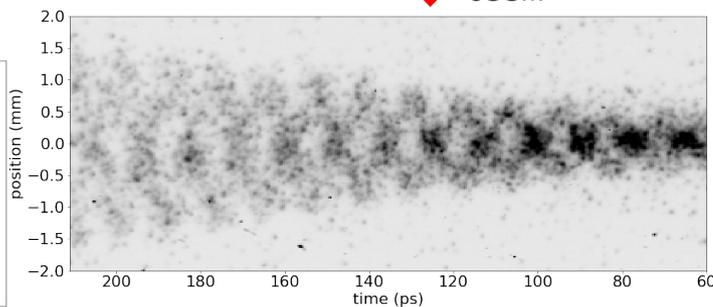
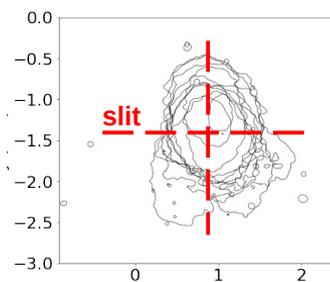
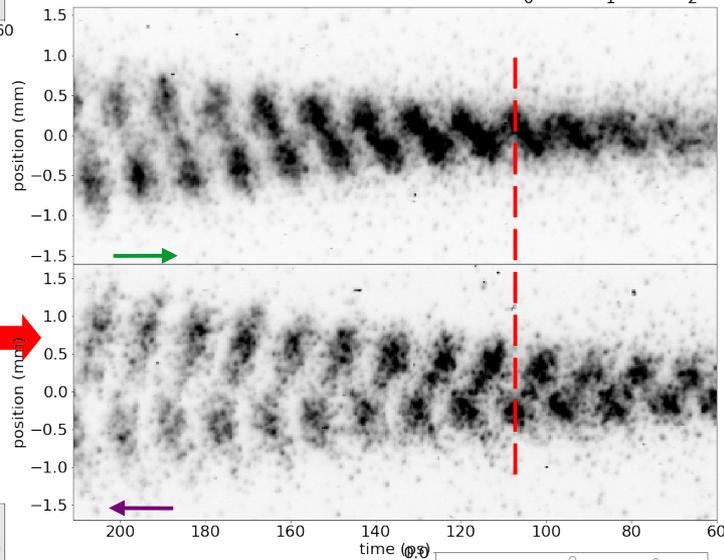
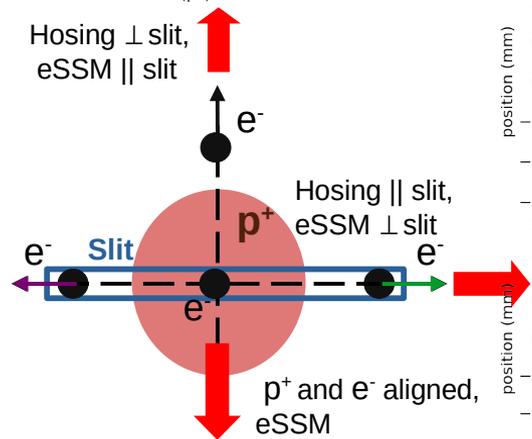
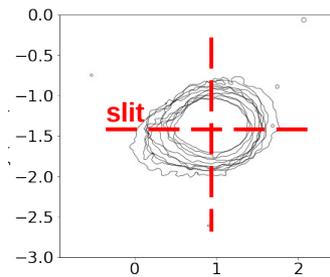
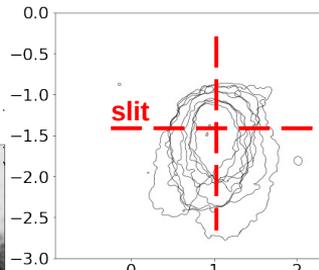
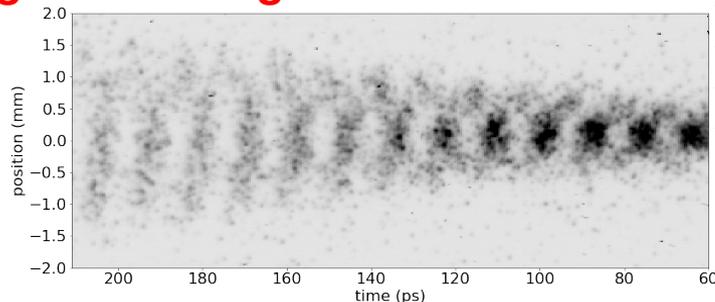
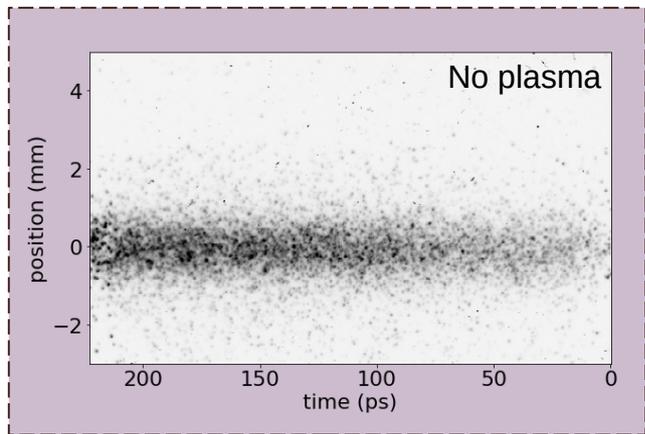
Images – averages of ~10 events



