

# Automatic Generation of the Lagrangian Beyond SM (BETA Version !!!)

***Neil Christensen***, Stefanus, Daniel Salmon,  
Christian Speckner, Nicholas Setzer

PITT Particle Astronomy and Cosmology Center (PITT PACC)  
University of Pittsburgh

# !! Disclaimer !!

ἐν οἶδα ὅτι οὐδὲν οἶδα *hèn oîda hótì oudèn oîda*  
- Σωκράτης

**“The only thing that I know is that I don’t know  
anything”**

- Socrates

# Outline

- It's FREE. Doesn't depend on Mathematica !!!
- Algebra Package (Tested)
- Compact Lie Algebra Package (Tested)
- Zn (Discrete Group) Package (Tested)
- Model package (Tested ?!??!?)
- GUI (In progress ...)
- Package Mentality (everything's library based)
- Automated Comprehensive Testing !!!
- Future Work
- Live Demo 😊 😊 😊 (Sneak Preview)

# Algebra Package

- Fraction (no rounding error of floating points)
  - Numerator, Root and Denominator
- Fraction Sum
- Fraction Sum Vector
- Fraction Sum Matrix
- Automated Testing for all fraction operations

# Compact Lie Algebra

- All Reps implemented(as long as enough memory) of Compact Lie Algebra
- Exact Reps, no rounding error using Fraction Sum class !!!
- Generator Matrices
- Singlet generation of product of Reps
- Automated Testing

# $Z_n$ (Discrete Group)

- Defining reps only for now and only  $Z_n$
- Automated Testing

# Model Package

- Gauge groups (local and global)
- Discrete group (now only  $Z_n$ )
- CompField class (container class including SUSY)
- Interaction class (container for Lagrangian terms)
- Automated Lagrangian generation
- Automated Testing ??!!?!??
  - MSSM
  - SM 1 and 2 Higgs (up to Dim 6) and QED

# QED

QED

$$\bar{\Psi}_L \gamma^\mu D_\mu \Psi_L + \bar{\Psi}_R \gamma^\mu D_\mu \Psi_R + F_{\mu\nu} F^{\mu\nu}$$

$$m_0 \bar{\Psi}_R \Psi_L + m_0^* \bar{\Psi}_L \Psi_R$$



# MSSM

MSSM up to Dimension 4

$$\begin{aligned}
 & \int d^2\theta d^2\bar{\theta} \Phi_q^\dagger \exp[g_0 G_C + g_1 W_L + g_2 B_Y] \Phi_q + \int d^2\theta d^2\bar{\theta} \Phi_u^\dagger \exp[g_0 G_C + g_2 B_Y] \Phi_u + \int d^2\theta d^2\bar{\theta} \\
 & \Phi_d^\dagger \exp[g_0 G_C + g_2 B_Y] \Phi_d + \int d^2\theta d^2\bar{\theta} \Phi_l^\dagger \exp[g_1 W_L + g_2 B_Y] \Phi_l + \int d^2\theta d^2\bar{\theta} \Phi_e^\dagger \exp[g_2 B_Y] \Phi_e + \int d^2\theta d^2\bar{\theta} \\
 & \Phi_{H1}^\dagger \exp[g_1 W_L + g_2 B_Y] \Phi_{H1} + \int d^2\theta d^2\bar{\theta} \Phi_{H2}^\dagger \exp[g_1 W_L + g_2 B_Y] \Phi_{H2} + \int d^2\theta G_C G_C + \int d^2\bar{\theta} G_C^\dagger G_C^\dagger + \\
 & \int d^2\theta W_L W_L + \int d^2\bar{\theta} W_L^\dagger W_L^\dagger + \int d^2\theta B_Y B_Y + \int d^2\bar{\theta} B_Y^\dagger B_Y^\dagger \\
 & \mu_0 \int d^2\theta \Phi_{H2} \Phi_{H1} + \mu_0^* \int d^2\bar{\theta} \Phi_{H1}^\dagger \Phi_{H2}^\dagger \\
 & y_1 \int d^2\theta \Phi_{H2} \Phi_u \Phi_q + y_1^* \int d^2\bar{\theta} \Phi_q^\dagger \Phi_u^\dagger \Phi_{H2}^\dagger + y_2 \int d^2\theta \Phi_{H1} \Phi_d \Phi_q + y_2^* \int d^2\bar{\theta} \Phi_q^\dagger \Phi_d^\dagger \Phi_{H1}^\dagger + y_3 \int d^2\theta \Phi_{H1} \Phi_e \Phi_l \\
 & + y_3^* \int d^2\bar{\theta} \Phi_l^\dagger \Phi_e^\dagger \Phi_{H1}^\dagger
 \end{aligned}$$

# SM 1 Higgs (Dim 4)

SM with 1 Higgs up to Dimension 4

$$\begin{aligned} & \overline{Q}_l \gamma^\mu D_\mu Q_l + \overline{U}_r \gamma^\mu D_\mu U_r + \overline{D}_r \gamma^\mu D_\mu D_r + \overline{L}_l \gamma^\mu D_\mu L_l + \overline{E}_r \gamma^\mu D_\mu E_r + D_\mu \Phi^* D^\mu \Phi + G_{C\mu\nu} G_C^{\mu\nu} + \theta_0 \epsilon_{\alpha\beta\gamma\delta} G_C^{\alpha\beta} G_C^{\gamma\delta} \\ & + W_{L\mu\nu} W_L^{\mu\nu} + \theta_1 \epsilon_{\alpha\beta\gamma\delta} W_L^{\alpha\beta} W_L^{\gamma\delta} + B_{Y\mu\nu} B_Y^{\mu\nu} \end{aligned}$$

$$\mu_{r0} \Phi \Phi^*$$

$$\lambda_{r1} \Phi \Phi \Phi^* \Phi^*$$

$$y_2 \Phi \overline{U}_r Q_l + y_2^* \Phi^* \overline{Q}_l U_r + y_3 \Phi^* \overline{D}_r Q_l + y_3^* \Phi \overline{Q}_l D_r + y_4 \Phi^* \overline{E}_r L_l + y_4^* \Phi \overline{L}_l E_r$$