Results

preliminary

Images – averages of ~10 events



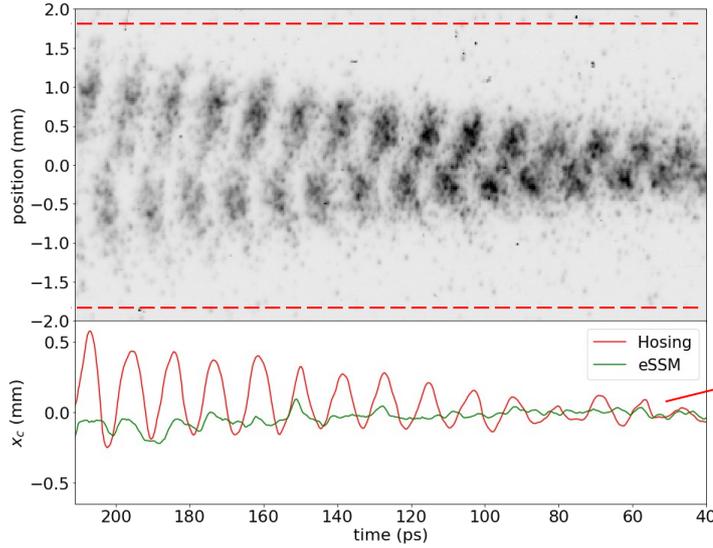
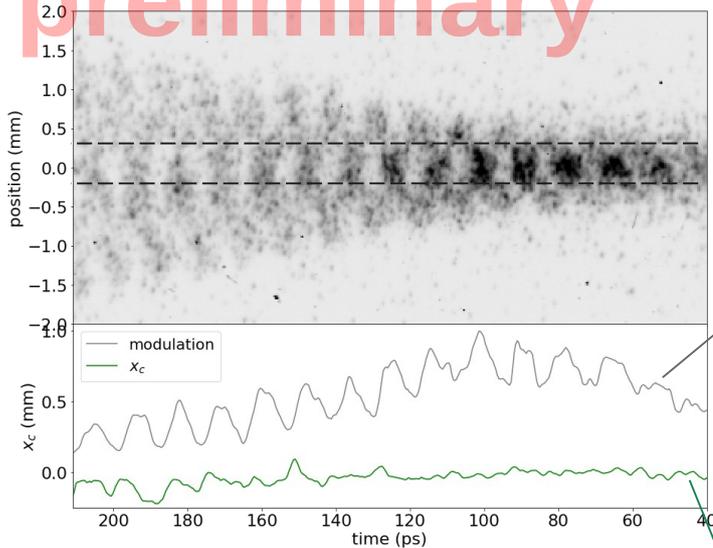
Frequency analysis

preliminary

Plasma e⁻ frequency

$$f_{pe} = \frac{1}{2\pi} \sqrt{\frac{n_{pe} e^2}{\epsilon_0 m_e}}$$

$$n_{pe} \sim 0.96 \cdot 10^{14} \text{ cm}^{-3}$$



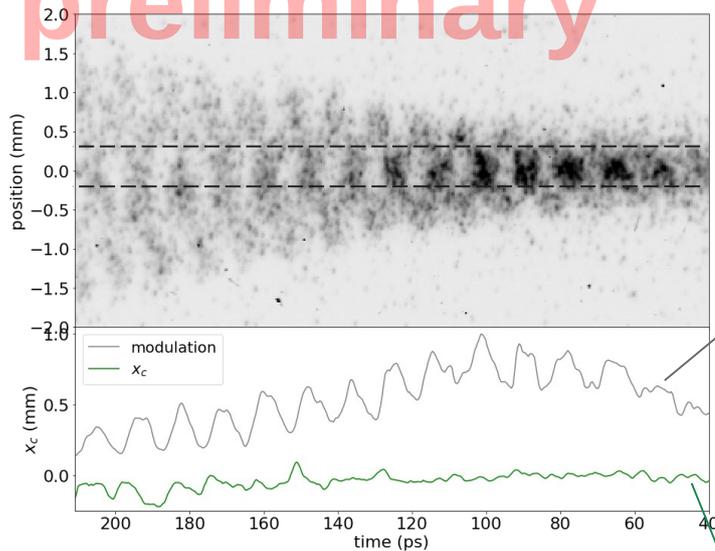
Frequency analysis

preliminary

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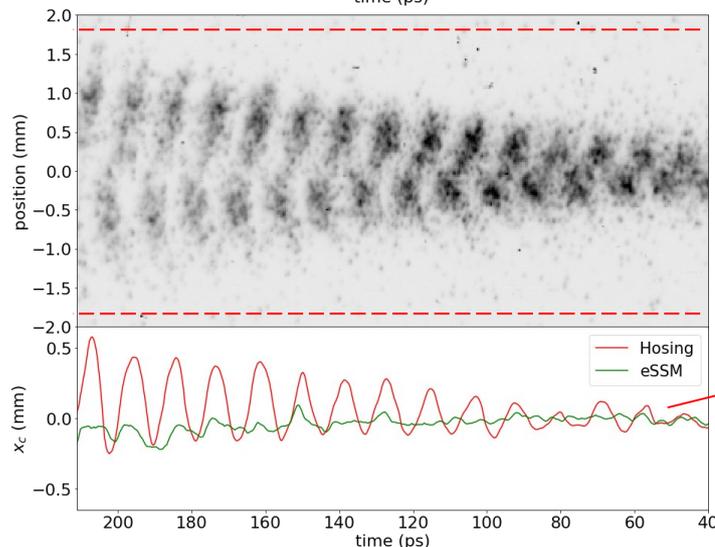
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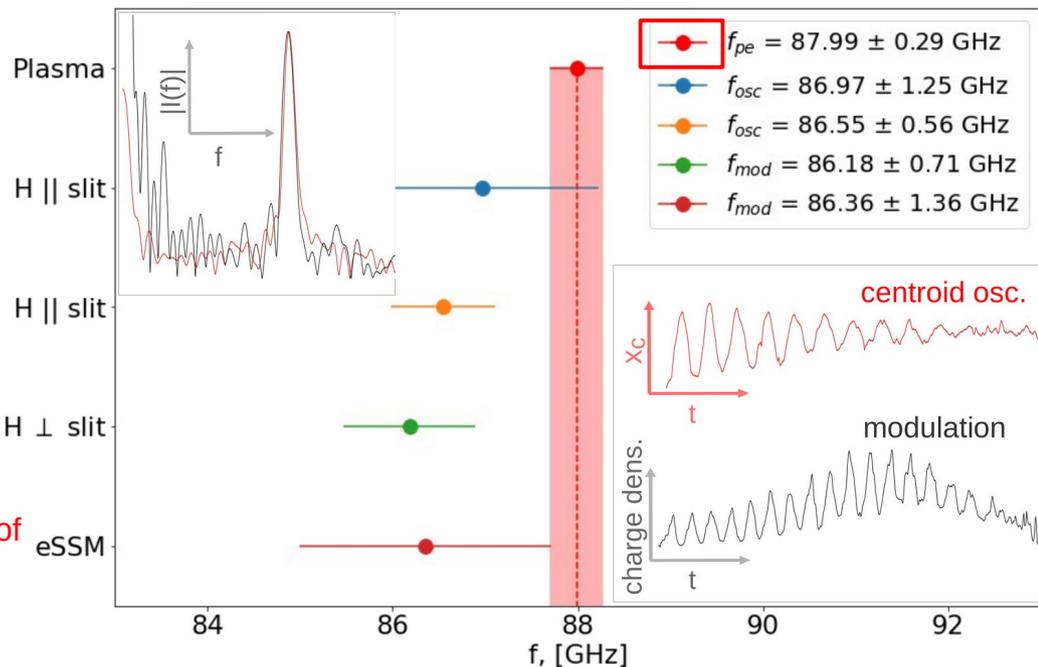


Summed charge density in the bunch core

DFT



Center of mass of each transverse bunch slice



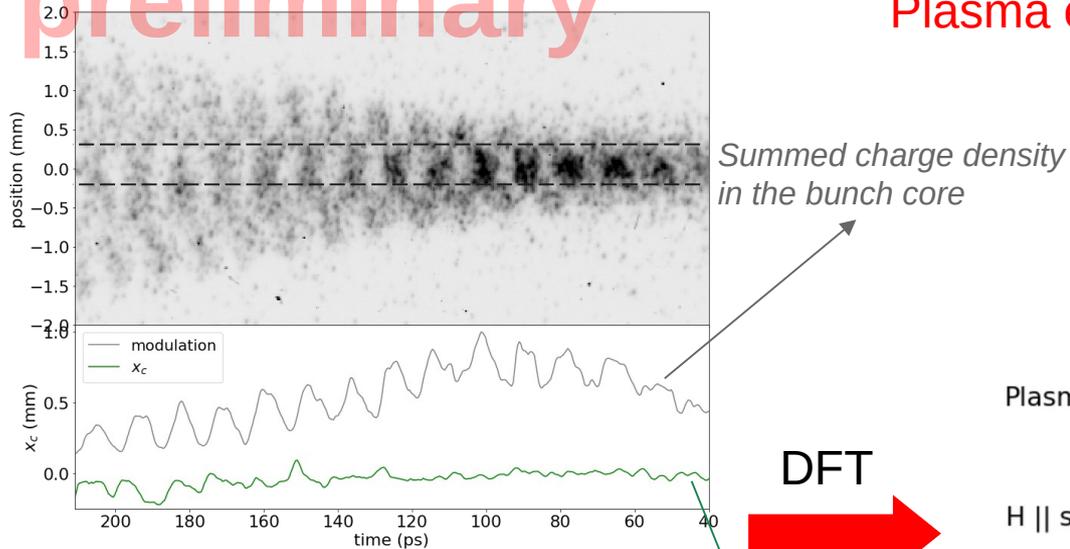
Frequency analysis

preliminary

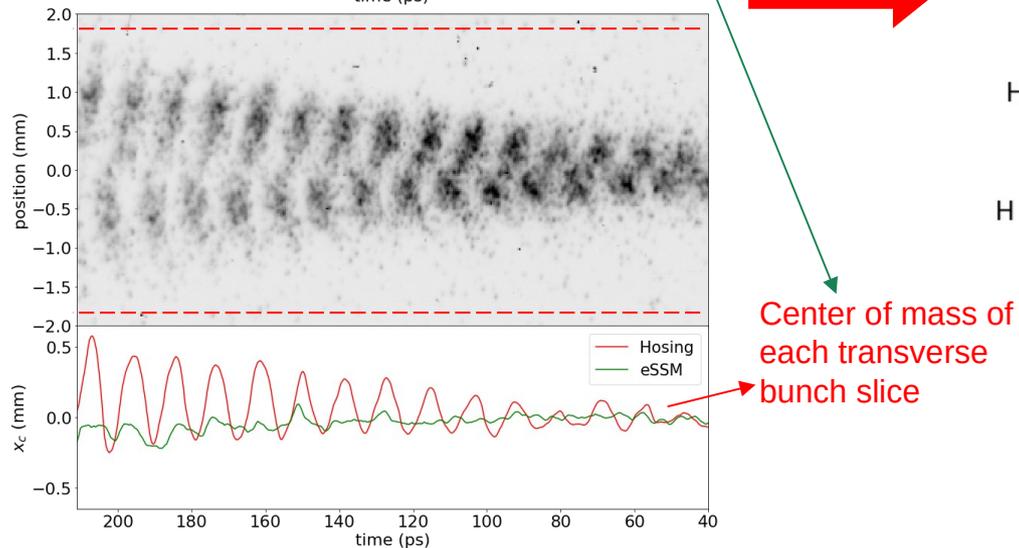
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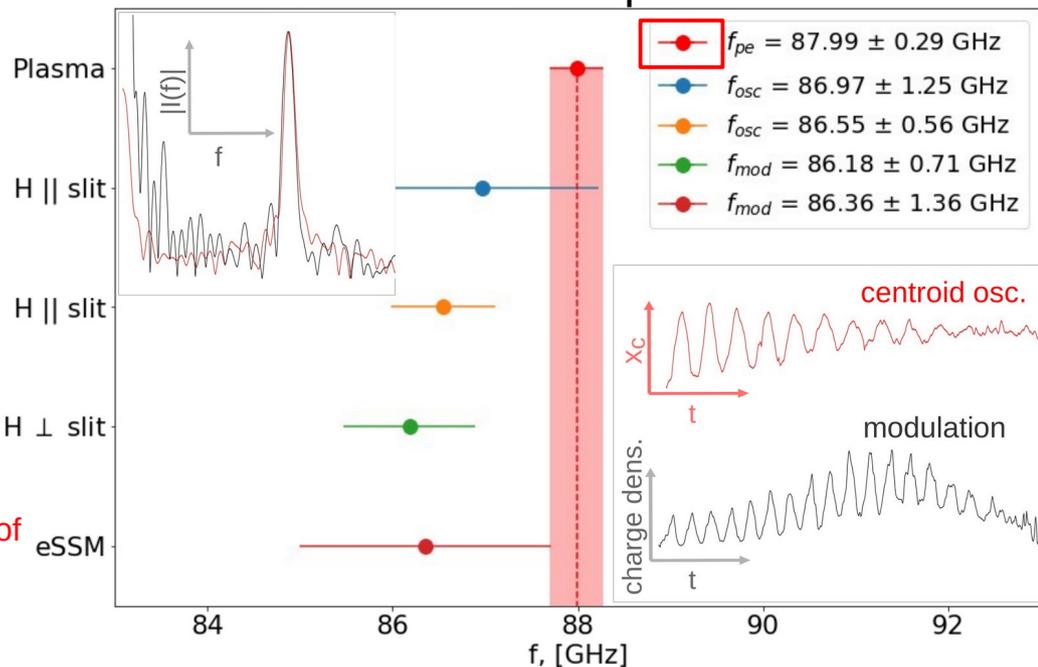
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DFT