# SM 1 Higgs (Dim 6)

$$\overline{Q}_l \gamma^\mu D_\mu Q_l + \overline{U}_r \gamma^\mu D_\mu U_r + \overline{D}_r \gamma^\mu D_\mu D_r + \overline{L}_l \gamma^\mu D_\mu L_l + \overline{E}_r \gamma^\mu D_\mu E_r + D_\mu \Phi^* D^\mu \Phi + G_{C\mu\nu} G_C^{\mu\nu} + \theta_0 \varepsilon_{\alpha\beta\gamma\delta} G_C^{\alpha\beta} G_C^{\gamma\delta} + W_{L\mu\nu} W_L^{\mu\nu} + \theta_1 \varepsilon_{\alpha\beta\gamma\delta} W_L^{\alpha\beta} W_L^{\gamma\delta} + B_{Y\mu\nu} B_Y^{\mu\nu}$$

$$\mu_{r0} \Phi \Phi^*$$

$$\lambda_{r1} \Phi \Phi \Phi^* \Phi^*$$

$$y_2 \Phi \overline{U}_r Q_l + y_2^* \Phi^* \overline{Q}_l U_r + y_3 \Phi^* \overline{D}_r Q_l + y_3^* \Phi \overline{Q}_l D_r + y_4 \Phi^* \overline{E}_r L_l + y_4^* \Phi \overline{L}_l E_r +$$

$$y_5 \Phi \Phi \overline{L}_l L_l^c + y_5^* \Phi^* \Phi^* \overline{L}_l^c L_l +$$

$$y_6 \Phi^* \Phi \Phi \overline{U}_r Q_l + y_6^* \Phi \Phi^* \Phi^* \overline{Q}_l U_r + y_7 \Phi^* \Phi^* \Phi \overline{D}_r Q_l + y_7^* \Phi \Phi \Phi^* \overline{Q}_l D_r + y_8 \Phi^* \Phi^* \Phi \overline{E}_r L_l + y_8^* \Phi \Phi \Phi^* \overline{L}_l E_r$$

$$\begin{aligned}
& g_{r9} \bar{Q}_l \gamma_\mu Q_l \bar{Q}_l \gamma^\mu Q_l + g_{r10} \bar{Q}_l^c \sigma_{\mu\nu} Q_l \bar{Q}_l \sigma^{\mu\nu} Q_l^c + g_{r11} \bar{Q}_l^c Q_l \bar{Q}_l Q_l^c + g_{r12} \bar{Q}_l \gamma_\mu Q_l \bar{U}_r \gamma^\mu U_r + g_{r13} \bar{Q}_l^c \gamma_\mu U_r \bar{U}_r \gamma^\mu Q_l^c + g_{r14} \bar{Q}_l \sigma_{\mu\nu} U_r \bar{U}_r \\
& \sigma^{\mu\nu} Q_l + g_{r15} \bar{Q}_l U_r \bar{U}_r Q_l + g_{r16} \bar{Q}_l \gamma_\mu Q_l \bar{D}_r \gamma^\mu D_r + g_{r17} \bar{Q}_l^c \gamma_\mu D_r \bar{D}_r \gamma^\mu Q_l^c + g_{r18} \bar{Q}_l \sigma_{\mu\nu} D_r \bar{D}_r \sigma^{\mu\nu} Q_l + g_{r19} \bar{Q}_l D_r \bar{D}_r Q_l + g_{r20} \bar{Q}_l \gamma_\mu L_l \\
& \bar{L}_l \gamma^\mu Q_l + g_{r21} \bar{Q}_l \gamma_\mu Q_l \bar{L}_l \gamma^\mu L_l + g_{r22} \bar{Q}_l^c \sigma_{\mu\nu} L_l \bar{L}_l \sigma^{\mu\nu} Q_l^c + g_{r23} \bar{Q}_l^c L_l \bar{L}_l Q_l^c + g_{r24} \bar{Q}_l \gamma_\mu Q_l \bar{E}_r \gamma^\mu E_r + g_{r25} \bar{Q}_l^c \gamma_\mu E_r \bar{E}_r \gamma^\mu Q_l^c + g_{r26} \bar{Q}_l \\
& \sigma_{\mu\nu} E_r \bar{E}_r \sigma^{\mu\nu} Q_l + g_{r27} \bar{Q}_l E_r \bar{E}_r Q_l + g_{r28} \bar{Q}_l \sigma_{\mu\nu} Q_l^c \bar{L}_l \sigma^{\mu\nu} Q_l^c + g_{r28}^* \bar{Q}_l^c \sigma_{\mu\nu} Q_l \bar{Q}_l^c \sigma^{\mu\nu} L_l + g_{r29} \bar{Q}_l Q_l^c \bar{L}_l Q_l^c + g_{r29}^* \bar{Q}_l^c Q_l \bar{Q}_l^c L_l + g_{r30} \bar{D}_r \\
& \sigma_{\mu\nu} Q_l \bar{U}_r \sigma^{\mu\nu} Q_l + g_{r30}^* \bar{Q}_l \sigma_{\mu\nu} D_r \bar{Q}_l \sigma^{\mu\nu} U_r + g_{r31} \bar{D}_r Q_l \bar{U}_r Q_l + g_{r31}^* \bar{Q}_l D_r \bar{Q}_l U_r + g_{r32} \bar{U}_r \sigma_{\mu\nu} Q_l \bar{D}_r \sigma^{\mu\nu} Q_l + g_{r32}^* \bar{Q}_l \sigma_{\mu\nu} U_r \bar{Q}_l \sigma^{\mu\nu} D_r + \\
& g_{r33} \bar{U}_r Q_l \bar{D}_r Q_l + g_{r33}^* \bar{Q}_l U_r \bar{Q}_l D_r + g_{r34} \bar{Q}_l \sigma_{\mu\nu} Q_l^c \bar{U}_r \sigma^{\mu\nu} D_r + g_{r34}^* \bar{Q}_l^c \sigma_{\mu\nu} Q_l \bar{D}_r \sigma^{\mu\nu} U_r^c + g_{r35} \bar{Q}_l Q_l^c \bar{U}_r^c D_r + g_{r35}^* \bar{Q}_l^c Q_l \bar{D}_r U_r^c + g_{r36} \bar{E}_r \\
& \gamma_\mu Q_l^c \bar{U}_r \gamma^\mu Q_l^c + g_{r36}^* \bar{Q}_l^c \gamma_\mu E_r \bar{Q}_l^c \gamma^\mu U_r + g_{r37} \bar{U}_r \gamma_\mu Q_l^c \bar{E}_r \gamma^\mu Q_l^c + g_{r37}^* \bar{Q}_l^c \gamma_\mu U_r \bar{Q}_l^c \gamma^\mu E_r + g_{r38} \bar{Q}_l \sigma_{\mu\nu} Q_l^c \bar{E}_r \sigma^{\mu\nu} U_r^c + g_{r38}^* \bar{Q}_l^c \sigma_{\mu\nu} Q_l \\
& \bar{U}_r^c \sigma^{\mu\nu} E_r + g_{r39} \bar{Q}_l Q_l^c \bar{E}_r U_r^c + g_{r39}^* \bar{Q}_l^c Q_l \bar{U}_r^c E_r + g_{r40} \bar{E}_r \sigma_{\mu\nu} Q_l \bar{U}_r \sigma^{\mu\nu} L_l + g_{r40}^* \bar{Q}_l \sigma_{\mu\nu} E_r \bar{L}_l \sigma^{\mu\nu} U_r + g_{r41} \bar{E}_r Q_l \bar{U}_r L_l + g_{r41}^* \bar{Q}_l E_r \bar{L}_l U_r \\
& + g_{r42} \bar{U}_r \sigma_{\mu\nu} Q_l \bar{E}_r \sigma^{\mu\nu} L_l + g_{r42}^* \bar{Q}_l \sigma_{\mu\nu} U_r \bar{L}_l \sigma^{\mu\nu} E_r + g_{r43} \bar{U}_r Q_l \bar{E}_r L_l + g_{r43}^* \bar{Q}_l U_r \bar{L}_l E_r + g_{r44} \bar{L}_l \sigma_{\mu\nu} Q_l^c \bar{U}_r^c \sigma^{\mu\nu} E_r + g_{r44}^* \bar{Q}_l^c \sigma_{\mu\nu} L_l \bar{E}_r \sigma^{\mu\nu} \\
& U_r^c + g_{r45} \bar{L}_l Q_l^c \bar{U}_r^c E_r + g_{r45}^* \bar{Q}_l^c L_l \bar{E}_r U_r^c + g_{r46} \bar{D}_r \gamma_\mu Q_l^c \bar{L}_l \gamma^\mu U_r^c + g_{r46}^* \bar{Q}_l^c \gamma_\mu D_r \bar{U}_r^c \gamma^\mu L_l + g_{r47} \bar{U}_r \gamma_\mu Q_l^c \bar{L}_l \gamma^\mu D_r^c + g_{r47}^* \bar{Q}_l^c \gamma_\mu U_r \bar{D}_r^c \gamma^\mu L_l \\