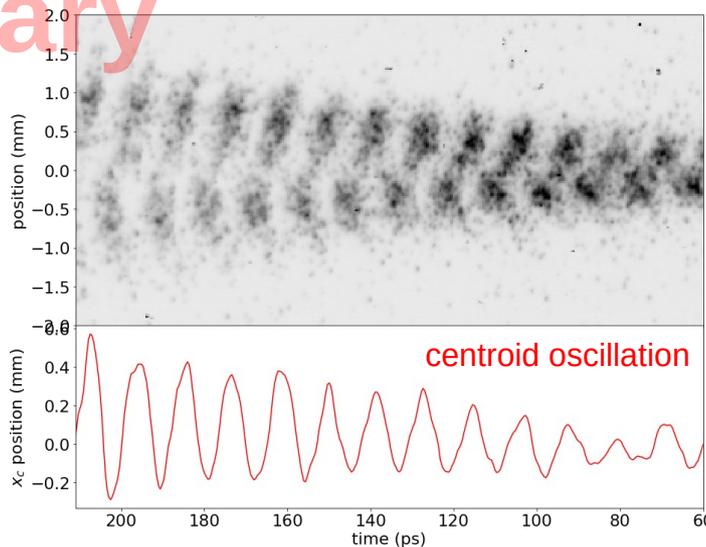
$$f_H \approx f_{SM} \approx f_{pe}$$



Frequency analysis

preliminary

$n_{pe} \sim 0.96 \cdot 10^{14} \text{ cm}^{-3}$
 $f_{pe} \sim 87.9 \text{ GHz}$



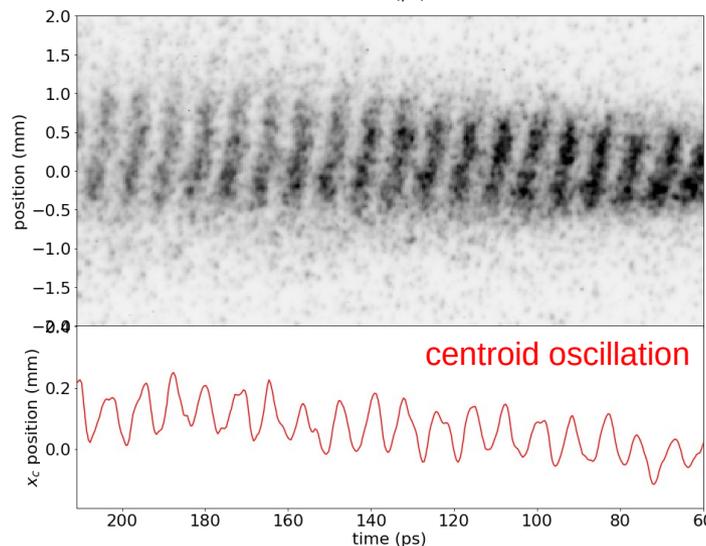
Plasma e⁻ frequency

$$f_{pe} = \frac{1}{2\pi} \sqrt{\frac{n_{pe} e^2}{\epsilon_0 m_e}}$$

→ $f_H = 86.97 \text{ GHz}$

$T_H \sim 11.4 \text{ ps}$

$n_{pe} \sim 2.03 \cdot 10^{14} \text{ cm}^{-3}$
 $f_{pe} \sim 127.8 \text{ GHz}$



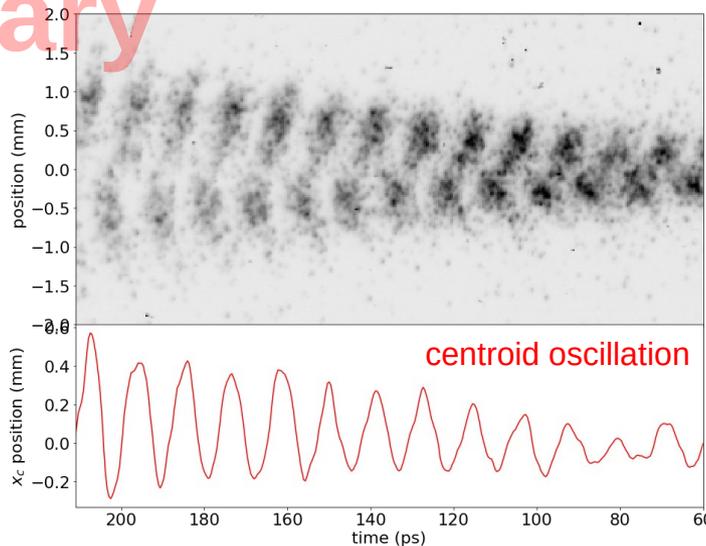
→ $f_H = 123.5 \text{ GHz}$

$T_H \sim 8 \text{ ps}$

Frequency analysis

preliminary

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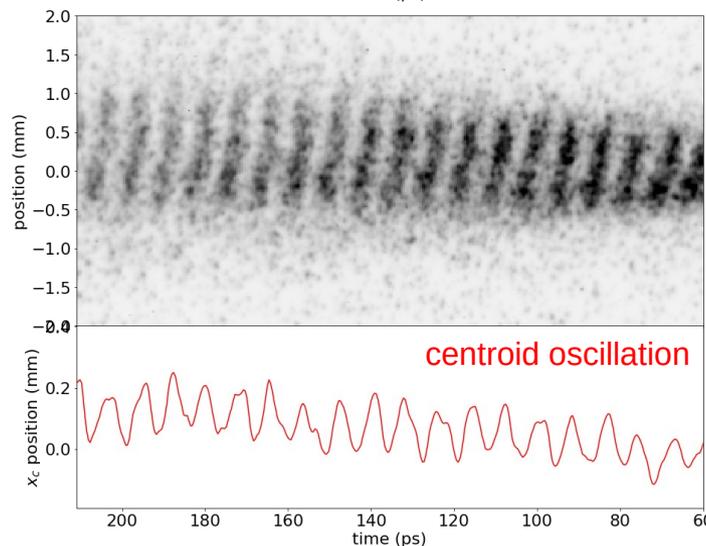
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→ $f_H = 123.5 \text{ GHz}$

$T_H \sim 8 \text{ ps}$

- n_{pe} increases $\Rightarrow f_{pe}$ increases \Rightarrow
- $f_{H, SM}$ increases
- $f_{H, SM} \approx f_{pe}$

Amplitude of oscillations vs p+ bunch charge

$$x_c = \delta_c \frac{e^{N_h}}{N_h^{1/2}} \frac{3^{1/4}}{(8\pi)^{1/2}} \cos(\pi/12 - k_p \xi - N_h/\sqrt{3}) \quad *$$