& + g_{r48} \bar{L}_l \sigma_{\mu\nu} Q_l^c \bar{D}_r \sigma^{\mu\nu} U_r^c + g_{r48}^* \bar{Q}_l^c \sigma_{\mu\nu} L_l \bar{U}_r^c \sigma^{\mu\nu} D_r + g_{r49} \bar{L}_l Q_l^c \bar{D}_r U_r^c + g_{r49}^* \bar{Q}_l^c L_l \bar{U}_r^c D_r + g_{r50} \bar{L}_l \gamma_\mu Q_l \bar{D}_r \gamma^\mu E_r + g_{r50}^* \bar{Q}_l \gamma_\mu L_l \bar{E}_r \gamma^\mu D_r \\
& + g_{r51} \bar{E}_r \gamma_\mu Q_l^c \bar{D}_r^c \gamma^\mu L_l + g_{r51}^* \bar{Q}_l^c \gamma_\mu E_r \bar{L}_l \gamma^\mu D_r^c + g_{r52} \bar{D}_r \sigma_{\mu\nu} Q_l \bar{L}_l \sigma^{\mu\nu} E_r + g_{r52}^* \bar{Q}_l \sigma_{\mu\nu} D_r \bar{E}_r \sigma^{\mu\nu} L_l + g_{r53} \bar{D}_r Q_l \bar{L}_l E_r + g_{r53}^* \bar{Q}_l D_r \bar{E}_r L_l + \\
& g_{r54} \bar{U}_r \gamma_\mu U_r \bar{U}_r \gamma^\mu U_r + g_{r55} \bar{U}_r^c \sigma_{\mu\nu} U_r \bar{U}_r \sigma^{\mu\nu} U_r^c + g_{r56} \bar{U}_r^c U_r \bar{U}_r U_r^c + g_{r57} \bar{U}_r \gamma_\mu D_r \bar{D}_r \gamma^\mu U_r + g_{r58} \bar{U}_r \gamma_\mu U_r \bar{D}_r \gamma^\mu D_r + g_{r59} \\
& \bar{U}_r^c \sigma_{\mu\nu} D_r \bar{D}_r \sigma^{\mu\nu} U_r^c + g_{r60} \bar{U}_r^c D_r \bar{D}_r U_r^c + g_{r61} \bar{U}_r \gamma_\mu U_r \bar{L}_l \gamma^\mu L_l + g_{r62} \bar{U}_r^c \gamma_\mu L_l \bar{L}_l \gamma^\mu U_r^c + g_{r63} \bar{U}_r \sigma_{\mu\nu} L_l \bar{L}_l \sigma^{\mu\nu} U_r + g_{r64} \bar{U}_r L_l \bar{L}_l U_r + \\
& g_{r65} \bar{U}_r \gamma_\mu E_r \bar{E}_r \gamma^\mu U_r + g_{r66} \bar{U}_r \gamma_\mu U_r \bar{E}_r \gamma^\mu E_r + g_{r67} \bar{U}_r^c \sigma_{\mu\nu} E_r \bar{E}_r \sigma^{\mu\nu} U_r^c + g_{r68} \bar{U}_r^c E_r \bar{E}_r U_r^c + g_{r69} \bar{E}_r \sigma_{\mu\nu} U_r^c \bar{D}_r \sigma^{\mu\nu} U_r^c + g_{r69}^* \bar{U}_r^c \sigma_{\mu\nu} E_r \\
& \bar{U}_r^c \sigma^{\mu\nu} D_r + g_{r70} \bar{E}_r U_r^c \bar{D}_r U_r^c + g_{r70}^* \bar{U}_r^c E_r \bar{U}_r^c D_r + g_{r71} \bar{D}_r \sigma_{\mu\nu} U_r^c \bar{E}_r \sigma^{\mu\nu} U_r^c + g_{r71}^* \bar{U}_r^c \sigma_{\mu\nu} D_r \bar{U}_r^c \sigma^{\mu\nu} E_r + g_{r72} \bar{D}_r U_r^c \bar{E}_r U_r^c + g_{r72}^* \bar{U}_r^c D_r \\
& \bar{U}_r^c E_r + g_{r73} \bar{U}_r \sigma_{\mu\nu} U_r^c \bar{E}_r \sigma^{\mu\nu} D_r^c + g_{r73}^* \bar{U}_r^c \sigma_{\mu\nu} U_r \bar{D}_r^c \sigma^{\mu\nu} E_r + g_{r74} \bar{U}_r U_r^c \bar{E}_r D_r^c + g_{r74}^* \bar{U}_r^c U_r \bar{D}_r^c E_r + g_{r75} \bar{D}_r \gamma_\mu D_r \bar{D}_r \gamma^\mu D_r + g_{r76} \\
& \bar{D}_r^c \sigma_{\mu\nu} D_r \bar{D}_r \sigma^{\mu\nu} D_r^c + g_{r77} \bar{D}_r^c D_r \bar{D}_r D_r^c + g_{r78} \bar{D}_r \gamma_\mu D_r \bar{L}_l \gamma^\mu L_l + g_{r79} \bar{D}_r^c \gamma_\mu L_l \bar{L}_l \gamma^\mu D_r^c + g_{r80} \bar{D}_r \sigma_{\mu\nu} L_l \bar{L}_l \sigma^{\mu\nu} D_r + g_{r81} \bar{D}_r L_l \bar{L}_l D_r + \\
& g_{r82} \bar{D}_r \gamma_\mu E_r \bar{E}_r \gamma^\mu D_r + g_{r83} \bar{D}_r \gamma_\mu D_r \bar{E}_r \gamma^\mu E_r + g_{r84} \bar{D}_r^c \sigma_{\mu\nu} E_r \bar{E}_r \sigma^{\mu\nu} D_r^c + g_{r85} \bar{D}_r^c E_r \bar{E}_r D_r^c + g_{r86} \bar{L}_l \gamma_\mu L_l \bar{L}_l \gamma^\mu L_l + g_{r87} \bar{L}_l^c \sigma_{\mu\nu} L_l \bar{L}_l \sigma^{\mu\nu} \\
& L_l^c + g_{r88} \bar{L}_l^c L_l \bar{L}_l L_l^c + g_{r89} \bar{L}_l \gamma_\mu L_l \bar{E}_r \gamma^\mu E_r + g_{r90} \bar{L}_l^c \gamma_\mu E_r \bar{E}_r \gamma^\mu L_l^c + g_{r91} \bar{L}_l \sigma_{\mu\nu} E_r \bar{E}_r \sigma^{\mu\nu} L_l + g_{r92} \bar{L}_l E_r \bar{E}_r L_l + g_{r93} \bar{E}_r \gamma_\mu E_r \bar{E}_r \gamma^\mu E_r + \\
& g_{r94} \bar{E}_r^c \sigma_{\mu\nu} E_r \bar{E}_r \sigma^{\mu\nu} E_r^c + g_{r95} \bar{E}_r^c E_r \bar{E}_r E_r^c + g_{r96} \Phi \Phi \Phi \Phi^* \Phi^* \Phi^*
\end{aligned}$$

# SM 2 Higgs (Dim 4)

SM with 2 Higgs up to Dimension 4

$$\begin{aligned} & \overline{Q}_l \gamma^\mu D_\mu Q_l + \overline{U}_r \gamma^\mu D_\mu U_r + \overline{D}_r \gamma^\mu D_\mu D_r + \overline{L}_l \gamma^\mu D_\mu L_l + \overline{E}_r \gamma^\mu D_\mu E_r + D_\mu \Phi_1^* D^\mu \Phi_1 + D_\mu \Phi_2^* D^\mu \Phi_2 + G_{C\mu\nu} G_C^{\mu\nu} \\ & + \theta_0 \varepsilon_{\alpha\beta\gamma\delta} G_C^{\alpha\beta} G_C^{\gamma\delta} + W_{L\mu\nu} W_L^{\mu\nu} + \theta_1 \varepsilon_{\alpha\beta\gamma\delta} W_L^{\alpha\beta} W_L^{\gamma\delta} + B_{Y\mu\nu} B_Y^{\mu\nu} \end{aligned}$$

$$\mu_{r0} \Phi_1 \Phi_1^* + \mu_1 \Phi_2 \Phi_1 + \mu_1^* \Phi_1^* \Phi_2^* + \mu_{r2} \Phi_2 \Phi_2^*$$

$$\begin{aligned} & \lambda_{r3} \Phi_1 \Phi_1 \Phi_1^* \Phi_1^* + \lambda_4 \Phi_2 \Phi_1 \Phi_1 \Phi_1^* + \lambda_4^* \Phi_1 \Phi_1^* \Phi_1^* \Phi_2^* + \lambda_{r5} \Phi_1 \Phi_2 \Phi_1^* \Phi_2^* + \lambda_6 \Phi_2 \Phi_2 \Phi_1 \Phi_1 + \lambda_6^* \Phi_1^* \Phi_1^* \Phi_2^* \Phi_2^* \\ & + \lambda_7 \Phi_2 \Phi_2 \Phi_1 \Phi_2^* + \lambda_7^* \Phi_2 \Phi_1^* \Phi_2^* \Phi_2^* + \lambda_{r8} \Phi_2 \Phi_2 \Phi_2^* \Phi_2^* \end{aligned}$$