δ_c = f(e⁻ parameters) – initial amplitude

N_h = f(p⁺ parameters) – growth rate

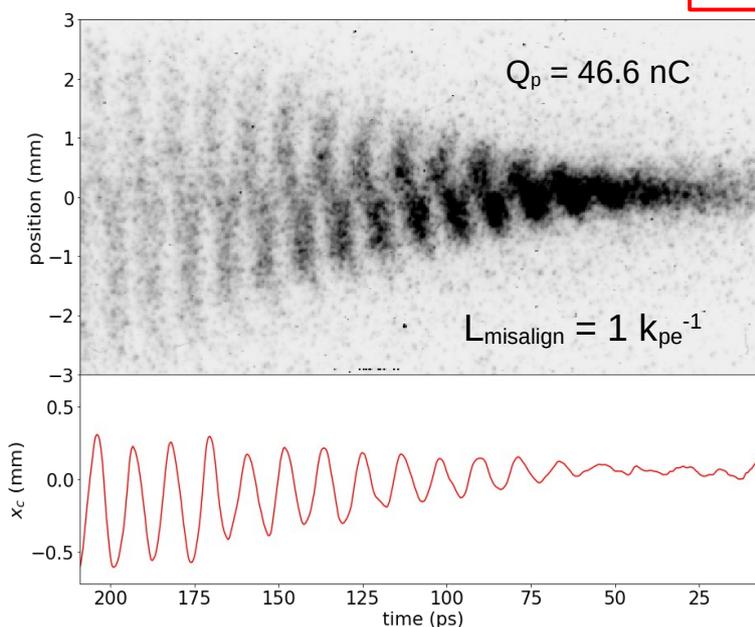
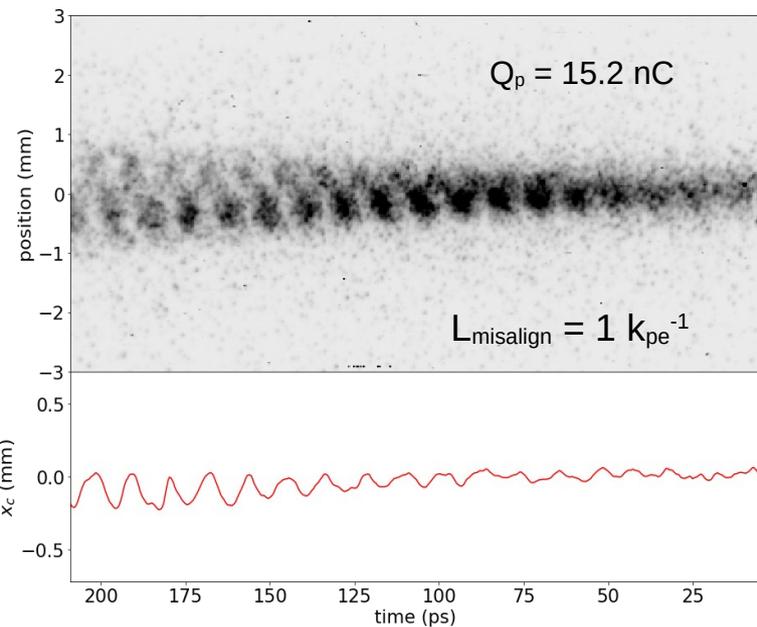
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preliminary

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- **Linear theory:**

- $N_h = f(n_b)$

- $n_p = f(Q_p)$:
 Q_p increases $\rightarrow n_p$ increases

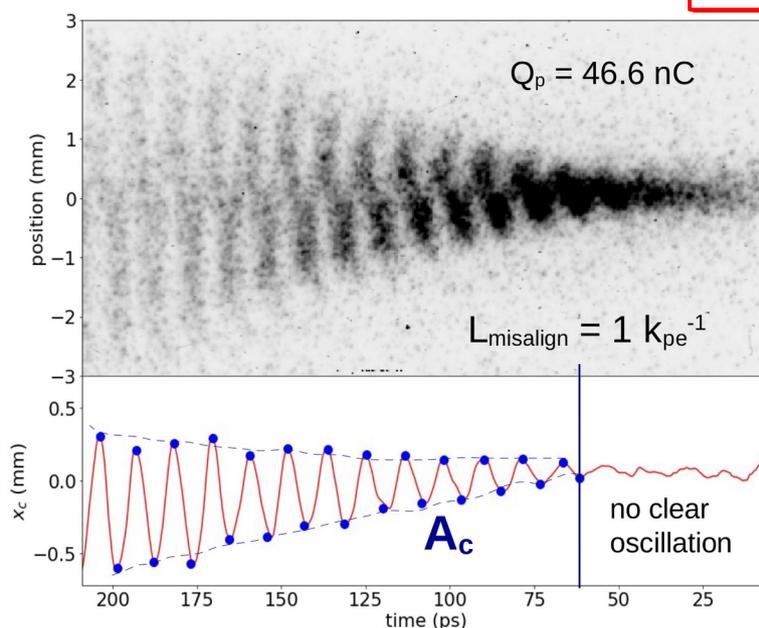
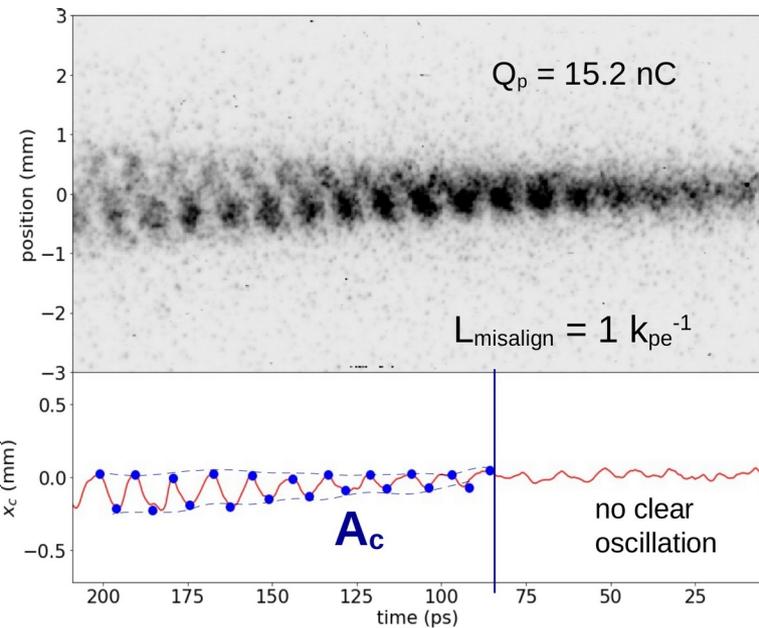
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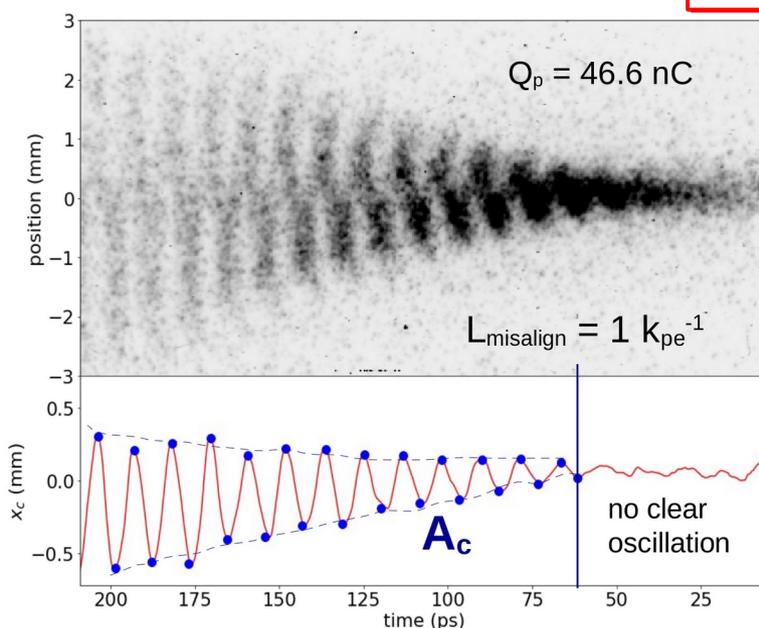
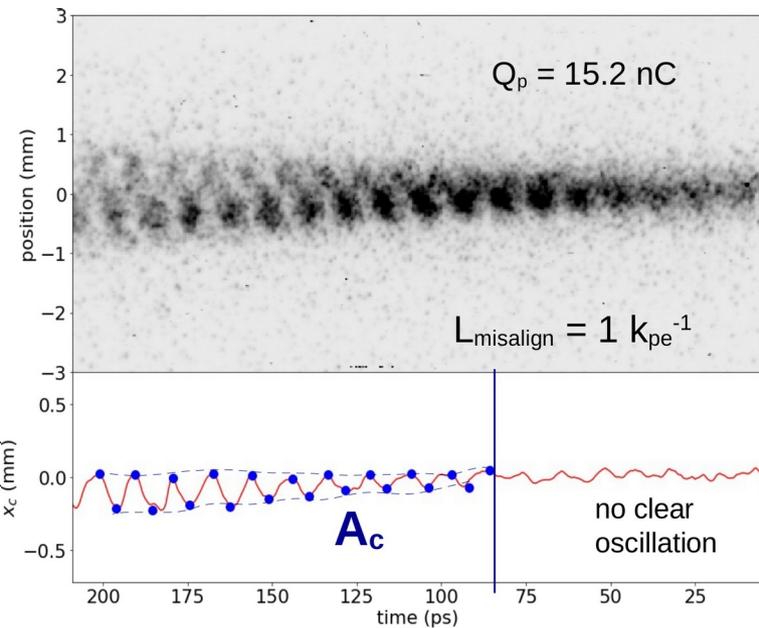
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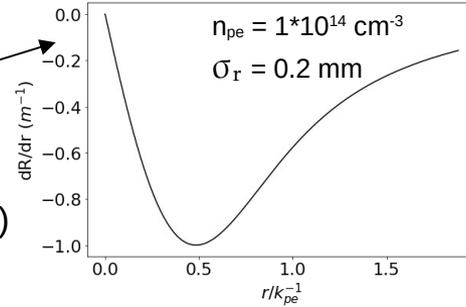
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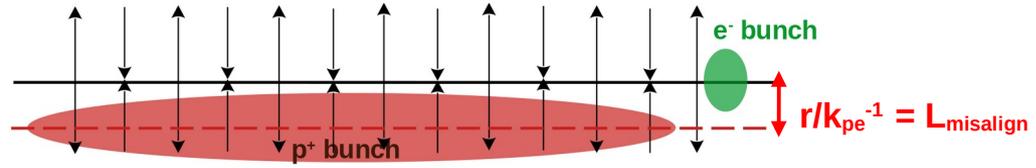
Amplitude of oscillations vs misalignment extent



$$x_c = \delta_c \frac{e^{N_h}}{N_h^{1/2}} \frac{3^{1/4}}{(8\pi)^{1/2}} \cos(\pi/12 - k_p \xi - N_h/\sqrt{3})^*$$

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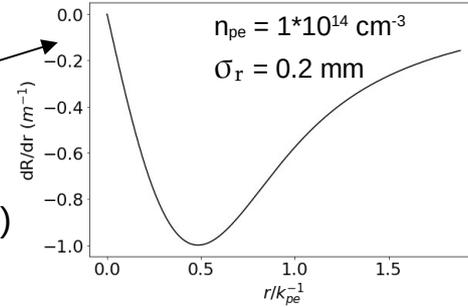
- **Linear theory:** $W_r \rightarrow W_{\perp, \text{seed}}$ depends on r as
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* C. Schroeder, *Phys. Rev. E* **86**, 026402 (2012)