$$\begin{aligned} & y_9 \Phi_1 \overline{U}_r Q_l + y_9^* \Phi_1^* \overline{Q}_l U_r + y_{10} \Phi_2^* \overline{U}_r Q_l + y_{10}^* \Phi_2 \overline{Q}_l U_r + y_{11} \Phi_1^* \overline{D}_r Q_l + y_{11}^* \Phi_1 \overline{Q}_l D_r + y_{12} \Phi_2 \overline{D}_r Q_l + y_{12}^* \Phi_2^* \\ & \overline{Q}_l D_r + y_{13} \Phi_1^* \overline{E}_r L_l + y_{13}^* \Phi_1 \overline{L}_l E_r + y_{14} \Phi_2 \overline{E}_r L_l + y_{14}^* \Phi_2^* \overline{L}_l E_r \end{aligned}$$

# SM 2 Higgs (Dim 6)

$$\overline{Q}_l \gamma^\mu D_\mu Q_l + \overline{U}_r \gamma^\mu D_\mu U_r + \overline{D}_r \gamma^\mu D_\mu D_r + \overline{L}_l \gamma^\mu D_\mu L_l + \overline{E}_r \gamma^\mu D_\mu E_r + D_\mu \Phi_1^* D^\mu \Phi_1 + D_\mu \Phi_2^* D^\mu \Phi_2 + G_{C\mu\nu} G_C^{\mu\nu} + \theta_0 \epsilon_{\alpha\beta\gamma\delta} G_C^{\alpha\beta} G_C^{\gamma\delta} + W_{L\mu\nu} W_L^{\mu\nu} + \theta_1 \epsilon_{\alpha\beta\gamma\delta} W_L^{\alpha\beta} W_L^{\gamma\delta} + B_{Y\mu\nu} B_Y^{\mu\nu}$$

$$\mu_{r0} \Phi_1 \Phi_1^* + \mu_1 \Phi_2 \Phi_1 + \mu_1^* \Phi_1^* \Phi_2^* + \mu_{r2} \Phi_2 \Phi_2^*$$

$$\lambda_{r3} \Phi_1 \Phi_1 \Phi_1^* \Phi_1^* + \lambda_4 \Phi_2 \Phi_1 \Phi_1 \Phi_1^* + \lambda_4^* \Phi_1 \Phi_1^* \Phi_1^* \Phi_2^* + \lambda_{r5} \Phi_1 \Phi_2 \Phi_1^* \Phi_2^* + \lambda_6 \Phi_2 \Phi_2 \Phi_1 \Phi_1 + \lambda_6^* \Phi_1^* \Phi_1^* \Phi_2^* \Phi_2^* + \lambda_7 \Phi_2 \Phi_2 \Phi_1 \Phi_1^* + \lambda_7^* \Phi_2 \Phi_1^* \Phi_2^* \Phi_2^* + \lambda_{r8} \Phi_2 \Phi_2 \Phi_2^* \Phi_2^*$$

$$y_9 \Phi_1 \overline{U}_r Q_l + y_9^* \Phi_1^* \overline{Q}_l U_r + y_{10} \Phi_2^* \overline{U}_r Q_l + y_{10}^* \Phi_2 \overline{Q}_l U_r + y_{11} \Phi_1^* \overline{D}_r Q_l + y_{11}^* \Phi_1 \overline{Q}_l D_r + y_{12} \Phi_2 \overline{D}_r Q_l + y_{12}^* \Phi_2^* \overline{Q}_l D_r + y_{13} \Phi_1^* \overline{E}_r L_l + y_{13}^* \Phi_1 \overline{L}_l E_r + y_{14} \Phi_2 \overline{E}_r L_l + y_{14}^* \Phi_2^* \overline{L}_l E_r +$$

$$y_{15} \Phi_1 \Phi_1 \overline{L}_l L_l^c + y_{15}^* \Phi_1^* \Phi_1^* \overline{L}_l^c L_l + y_{16} \Phi_2^* \Phi_1 \overline{L}_l L_l^c + y_{16}^* \Phi_2 \Phi_1^* \overline{L}_l^c L_l + y_{17} \Phi_2^* \Phi_2^* \overline{L}_l L_l^c + y_{17}^* \Phi_2 \Phi_2 \overline{L}_l^c L_l +$$