Amplitude of oscillations vs misalignment extent

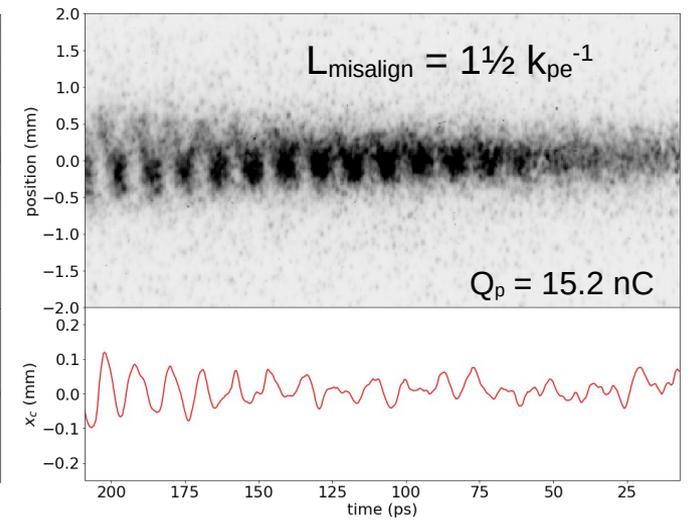
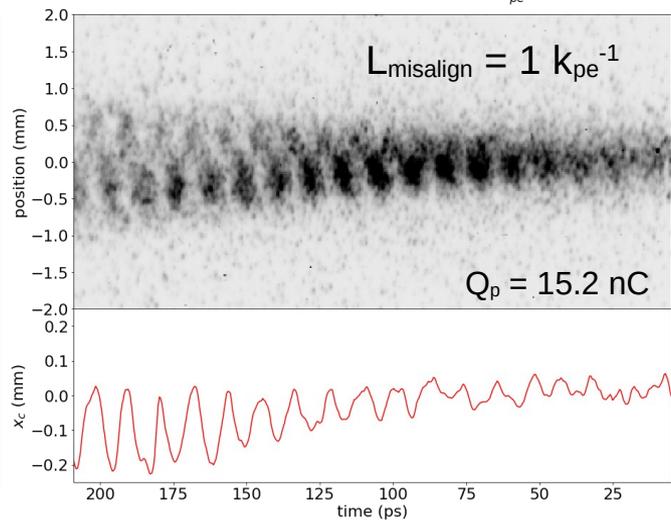
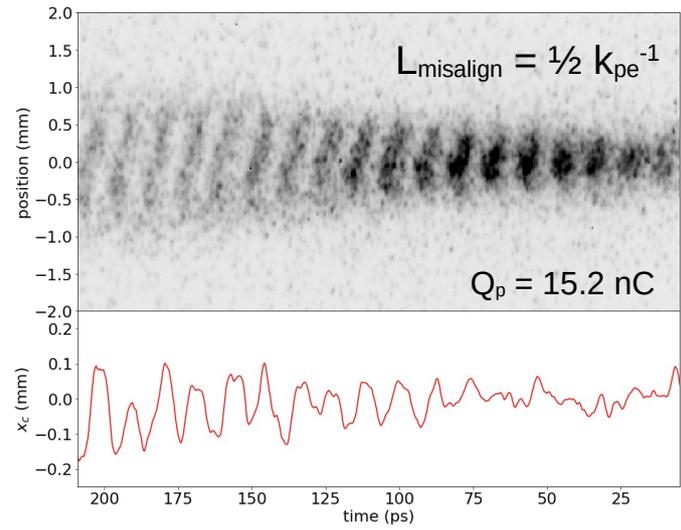
preliminary



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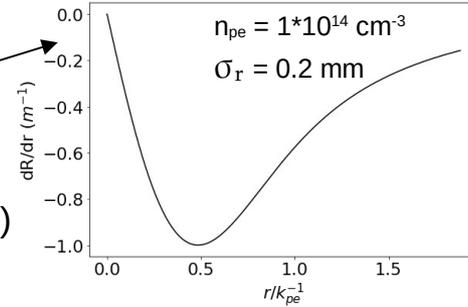
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Amplitude of oscillations vs misalignment extent

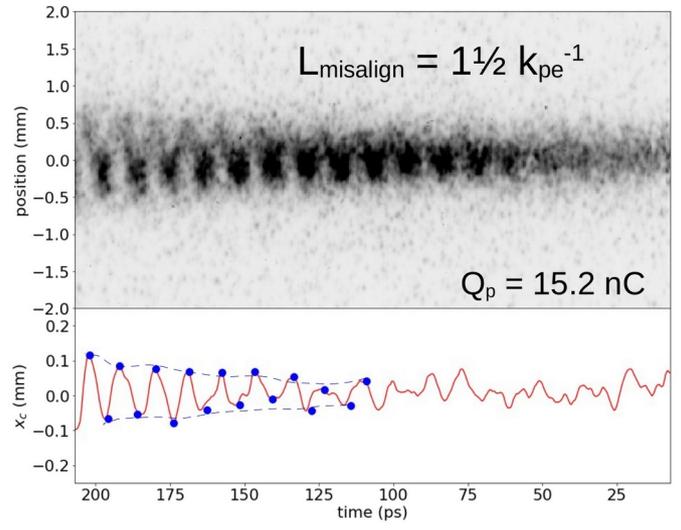
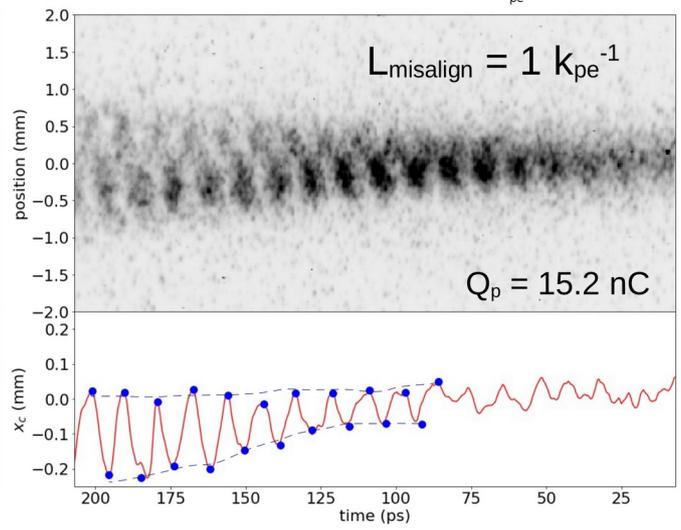
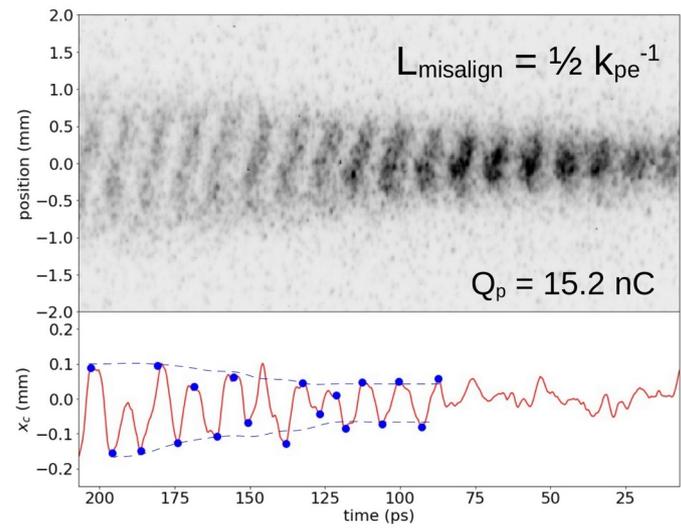
preliminary



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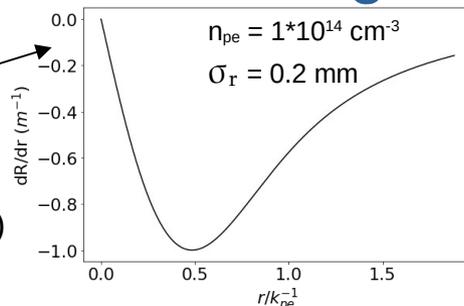