$$\begin{aligned}
& y_{18} \Phi_1^* \Phi_1 \Phi_1 \bar{U}_r Q_l + y_{18}^* \Phi_1 \Phi_1^* \Phi_1^* \bar{Q}_l U_r + y_{19} \Phi_1^* \Phi_2^* \Phi_1 \bar{U}_r Q_l + y_{19}^* \Phi_1 \Phi_2 \Phi_1^* \bar{Q}_l U_r + y_{20} \Phi_1^* \Phi_2^* \Phi_2^* \bar{U}_r Q_l + y_{20}^* \Phi_1 \Phi_2 \Phi_2 \bar{Q}_l U_r + \\
& y_{21} \Phi_1 \Phi_1 \Phi_2 \bar{U}_r Q_l + y_{21}^* \Phi_1^* \Phi_1^* \Phi_2^* \bar{Q}_l U_r + y_{22} \Phi_2^* \Phi_1 \Phi_2 \bar{U}_r Q_l + y_{22}^* \Phi_2 \Phi_1^* \Phi_2^* \bar{Q}_l U_r + y_{23} \Phi_2^* \Phi_2^* \Phi_2 \bar{U}_r Q_l + y_{23}^* \Phi_2 \Phi_2 \Phi_2^* \bar{Q}_l U_r + \\
& y_{24} \Phi_1^* \Phi_1^* \Phi_1 \bar{D}_r Q_l + y_{24}^* \Phi_1 \Phi_1 \Phi_1^* \bar{Q}_l D_r + y_{25} \Phi_1^* \Phi_1^* \Phi_2^* \bar{D}_r Q_l + y_{25}^* \Phi_1 \Phi_1 \Phi_2 \bar{Q}_l D_r + y_{26} \Phi_1^* \Phi_1 \Phi_2 \bar{D}_r Q_l + y_{26}^* \Phi_1 \Phi_1^* \Phi_2^* \bar{Q}_l D_r + \\
& y_{27} \Phi_1^* \Phi_2^* \Phi_2 \bar{D}_r Q_l + y_{27}^* \Phi_1 \Phi_2 \Phi_2^* \bar{Q}_l D_r + y_{28} \Phi_1 \Phi_2 \Phi_2 \bar{D}_r Q_l + y_{28}^* \Phi_1^* \Phi_2^* \Phi_2^* \bar{Q}_l D_r + y_{29} \Phi_2^* \Phi_2 \Phi_2 \bar{D}_r Q_l + y_{29}^* \Phi_2 \Phi_2^* \Phi_2^* \bar{Q}_l D_r + \\
& y_{30} \Phi_1^* \Phi_1^* \Phi_1 \bar{E}_r L_l + y_{30}^* \Phi_1 \Phi_1 \Phi_1^* \bar{L}_l E_r + y_{31} \Phi_1^* \Phi_1^* \Phi_2^* \bar{E}_r L_l + y_{31}^* \Phi_1 \Phi_1 \Phi_2 \bar{L}_l E_r + y_{32} \Phi_1^* \Phi_1 \Phi_2 \bar{E}_r L_l + y_{32}^* \Phi_1 \Phi_1^* \Phi_2^* \bar{L}_l E_r + y_{33} \\
& \Phi_1^* \Phi_2^* \Phi_2 \bar{E}_r L_l + y_{33}^* \Phi_1 \Phi_2 \Phi_2^* \bar{L}_l E_r + y_{34} \Phi_1 \Phi_2 \Phi_2 \bar{E}_r L_l + y_{34}^* \Phi_1^* \Phi_2^* \Phi_2^* \bar{L}_l E_r + y_{35} \Phi_2^* \Phi_2 \Phi_2 \bar{E}_r L_l + y_{35}^* \Phi_2 \Phi_2^* \Phi_2^* \bar{L}_l E_r
\end{aligned}$$

$$\begin{aligned}
& g_{r36} \bar{Q}_l \gamma_\mu Q_l \bar{Q}_l \gamma^\mu Q_l + g_{r37} \bar{Q}_l^c \sigma_{\mu\nu} Q_l \bar{Q}_l \sigma^{\mu\nu} Q_l^c + g_{r38} \bar{Q}_l^c Q_l \bar{Q}_l Q_l^c + g_{r39} \bar{Q}_l \gamma_\mu Q_l \bar{U}_r \gamma^\mu U_r + g_{r40} \bar{Q}_l^c \gamma_\mu U_r \bar{U}_r \gamma^\mu Q_l^c + g_{r41} \bar{Q}_l \sigma_{\mu\nu} U_r \bar{U}_r \sigma^{\mu\nu} \\
& Q_l + g_{r42} \bar{Q}_l U_r \bar{U}_r Q_l + g_{r43} \bar{Q}_l \gamma_\mu Q_l \bar{D}_r \gamma^\mu D_r + g_{r44} \bar{Q}_l^c \gamma_\mu D_r \bar{D}_r \gamma^\mu Q_l^c + g_{r45} \bar{Q}_l \sigma_{\mu\nu} D_r \bar{D}_r \sigma^{\mu\nu} Q_l + g_{r46} \bar{Q}_l D_r \bar{D}_r Q_l + g_{r47} \bar{Q}_l \gamma_\mu L_l \bar{L}_l \gamma^\mu Q_l \\
& + g_{r48} \bar{Q}_l \gamma_\mu Q_l \bar{L}_l \gamma^\mu L_l + g_{r49} \bar{Q}_l^c \sigma_{\mu\nu} L_l \bar{L}_l \sigma^{\mu\nu} Q_l^c + g_{r50} \bar{Q}_l^c L_l \bar{L}_l Q_l^c + g_{r51} \bar{Q}_l \gamma_\mu Q_l \bar{E}_r \gamma^\mu E_r + g_{r52} \bar{Q}_l^c \gamma_\mu E_r \bar{E}_r \gamma^\mu Q_l^c + g_{r53} \bar{Q}_l \sigma_{\mu\nu} E_r \bar{E}_r \sigma^{\mu\nu} Q_l \\
& + g_{r54} \bar{Q}_l E_r \bar{E}_r Q_l + g_{55} \bar{Q}_l \sigma_{\mu\nu} Q_l^c \bar{L}_l \sigma^{\mu\nu} Q_l^c + g_{55}^* \bar{Q}_l^c \sigma_{\mu\nu} Q_l \bar{Q}_l^c \sigma^{\mu\nu} L_l + g_{56} \bar{Q}_l Q_l^c \bar{L}_l Q_l^c + g_{56}^* \bar{Q}_l^c Q_l \bar{Q}_l^c L_l + g_{57} \bar{D}_r \sigma_{\mu\nu} Q_l \bar{U}_r \sigma^{\mu\nu} Q_l + g_{57}^* \\
& \bar{Q}_l \sigma_{\mu\nu} D_r \bar{Q}_l \sigma^{\mu\nu} U_r + g_{58} \bar{D}_r Q_l \bar{U}_r Q_l + g_{58}^* \bar{Q}_l D_r \bar{Q}_l U_r + g_{59} \bar{U}_r \sigma_{\mu\nu} Q_l \bar{D}_r \sigma^{\mu\nu} Q_l + g_{59}^* \bar{Q}_l \sigma_{\mu\nu} U_r \bar{Q}_l \sigma^{\mu\nu} D_r + g_{60} \bar{U}_r Q_l \bar{D}_r Q_l + g_{60}^* \bar{Q}_l U_r \\
& \bar{Q}_l D_r + g_{61} \bar{Q}_l \sigma_{\mu\nu} Q_l^c \bar{U}_r^c \sigma^{\mu\nu} D_r + g_{61}^* \bar{Q}_l^c \sigma_{\mu\nu} Q_l \bar{D}_r \sigma^{\mu\nu} U_r^c + g_{62} \bar{Q}_l Q_l^c \bar{U}_r^c D_r + g_{62}^* \bar{Q}_l^c Q_l \bar{D}_r U_r^c + g_{63} \bar{E}_r \gamma_\mu Q_l^c \bar{U}_r \gamma^\mu Q_l^c + g_{63}^* \bar{Q}_l^c \gamma_\mu E_r \\
& \bar{Q}_l^c \gamma^\mu U_r + g_{64} \bar{U}_r \gamma_\mu Q_l^c \bar{E}_r \gamma^\mu Q_l^c + g_{64}^* \bar{Q}_l^c \gamma_\mu U_r \bar{Q}_l^c \gamma^\mu E_r + g_{65} \bar{Q}_l \sigma_{\mu\nu} Q_l^c \bar{E}_r \sigma^{\mu\nu} U_r^c + g_{65}^* \bar{Q}_l^c \sigma_{\mu\nu} Q_l \bar{U}_r^c \sigma^{\mu\nu} E_r + g_{66} \bar{Q}_l Q_l^c \bar{E}_r U_r^c + g_{66}^* \\
& \bar{Q}_l^c Q_l \bar{U}_r^c E_r + g_{67} \bar{E}_r \sigma_{\mu\nu} Q_l \bar{U}_r \sigma^{\mu\nu} L_l + g_{67}^* \bar{Q}_l \sigma_{\mu\nu} E_r \bar{L}_l \sigma^{\mu\nu} U_r + g_{68} \bar{E}_r Q_l \bar{U}_r L_l + g_{68}^* \bar{Q}_l E_r \bar{L}_l U_r + g_{69} \bar{U}_r \sigma_{\mu\nu} Q_l \bar{E}_r \sigma^{\mu\nu} L_l + g_{69}^* \bar{Q}_l \sigma_{\mu\nu} U_r \bar{L}_l \\
& \sigma^{\mu\nu} E_r + g_{70} \bar{U}_r Q_l \bar{E}_r L_l + g_{70}^* \bar{Q}_l U_r \bar{L}_l E_r + g_{71} \bar{L}_l \sigma_{\mu\nu} Q_l^c \bar{U}_r^c \sigma^{\mu\nu} E_r + g_{71}^* \bar{Q}_l^c \sigma_{\mu\nu} L_l \bar{E}_r \sigma^{\mu\nu} U_r^c + g_{72} \bar{L}_l Q_l^c \bar{U}_r^c E_r + g_{72}^* \bar{Q}_l^c L_l \bar{E}_r U_r^c + g_{73} \bar{D}_r \\
& \gamma_\mu Q_l^c \bar{L}_l \gamma^\mu U_r^c + g_{73}^* \bar{Q}_l^c \gamma_\mu D_r \bar{U}_r^c \gamma^\mu L_l + g_{74} \bar{U}_r \gamma_\mu Q_l^c \bar{L}_l \gamma^\mu D_r^c + g_{74}^* \bar{Q}_l^c \gamma_\mu U_r \bar{D}_r^c \gamma^\mu L_l + g_{75} \bar{L}_l \sigma_{\mu\nu} Q_l^c \bar{D}_r \sigma^{\mu\nu} U_r^c + g_{75}^* \bar{Q}_l^c \sigma_{\mu\nu} L_l \bar{U}_r^c \sigma^{\mu\nu} D_r +
\end{aligned}$$

$$\begin{aligned}
& g_{76} \bar{L}_i Q_i^c \bar{D}_r U_r^c + g_{76}^* \bar{Q}_i^c L_i \bar{U}_r^c D_r + g_{77} \bar{L}_i \gamma_\mu Q_i \bar{D}_r \gamma^\mu E_r + g_{77}^* \bar{Q}_i \gamma_\mu L_i \bar{E}_r \gamma^\mu D_r + g_{78} \bar{E}_r \gamma_\mu Q_i^c \bar{D}_r^c \gamma^\mu L_i + g_{78}^* \bar{Q}_i^c \gamma_\mu E_r \bar{L}_i \gamma^\mu D_r^c + g_{79} \bar{D}_r \sigma_{\mu\nu} \\
& Q_i \bar{L}_i \sigma^{\mu\nu} E_r + g_{79}^* \bar{Q}_i \sigma_{\mu\nu} D_r \bar{E}_r \sigma^{\mu\nu} L_i + g_{80} \bar{D}_r Q_i \bar{L}_i E_r + g_{80}^* \bar{Q}_i D_r \bar{E}_r L_i + g_{81} \bar{U}_r \gamma_\mu U_r \bar{U}_r \gamma^\mu U_r + g_{82} \bar{U}_r^c \sigma_{\mu\nu} U_r \bar{U}_r \sigma^{\mu\nu} U_r^c + g_{83} \bar{U}_r^c U_r \bar{U}_r \\
& U_r^c + g_{84} \bar{U}_r \gamma_\mu D_r \bar{D}_r \gamma^\mu U_r + g_{85} \bar{U}_r \gamma_\mu U_r \bar{D}_r \gamma^\mu D_r + g_{86} \bar{U}_r^c \sigma_{\mu\nu} D_r \bar{D}_r \sigma^{\mu\nu} U_r^c + g_{87} \bar{U}_r^c D_r \bar{D}_r U_r^c + g_{88} \bar{U}_r \gamma_\mu U_r \bar{L}_i \gamma^\mu L_i + g_{89} \bar{U}_r^c \gamma_\mu L_i \\
& \bar{L}_i \gamma^\mu U_r^c + g_{90} \bar{U}_r \sigma_{\mu\nu} L_i \bar{L}_i \sigma^{\mu\nu} U_r + g_{91} \bar{U}_r L_i \bar{L}_i U_r + g_{92} \bar{U}_r \gamma_\mu E_r \bar{E}_r \gamma^\mu U_r + g_{93} \bar{U}_r \gamma_\mu U_r \bar{E}_r \gamma^\mu E_r + g_{94} \bar{U}_r^c \sigma_{\mu\nu} E_r \bar{E}_r \sigma^{\mu\nu} U_r^c + g_{95} \bar{U}_r^c E_r \\
& \bar{E}_r U_r^c + g_{96} \bar{E}_r \sigma_{\mu\nu} U_r^c \bar{D}_r \sigma^{\mu\nu} U_r^c + g_{96}^* \bar{U}_r^c \sigma_{\mu\nu} E_r \bar{U}_r^c \sigma^{\mu\nu} D_r + g_{97} \bar{E}_r U_r^c \bar{D}_r U_r^c + g_{97}^* \bar{U}_r^c E_r \bar{U}_r^c D_r + g_{98} \bar{D}_r \sigma_{\mu\nu} U_r^c \bar{E}_r \sigma^{\mu\nu} U_r^c + g_{98}^* \\
& \bar{U}_r^c \sigma_{\mu\nu} D_r \bar{U}_r^c \sigma^{\mu\nu} E_r + g_{99} \bar{D}_r U_r^c \bar{E}_r U_r^c + g_{99}^* \bar{U}_r^c D_r \bar{U}_r^c E_r + g_{100} \bar{U}_r \sigma_{\mu\nu} U_r^c \bar{E}_r \sigma^{\mu\nu} D_r^c + g_{100}^* \bar{U}_r^c \sigma_{\mu\nu} U_r \bar{D}_r^c \sigma^{\mu\nu} E_r + g_{101} \bar{U}_r U_r^c \bar{E}_r D_r^c + \\
& g_{101}^* \bar{U}_r^c U_r \bar{D}_r^c E_r + g_{102} \bar{D}_r \gamma_\mu D_r \bar{D}_r \gamma^\mu D_r + g_{103} \bar{D}_r^c \sigma_{\mu\nu} D_r \bar{D}_r \sigma^{\mu\nu} D_r^c + g_{104} \bar{D}_r^c D_r \bar{D}_r D_r^c + g_{105} \bar{D}_r \gamma_\mu D_r \bar{L}_i \gamma^\mu L_i + g_{106} \bar{D}_r^c \gamma_\mu L_i \bar{L}_i \gamma^\mu \\
& D_r^c + g_{107} \bar{D}_r \sigma_{\mu\nu} L_i \bar{L}_i \sigma^{\mu\nu} D_r + g_{108} \bar{D}_r L_i \bar{L}_i D_r + g_{109} \bar{D}_r \gamma_\mu E_r \bar{E}_r \gamma^\mu D_r + g_{110} \bar{D}_r \gamma_\mu D_r \bar{E}_r \gamma^\mu E_r + g_{111} \bar{D}_r^c \sigma_{\mu\nu} E_r \bar{E}_r \sigma^{\mu\nu} D_r^c + g_{112} \\
& \bar{D}_r^c E_r \bar{E}_r D_r^c + g_{113} \bar{L}_i \gamma_\mu L_i \bar{L}_i \gamma^\mu L_i + g_{114} \bar{L}_i^c \sigma_{\mu\nu} L_i \bar{L}_i \sigma^{\mu\nu} L_i^c + g_{115} \bar{L}_i^c L_i \bar{L}_i L_i^c + g_{116} \bar{L}_i \gamma_\mu L_i \bar{E}_r \gamma^\mu E_r + g_{117} \bar{L}_i^c \gamma_\mu E_r \bar{E}_r \gamma^\mu L_i^c + g_{118} \bar{L}_i \\
& \sigma_{\mu\nu} E_r \bar{E}_r \sigma^{\mu\nu} L_i + g_{119} \bar{L}_i E_r \bar{E}_r L_i + g_{120} \bar{E}_r \gamma_\mu E_r \bar{E}_r \gamma^\mu E_r + g_{121} \bar{E}_r^c \sigma_{\mu\nu} E_r \bar{E}_r \sigma^{\mu\nu} E_r^c + g_{122} \bar{E}_r^c E_r \bar{E}_r E_r^c + g_{123} \Phi_1 \Phi_1 \Phi_1 \Phi_1^* \Phi_1^* \Phi_1^* + \\
& g_{124} \Phi_2 \Phi_1 \Phi_1 \Phi_1 \Phi_1^* \Phi_1^* + g_{124}^* \Phi_1 \Phi_1 \Phi_1^* \Phi_1^* \Phi_1^* \Phi_2^* + g_{125} \Phi_1 \Phi_1 \Phi_2 \Phi_1^* \Phi_1^* \Phi_2^* + g_{126} \Phi_2 \Phi_2 \Phi_1 \Phi_1 \Phi_1 \Phi_1^* + g_{126}^* \Phi_1 \Phi_1^* \Phi_1^* \Phi_1^* \Phi_2^* \\
& \Phi_2^* + g_{127} \Phi_2 \Phi_2 \Phi_1 \Phi_1 \Phi_2^* \Phi_1^* + g_{127}^* \Phi_1 \Phi_2 \Phi_1^* \Phi_1^* \Phi_2^* \Phi_2^* + g_{128} \Phi_1 \Phi_2 \Phi_2 \Phi_1^* \Phi_2^* \Phi_2^* + g_{129} \Phi_2 \Phi_2 \Phi_2 \Phi_1 \Phi_1 \Phi_1 + g_{129}^* \Phi_1^* \Phi_1^* \Phi_1^* \\
& \Phi_2^* \Phi_2^* \Phi_2^* + g_{130} \Phi_2 \Phi_2 \Phi_2 \Phi_1 \Phi_1 \Phi_2^* + g_{130}^* \Phi_2 \Phi_1^* \Phi_1^* \Phi_2^* \Phi_2^* \Phi_2^* + g_{131} \Phi_2 \Phi_2 \Phi_2 \Phi_1 \Phi_2^* \Phi_2^* + g_{131}^* \Phi_2 \Phi_2 \Phi_1^* \Phi_2^* \Phi_2^* \Phi_2^* + g_{132} \Phi_2 \\
& \Phi_2 \Phi_2 \Phi_2^* \Phi_2^* \Phi_2^*
\end{aligned}$$



# GUI

- For now done through web browser using Wt
- In the future, can be installed on a local server
- Can also be run on a stand alone computer
- Output is in MathML, (should) work on any mobile device

# Future Work

- Symmetry Breaking
- Read/Write model from/to a file
- Connect to FeynRules
- GUI of Dynkin Diagram of Reps
- Discrete Groups other than  $Z_n$