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Amplitude of oscillations vs misalignment extent

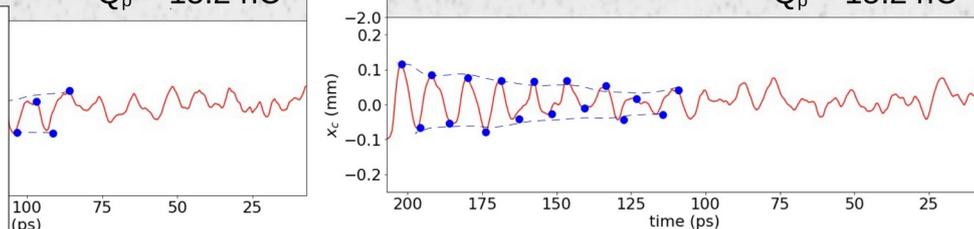
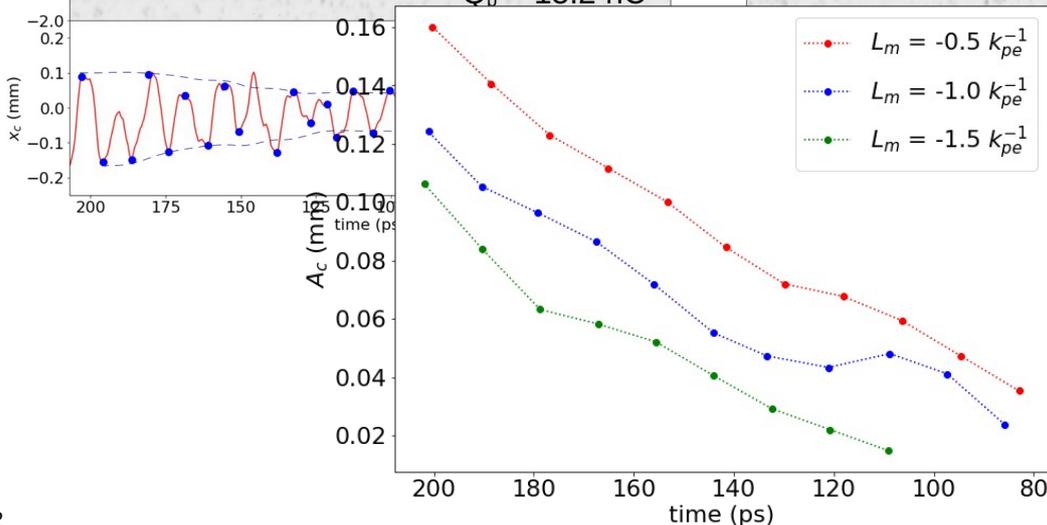
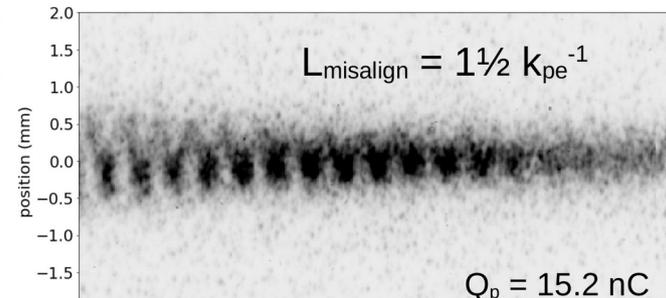
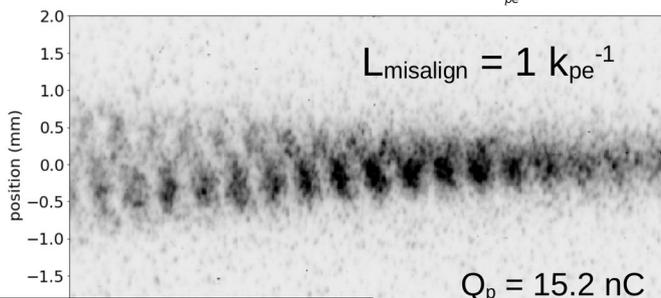
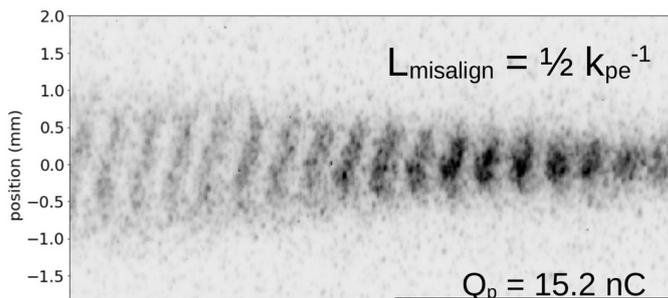
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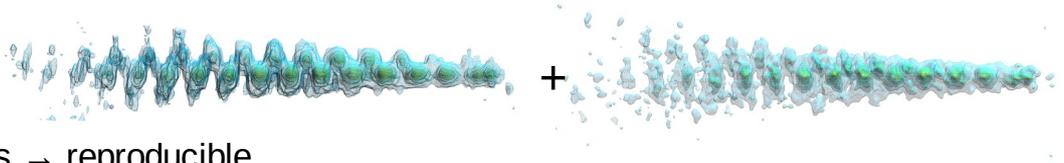


L_{misalign} increases $\rightarrow A_c$ decreases

* C. Schroeder, *Phys. Rev. E* **86**, 026402 (2012)

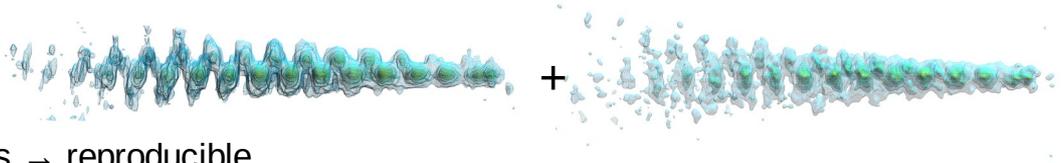
Conclusion and outlook

- Understanding hosing is important for PWFA (LWFA)
- Hosing @ AWAKE: can occur in the 1st stage → might grow further in the 2nd stage →
- Study hosing → know how to suppress it
- **Preliminary study of hosing:**
 - Induced by e⁻ bunch (wakefields) misalignment
 - At f_{pe}
 - Occurs at the same time as eSSM (in \perp planes)
 - Hosing and eSSM caused by the same wakefields → reproducible
 - Direction reverses with direction of misalignment
 - Observed growth along the bunch
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 - Depends on the L_{misalign}



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Thank you for your attention!